CONVERSIONS & TABLES:

Power definitions. 02: 09: SI - units. 14: Metric conversions, - feet, inches, fractions and tool sizes. 39: United States - weights and measures. British [Imperial] - SI conversions. 54: 71: Kilowatts [kW] - Horse power [hp] - Energy. 74: Temperature. 77: Statistical tables. 80: Angles, geometry & area measurement. 108: Parabola construction. Triangulation. 115: Four-figure trigonometrical tables. 122: Laying-out dimensions. 128: 138: Rectangular box construction. 140: Pulleys, pulley speeds & belts. 145: Interest tables, investment appraisal, NPV & discount factors. [see also: Appraisal of Projects in Developing Countries. ODA HMSO London UK. 1988. 0-11-5802568]

Power

7.1 POWER GENERALLY

7.1.1 Definition

Power is a rate of doing work. It requires more power to move a load quickly than slowly, although the work done may be the same in each case. If a force or a load moves over a distance, energy is consumed and work is done. In other words work = force \times distance, and rate of work, or power = work \div time.

7.1.2 Units

In the past, before the development of mechanical engines, power was measured in relation to the rate of work of the horse. Hence the unit of power came to be known as the horsepower (hp). The scientific unit of power is the watt (W), and because this is small it is very often expressed as the kilowatt (kW). The unit of work or energy corresponding to the watt is the joule (J), which is defined as the work done when a force of one newton (1N) moves through a distance of one metre (1 m). Watts = joules per second.

 $J = N \times m$ W = J/s kW = 1000 W

The horsepower, which was originally defined in terms of poundfoot units, is equivalent to 746 W. The metric hp is 735.5 W.

7.1.3 Brake Horsepower

The brake horsepower of a power unit defines its power output. The name derives from the original method of measuring the output power of an engine by causing it to work against a brake whose loading could be measured. The efficiency of an engine is the ratio of its power output to its power input.

7.2 LIVE POWER

7.2.1 Human Power

While the human physique is capable of short bursts of intense power, the sustained energy output over a prolonged period, such as might be required for pumping or load haulage or other similar labouring activity, is about 60 W.

7.2.2 Animal Power

Draught animals can provide power for ploughing and other agricultural operations, transport and water lifting. Table 7.1 gives the power output of some animals.

| | 1 4010 7. | 1 minus po | | |
|-------------|----------------|---------------------|-----------------------|-----------|
| Animal | Weight (kg) | Draft force (kg) | Ave. speed (m/sec) | Power (W) |
| Heavy horse | 680-1200 | 50-120 | 0.7-1.25 | 350-1500 |
| Light horse | 400-700 | 45–78 | 0.8-1.40 | 370-1080 |
| Mule | 350-500 | 50-60 | 0.9-1.00 | 450- 600 |
| Donkey | 200-300 | 30-40 | 0.7 | 250 |
| Cow | 400-600 | 50-60 | 0.7 | 350 |
| Bullock | 500-900 | 60-80 | 0.6-0.80 | 360- 640 |

Table 7.1 Animal power.

Source: Reproduced from Economics and Power Requirements of Small Irrigation Pumps in Bangladesh and Egypt, by David Birch, Institute of Irrigation Studies, University of Southampton, 1979. Sources of information: (1) S. B. Watt, Chinese Chain and Washer Pumps, IT Publications; and (2) Civil Engineers in Management in the Community, a Conference at N.E. London Polytechnic.

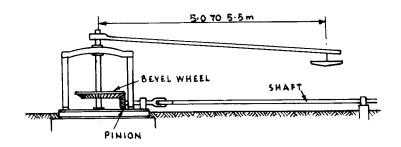


Figure 7.1 Horse gear.

It is often assumed that an animal working on a circular track can exert a force of one tenth of its weight at a speed of 0.7 m/s. To enable an animal to walk in a circular track the diameter of the walk should not be less than 7.5 m; 9-10 m would be still better. Figure 7.1 gives a sketch of animal gear suitable for water raising.

7.3 WIND POWER

7.3.1 Power in the Wind

The power which can be extracted from the wind by a windmill is, theoretically:

$$W = 0.373 AV^3 W$$

where A is the swept area of the rotating blades in square metres and V is the velocity of the wind in metres per second. A well-made propeller or rotor will extract 30-40 per cent of the wind energy; if the efficiency is, say, 0.35, the power is given by:

$$W = 0.131 AV^3 W$$

7.3.2 Windmills

Although the initial cost of a windmill is higher than the equivalent powered petrol or diesel engine, having no fuel costs and minimal maintenance, running costs are very low. A well-designed windmill will start in a light breeze of under 2 m/sec velocity, and must be able to withstand winds of up to 30 m/sec. A moderate breeze is about 7 m/sec, a strong breeze is about 12 m/sec and 15 m/sec is a near gale. Towers are usually from 6 to 20 m in height, and the top of the tower must always be at least 5 m higher than any surrounding obstructions to wind flow.

7.3.3 Windmills for Pumping

The most common use of windmills is for pumping water, but they are also used for generating electricity. When used for pumping, the pump must be matched to the wind machine. Storage capacity for pumped water is necessary as winds are variable and the machine may not work every day. Table 7.2 gives some wind pump performance figures for Kijito windmill pumps manufactured in Kenya.

Table 7.2 Wind pump performance.*

| Rotor dia. | Rotor dia. Total head (m) | | | | | | | | | |
|------------|---------------------------|-----------|----|----|----|-----|-----|-----|-----|-----|
| (m) | 15 | <i>30</i> | 45 | 60 | 90 | 120 | 150 | 180 | 210 | 240 |
| 3.7 | 45 | 20 | 13 | 9 | 6 | 4 | _ | _ | | |
| 4.9 | 75 | 30 | 20 | 15 | 10 | 6 | 4 | 3 | _ | _ |
| 6.1 | 125 | 55 | 35 | 25 | 17 | 11 | 7 | 5 | 3 | _ |
| 7.3 | 180 | 80 | 52 | 38 | 24 | 16 | 11 | 8 | 5 | 3 |

^{*} Output in m³/day for an average wind speed of 3.5 m/sec.

7.4 WATER POWER

7.4.1 Power from Water

The theoretical power in kilowatts developed by a flow of water of Q l/sec falling through a vertical distance H m is given by:

$$W = \frac{QH}{102} \text{ kW}$$

In practice energy is lost through mechanical and electrical friction, and sometimes, through leakage of water. The actual power output is less than the theoretical power, and the ratio of actual to theoretical power is the efficiency of the system converting the power. If k = efficiency, then actual power is given by:

$$W = k \cdot \frac{QH}{102} kW$$

7.5 OTHER FORMS OF POWER

7.5.1 Solar Power

The most practical form of solar power development for use on a small scale in rural areas is the solar or photovoltaic cell which transforms sunlight directly into electrical energy. In this system, silicon solar cells, usually 100 mm dia., are connected in groups known as modules, several modules being mounted in a panel known as an array.

Under a solar irradiance of 1 kW/m² a single cell will give about 2 ampères (A) at 0.5 volts (V), or 1 W of electrical energy. An array of 144 cells will therefore produce about 100–120 W for an irradiance of 1 kW/m².

7.5.2 Solar Pumping

Solar pumps have been used successfully in a number of countries. Initial costs are high and in 1982 were about US\$20 per peak watt electrical output. Operation is very cheap because there are no fuel costs, and very little maintenance is required.

7.5.3 Petrol and Diesel Engines

The small petrol and diesel engine is still popular as a power unit in rural areas. Rising fuel costs make operation expensive. The brake horsepower of an engine is the power developed at its drive shaft, under normal operating conditions.

Engines are usually rated by the manufacturers at sea level and at

an ambient temperature of 15°C. If engines are used at higher altitudes or higher ambient temperatures, the power output is reduced. The percentage reductions to be applied to diesel engines are given in Table 7.4.

Table 7.4 Diesel engine reduction of power with altitude and temperature.*

| Metres above | | Temperature (°C) | | | | | | | |
|--------------|------|------------------|------|------|------|------|------|--|--|
| sea level | 15 | 20 | 25 | 30 | 35 | 40 | 45 | | |
| 500 | 1.9 | 2.8 | 3.7 | 4.6 | 5.5 | 6.4 | 7.3 | | |
| 1000 | 6.9 | 7.8 | 8.7 | 9.6 | 10.5 | 11.4 | 12.3 | | |
| 1500 | 11.9 | 12.8 | 13.7 | 14.6 | 15.5 | 16.4 | 17.3 | | |
| 2000 | 16.9 | 17.8 | 18.7 | 19.6 | 20.5 | 21.4 | 22.3 | | |
| 2500 | 21.9 | 22.8 | 23.7 | 24.6 | 25.5 | 26.4 | 27.3 | | |

Percentage reduction of power for heights above sea level and temperatures above 15°C.

For continuous use, reduce the normal rating by 25 per cent.

Example

A diesel engine rated at 18 bhp is to be used at an altitude of 2000 m above sea level, during daylight hours when the average ambient temperature is 22.5° C. From Table 7.4 the percentage reduction is between 17.8 and 18.7, which, by interpolation is 18.25, and the reduced output is therefore $(100-18.25) \times 18/100 = 0.8175 \times 18 = 14.7$ hp. If the engine is to be run continuously, this should be reduced by a further 25%, giving 11 hp.

Specific fuel consumption for a diesel engine is 0.25 l/bhp/hour at full load. At threequarters load it is 0.26 l/bhp/hour and at half load, 0.27 l/bhp/hour.

7.5.4 Electric Motors

Wherever electric power is available, electric motors can be used. Power supply is usually alternating (a.c.), and motors are rated in kilovolt amps (kVA). Power in kilowatts = $kVA \times power factor$. A very wide range of electric motors is available commercially and professional advice should be sought in choosing a motor for a particular purpose. It is very important to specify the frequency of an a.c. supply, together with the operating voltage, and whether the supply is single-phase or three-phase.

7.6 MECHANICAL AIDS

7.6.1 Buoyancy

The buoyancy of a floating object is its resistance to sinking and is measured by the minimum weight required to sink the object, so that it is totally immersed. The uplift on a body immersed in water is equal to the weight of the volume of water which it displaces.

The buoyancy of a closed cylindrical drum of circumference C and length L, both in metres, is approximately $80 C^2 L - W$ in kilogrammes, where W is the weight of the drum in kilogrammes. In practice the safe buoyancy is 90 per cent of the total buoyancy.

7.6.2 Mechanical Advantage Gained by Blocks

The theoretical gain achieved by a hoist consisting of a fixed block and a moveable block is the number of ropes leading to or from the moveable block. In practice energy is used in overcoming friction in the blocks and the actual force P required to lift a weight W is given by:

$$P = \frac{W}{G} (1 + fn)$$

where G is the theoretical gain as above, f is a friction coefficient equal to 0.17 for tackle in average condition, or 0.2 or more for tackle in poor condition, and n is the total number of sheaves (wheels in the blocks) in the tackle.

Basic SI units, prefixes, and most common derived SI units used

Basic SI units

| Quantity | Basic unit | Symbol | |
|------------------|------------|--------|--|
| Length | metre | m | |
| Mass | kilogram | kg | |
| Time | second | s | |
| Electric current | ampère | Α | |
| Temperature | kelvin | Κ | |

SI prefixes

| Prefix | Symbol | Factor | Prefix | Symbol | Factor |
|--------|--------|------------------|--------|--------|-------------------|
| exa | E | 10 ¹⁸ | deci | d | 10-1 |
| peta | Р | 10 ¹⁵ | centi | С | 10-2 |
| tera | Т | 10 ¹² | milli | m | 10 ⁻³ |
| giga | G | 10 ⁹ | micro | μ | 10 ⁻⁶ |
| mega | M | 10 ⁶ | nano | 'n | 10 ^{–9} |
| kilo | k | 10 ³ | pico | р | 10-12 |
| hecto | h | 10 ² | femto | f | 10 ^{–15} |
| deca | da | 10¹ | atto | а | 10 ⁻¹⁸ |

Most common derived SI units

| Quantity | Unit | Symbol | |
|-------------------------|---------------------------|-------------------------|---|
| Area | square metre | m² | - |
| Volume (contents) | cubic metre | m³ | |
| Speed | metre per second | m/s | |
| Acceleration | metre per second, squared | m/s² | |
| Frequency | hertz | Hz (= s ⁻¹) | |
| Pressure | pascal | Pa (= N/m²) | |
| Volume flow | cubic metre per second | m³/s | |
| Mass flow | kilogram per second | kg/s | |
| Density (specific mass) | kilogram per cubic metre | kg/m³ | |
| Force | newton | N (= kg.m/s²) | |
| Energy/heat/work | joule | J (= N.m)* | |
| Power/energy flow | watt | W (J/s) | |
| Energy flux | watt per square metre | W/m² | |
| Calorific value | joule per kilogram | J/kg | |
| (heat of combustion) | | - | |
| Specific heat capacity | joule per kilogram kelvin | J/kg K | |
| Voltage | volt | V (= W/A) | |

^{*} NB The joule can also be written in the form watt second (1J = 1W.s)

Conversion of non-SI units to SI units

Although academic scientists and engineers may be strict in their use of SI units for their calculations, a number of non-SI units are still in everyday use. For example, engines are still sold by cc (cubic centimetres) and hp (horse power), and water-pumping windmill manufacturers often quote in terms of cubic feet of

the same type of equipment there is not always consistency. In order to be able to compare different manufacturers' products, therefore, it is important to be able convert the different data to a common unit. The following tables give some useful conversion factors for many of the common non-SI units.

| Length | | | | | | |
|------------------|---------------------|--------------|----------------------|---------------|--------------|------------------------|
| Unit (symbol) | millimetre (mm) | metre (m) | kilometre (km) | inch (in.) | foot (ft) | mile (m.) |
| | 1 | 0.001 | 10-6 | 0.0394 | 0.0033 | 5.4×10^{-7} |
| | 1000 | 1 | 0.001 | 39.4 | 3.28 | 5.4×10^{-4} |
| | 106 | 1000 | 1 | 39360 | 3280 | 0.5392 |
| | 25.4 | 0.025 | 2.5×10^{-5} | 1 | 0.083 | 1.4 × 10 ⁻⁵ |
| | 305 | 0.305 | 3.0×10^{-4} | 12 | 1 | 1.9 × 10 ⁻⁴ |
| | 1.6×10^{6} | 1609 | 1.609 | 63360 | 5280 | 1 |

Area

| Unit | square metre | hectare | square kilometre | square foot | acre | square mile |
|----------|-------------------|----------------------|------------------------|---------------------|------------------------|------------------------|
| (symbol) | (m²) | (ha) | (km²) | (ft²) | - | (sq. m.) |
| | 1 | 10-4 | 10-6 | 10.76 | 2.5 × 10 ⁻⁴ | 3.9 × 10 ⁻⁷ |
| | 10000 | 1 | 0.01 | 1.1×10^{5} | 2.471 | 3.9×10^{-3} |
| | 106 | 100 | 1 | 1.1×10^{7} | 247.1 | 0.386 |
| | 0.0929 | 9.3×10^{-6} | 9.3 × 10 ^{–8} | 1 | 2.3 × 10 ⁻⁵ | 3.6 × 10− ⁸ |
| | 4047 | 0.4047 | 4×10^{-3} | 43560 | 1 | 1.6×10^{-3} |
| | 2.6×10^6 | 259 | 2.590 | 2.8×10^7 | 640 | 1 |

Volume

| Unit | litre | cubic metre | cubic inch | US gallon | lmperial gallon | cubic foot | |
|----------|--------|----------------------|------------|----------------------|----------------------|------------------------|--|
| (symbol) | (I)* | (m³) | (in³) | (gal) | (gal) | (ft³) | |
| | 1 | 10-3 | 61.02 | 0.264 | 0.220 | 0.0353 | |
| | 1000 | 1 | 6102 | 264 | 220 | 35.31 | |
| | 0.0164 | 1.6 × 10⁻⁵ | 1 | 4.3×10^{-3} | 3.6×10^{-3} | 5.8 × 10 ^{−4} | |
| | 3.785 | 3.8×10^{-3} | 231.1 | 1 | 0.833 | 0.134 | |
| | 4.546 | 4.5×10^{-3} | 277.4 | 1.201 | 1 | 0.160 | |
| | 28.32 | 0.0283 | 1728 | 7.47 | 6.23 | 1 | |

^{*} L in some countries

Mass

| Unit (symbol) | gram (g) | kilogram (kg) | tonne (t) | pound (Ib) | ton - |
|------------------|-----------------|------------------|----------------------|------------------------|------------------------|
| | 1 | 0.001 | 10 ⁻⁶ | 2.2 × 10 ⁻³ | 9.8 × 10 ⁻⁷ |
| | 1000 | 1 | 0.001 | 2.205 | 9.8 × 10 ⁻⁴ |
| | 106 | 1000 | 1 | 2205 | 0.984 |
| | 453.6 | 0.4536 | 4.5×10^{-4} | 1 | 4.5 × 10 ⁻⁴ |
| | 10 ⁶ | 1016 | 1.016 | 2240 | 1 |

Velocity

| Unit | metres per second | kilometres per hour | feet per second | miles per hour | knots |
|----------|----------------------|------------------------|-----------------|----------------|-------|
| (symbol) | (m/s) | (km/h) | (ft/s) | (mph) | (kt) |
| | 1 | 3.60 | 3.28 | 2.237 | 1.942 |
| | 0.278 | 1 | 0.912 | 0.621 | 0.539 |
| | 0.305 | 1.097 | 1 | 0.682 | 0.592 |
| | 0.447 | 1.609 | 1.467 | 1 | 0.868 |
| | 0.566 | 1.853 | 1.689 | 1.152 | 1 |

Frequency

| Unit (symbol) | hertz (Hz) | revolutions per minute (rpm) | radians per second (rad/s) |
|------------------|---------------|---------------------------------|-------------------------------|
| | 1 | 60 | 6.283 |
| | 0.0167 | 1 | 0.1047 |
| | 0.159 | 9.549 | 1 |

| ٠, | | |
|----|----|-----|
| | av | rai |

| Unit (symbol) | litres per minute (l/min) | cubic metres per second (m³/s) | Imperial gallons per minute (gal(Imp)/min) | cubic feet per second (ft³/s) |
|------------------|------------------------------|--------------------------------------|--|-------------------------------------|
| - | 1 | 1.7 × 10 ⁻⁵ | 0.220 | 5.9 × 10 ⁻⁴ |
| | 60 000 | 1 | 13206 | 35.315 |
| | 4.546 | 7.6 × 10 ⁻⁵ | 1 | 2.7×10^{-3} |
| | 1699 | 0.0283 | 373.7 | 1 |

Force

| Unit (symbol) | newton (N) | kilonewton (kN) | kilogram force (kgf) | tonne force (t) | pound force (lbf) | ton force – |
|------------------|---------------|--------------------|-------------------------|----------------------|----------------------|----------------------|
| | 1 | 0.001 | 0.102 | 1 × 10 ⁻⁴ | 0.225 | 1 × 10 ⁻⁴ |
| | 1000 | 1 | 102 | 0.102 | 225 | 0.100 |
| | 9.807 | 0.010 | 1 | 0.001 | 2.205 | 9.8×10^{-4} |
| | 9807 | 9.807 | 1000 | 1 | 2205 | 0.984 |
| | 4.448 | 0.004 | 0.5436 | 4.5×10^{-4} | 1 | 4.5×10^{-4} |
| | 9964 | 9.964 | 1016 | 1.1016 | 2240 | 1 |

Torque

| Unit (symbol) | newton-metre (Nm) | kilonewton-metre (kNm) | foot-pound (ft.lb) |
|------------------|----------------------|---------------------------|-----------------------|
| | 1 | 0.001 | 0.738 |
| | 1000 | 1 | 738 |
| | 1.365 | 1.4×10^{-3} | 1 |

Work/heat/energy (smaller quantities)

| Unit | calorie | joule | watt-hour | British Thermal Unit | footpound force | horsepower- hour |
|----------|-------------------|-------------------|----------------------|-------------------------|--------------------|------------------------|
| (symbol) | (cal) | (J) | (Wh) | (BTU) | (ft.lbf) | (hp.h) |
| | 1 | 4.182 | 1.2 × 10−3 | 3.9 × 10 ⁻³ | 3.088 | 1.6 × 10 ⁻⁶ |
| | 0.239 | 1 | 2.8×10^{-4} | 9.4×10^{-4} | 0.7376 | 3.7×10^{-7} |
| | 860.4 | 3600 | 1 | 3.414 | 2655 | 1.3×10^{-3} |
| | 252 | 1055 | 2.93 | 1 | 778 | 3.9×10^{-4} |
| | 0.324 | 1.356 | 3.8×10^{-4} | 1.3×10^{-3} | 1 | 5.0×10^{-7} |
| | 6.4×10^5 | 2.6×10^{6} | 745.7 | 2546 | 2.0×10^6 | 1 |

Work/heat/energy (larger quantities)

| Unit | kilocalorie | megajoule | kilowatt hour | British Thermal Unit | horsepower- hour |
|----------|-------------|------------------------|------------------------|-------------------------|------------------------|
| (symbol) | (kcal) | (MJ) | (kWh) | (BTU) | (hp.h) |
| | 1 | 4.2 × 10 ⁻³ | 1.2 × 10 ⁻³ | 3.968 | 1.6 × 10 ⁻³ |
| | 239 | 1 | 0.2887 | 947.8 | 0.3725 |
| | 860.4 | 3.600 | 1 | 3414 | 1.341 |
| | 0.252 | 1.1×10^{-3} | 2.9×10^{-4} | 1 | 3.9×10^{-4} |
| | 641.6 | 2.685 | 0.7457 | 2546 | 1 |

| Power | | | | | | |
|----------|------------|------------------------|------------------------|--------------------------|------------------------|--|
| Unit | watt | kilowatt | metric horse- power | foot-pound per second | horse-power | British Thermal Units per minute |
| (symbol) | (W or J/s) | (kW) | (CV) | (ft.lbf/s) | (hp) | (BTU/min) |
| | 1 | 0.001 | 1.4 × 10 ⁻³ | 0.7376 | 1.3 × 10 ⁻³ | 0.0569 |
| | 1000 | 1 | 1.360 | 737.6 | 1.341 | 56.9 |
| | 735 | 0.735 | 1 | 558 | 1.014 | 41.8 |
| | 1.356 | 1.4 × 10 ^{−3} | 1.8 × 10 ^{−3} | 1 | 1.8×10^{-3} | 0.077 |
| | 746 | 0.746 | 0.9860 | 550 | 1 | 42.44 |
| | 17.57 | 0.0176 | 0.0239 | 12.96 | 0.0236 | 1 |

Power flux

| Unit (symbol) | watts per square metre (W/m²) | kilowatts per square metre (kW/m²) | horsepower per square foot (hp/ft²) |
|------------------|-------------------------------|---------------------------------------|--|
| | 1 | 0.001 | 1.2×10^{-4} |
| | 1000 | 1 | 0.1246 |
| | 8023 | 8.023 | 1 |

Calorific value (heat of combustion)

| Unit (symbol) | calories per gram (cal/g) | megajoules per kilogram (MJ/kg) | British thermal units per pound (BTU/lb) |
|------------------|------------------------------|------------------------------------|--|
| | 1 | 4.2 × 10 ^{−3} | 1.8 |
| | 239 | 1 | 430 |
| | 0.556 | 2.3 × 10 ^{−3} | 1 |

Density (specific mass) and (net) calorific value (heat of combustion) of fuels

| | Density (kg/m³) | Calorific value (MJ/kg) |
|-------------------|-----------------|--|
| LPG | 560 | 45.3 |
| Gasoline (petrol) | 720 | 44.0 |
| Kerosene | 806 | 43.1 |
| Diesel oil | 850 | 42.7 |
| Fuel oil | 961 | 40.1 |
| Wood, oven-dried | varies | 16–20 |
| Natural gas | - | 103m^3 at 1013mbar , $0^{\circ}\text{C} = 39.36 \times 10^9\text{J}$ |

NB These values are approximate since the fuels vary in composition and this affects both the density and calorific value.

Replacement values

When trying to compare different fuel options, energy planners often use replacement values, which indicate in a specific situation how much fuel it would take to replace another one. For example, the tonne coal equivalent (tce) would be used to say how much coal it would take to replace a given quanity of oil or natural gas. The table below gives some of the most common equivalence values.

| Fuel | Unit | Tonnes of coal equivalent (tce) | Tonnes of oil equivalent (toe) | Barrels of oil equivalent (boe) | GJ* |
|----------------------|--------------------|---------------------------------------|--------------------------------------|---------------------------------------|--------|
| Coal | tonne | 1.00 | 0.70 | 5.05 | 29.3** |
| Firewood (air-dried) | tonne | 0.46 | 0.32 | 2.34 | 13.6 |
| Kerosene | tonne | 1.47 | 1.03 | 7.43 | 43.1 |
| Natural gas | 1000m ³ | 1.19 | 0.83 | 6.00 | 34.8 |
| Gasoline (petrol) | barrel*** | 0.18 | 0.12 | 0.90 | 5.2 |
| Gasoil/diesel | barrel*** | 0.20 | 0.14 | 1.00 | 5.7 |

^{*} GJ/tonne is numerically equivalent to MJ/kg

^{**} The energy content of 1 tce and 1 toe varies. The values used here are the European Community norms:

¹ tce = $29.31 \times 10^9 \text{J}$ and 1 toe = $41.868 \times 10^9 \text{J}$

^{*** 1} barrel of oil = 42 US gallons = 0.158987m³

Power equivalents

| | 11.100, , . | | ,,. | - · · tn | , , . |
|------------------|-------------|----------------------|-------|----------|-------|
| Mtoe/yr | 1 | 0.02 | 1.55 | 1.43 | 45 |
| Mbd | 50 | 1 | 77 | 71 | 2235 |
| Mtce/yr | 0.65 | 0.013 | 1 | 0.92 | 29 |
| GW _{th} | 0.70 | 0.014 | 1.09 | 1 | 32 |
| PJ/yr | 0.02 | 4.5×10^{-4} | 0.034 | 0.031 | 1 |

Mtce/vr

GW.

PJ/vr

PJ/vr = Petrajoules per year

Mtoe/vr = Million tonnes of oil per year Mbd = Million barrels of oil per day

Mtoe/vr

Mtce/vr = Million tonnes of coal equivalent per year

GW_{th} = Gigawatts thermal (see page 203 for further information)

Mbd

USEFUL CONVERSION FORMULAE & TABLES

To convert Pounds (lb) to Kilogrammes (kg) multiply by 0.4536 and kilogrammes to pounds multiply by 2.205

Water

1 litre weighs 1.00 kg/2.2 lb. 1 gallon weighs 4.53 kg/10 lb.

Gallons to litres: Multiply by 4.546 Litres to gallons: Multiply by 0.22 1 cu ft holds 61/4 gallons & weighs 62.3lb

To convert cubic feet to cubic metres multiply by 0.028

The central figure in the table represents either of the two outside columns, as the case may be i.e. 1 gallon = 4.546 litres or 1 litre = 0.22 gallons. Gallons

1

2

3

4

5

6

7

8

9

0.220

0.440

0.660

0.880

1.100

1.320

1.540

1.760

1.980

Litres

4.546 9.092 13.638 18.184

22.730 27.276

Petrol

31.822 36.368 40.914 1 litre weighs 0.73 kg/1.61 lb. 1 gallon weighs 3.36 kg/7.4 lb. 1 litre weighs 0.84 kg/1.85 lb 1 gallon weighs 3.86 kg/8.5 lb.

Diesel

Measurements To convert inches to centimetres (cm) multiply by 2.54 and centimetres to inches multiply by 0.393 1 inch = 25.4 millimetres (mm) 1 foot = 30.48 centimetres (cm) 1 yard = 0.9144 metre (m)1 mile = 1.6093 kilometres (km)

1 millimetre = 0.03937 inch 1 centimetre = 0.0328 foot (ft) 1 metre = 1.094 yards (yd)1 kilometre = 0.62137 mile The central figure in the table represents either of the

two outside columns, as the case may be i.e. 1 inch = 2.54 centimetres or 1 centimetre = 0.394 inches.

Centimetres 2.540 5.080 7.620 10.160 12,700

15.240 17.780 20.320

22.860 Metres 0.914

3.658

4.572

5.486

6.401

7.315

8.230

7 8

9 1 1.829 2 3 2.743

1

2

3

4

5

6

4

5

6

7

8

9

2.756 3.150 3.543 Yards

Inches

0.394

0.787

1.181

1.575

1.969

2.362

1.094 2.187

3.281

4.374

5.468 6.562

7.655 8.749

9.843

Speed

To convert knots to miles per hour, multiply by 1.15

Distance

To convert miles to kilometres multiply by 1.609 and kilometres to miles multiply by 0.621

Temperature

To convert Centigrade to Fahrenheit divide by 5, multiply by 9 and add 32. To convert Fahrenheit to Centigrade deduct 32, divide by 9 and multiply by 5.

PLEASE NOTE: The above are only RECOMMENDATIONS and NO LIABILITY can be accepted for ANY DECISION based on these figures. The conversion between Imperial and Metric sizes is approximate.

Easy Conversions

Metres into yards . . . add one-tenth Yards into metres . . . deduct one-tenth Kilometres into miles . . . multiply by 5 and divide by 8 Miles into kilometres . . . multiply by 8 and divide by 5 Litres into pints . . . multiply by 7 and divide by 4 Pints into litres . . . multiply by 4 and divide by 7 Litres into gallons . . . multiply by 2 and divide by 9 Gallons into litres . . . multiply by 9 and divide by 2 Kilogrammes into pounds . . . divide by 9 and multiply

by 20 Pounds into kilogrammes . . . divide by 20 and multiply by 9 10 millimetres (equal to 1 centimetre) about four inches 10 centimetres

1 metre a long pace (a little more than a yard) 1000 metres (a little more than half a mile) 1 kilometre

10 square metres about 12 square yards = 10 000 square metres 1 hectare (about two-and-a-half acres)

a little less than two ounces 50 grams a little more than one pound 500 grams

1 tonne = 1000 kilograms (a little less than one ton)

500 millilitres a little less than one pint about one-and-three-quarter pints 1 litre 200 litres the volume of a 44-gailon drum.

MEASUREMENTS (USING THE BODY) AND OTHER COMMON REFERENCES.

Often when you want to measure something you find that you have left your ruler behind. One ruler that you can't lose is yourself. Different parts of your body can be conveniently used as a ruler. These measurements may be a little different for different people. Here are some typical measurements for one person. You can check your own. you don't need to be exact these will give you Ιf a close measurement.

3-4 cm The distance from the tip of your thumb to first knuckle.

8 cm The distance across your hand at the widest part of four fingers.

10 cm The distance across a flat hand including

the thumb.
The distance from your thumb tip to the 20-22cm tip of your little finger when stretched as far apart as possible.

The length of a bare foot, heel to big toe. The distance from elbow to tip of longest 25 cm 45 cm

finger. Often you can estimate this as half a metre (50cm) The distance of a long pace. This distance is slightly longer than a step 1 metre when walking comfortably. Measure out

metre lengths for about 20 metres with chalk on concrete. Practice walking so that your toe always hits the metre mark. Soon your body will learn the feel of a metre step. This is particularly useful if you need to measure the side of a garden, or the length of a fence.

Properly used these measurements will give you within 10% of the actual distance. This is close enough for most agricultural requirements.

1 fish tin holds about ½kg (500 g) of fertilizer, salt, sugar.

1 bottle cap holds 3 cc when level.

The wood of a matchbox cover is approx. .50mm (Suitable to check the gap for spark plugs or contact points in an emergency. (A hacksaw blade is approx. 0.030", or 0.76 mm.)



Metric conversion charts

Metric prefixes and abbreviations

The metre is used as an example below. The same prefixes apply to litres (I or lit) and grams (g). The abbreviation lit is used for litre when unqualified to avoid confusion with the numeral 1.

| millimetre (mm) centimetre (cm) | 0.001 0.01 | one thousandth metre one hundredth metre |
|------------------------------------|---------------|--|
| decimetre (dm) | 0.1 | one tenth metre |
| metre (m) | 1 | one metre |
| decametre (dam) | 10 | ten metres |
| hectometre (hm) | 100 | one hundred metres |
| kilometre (km) | 1000 | one thousand metres |

Conversion from inches is only taken up to 40 in the chart below,

> mm 25.4

> 50.8

76.2

101.6

127.0

152.4

177.8

203.2

228.6

254.0

279.4

304.8

330.2

355.6

381.0

406.4

431.8

457.2

482.6

508.0 533.4

558.8

584.2

609 6

635.0

660.4

685.8

711.2

736.6

762.0

787.4

812.8

838.2

863.6

889.0

914.4 939.8

965.2

990.6

1016.0

see next chart for continuation.

2

3

4

5

6 7 8

9

10

11

12

13

14

15

16

17

18

19

20 21 22

27

28

29 30 31

32

33

34

600

700

800

900

1000

23.62

27.56

31.50

35.43

39.37

Inches/millimetres

Length (linear measure)

Fractions of 1 inch in millimetres

Thirty-seconds, sixteenths,

| eighths, | quarters and one half | in |
|---------------|-----------------------|--------------|
| in | mm | 0.04 |
| 1/32 | 0.8 | 0.08 |
| 1/16 | 1.6 | 0.12 |
| 3/32 | 2.4 | 0.16 |
| 1/8 | 3.2 | 0.20 |
| 5/32 | 4.0 | 0.24 |
| 3/16 | 4.8 | 0.28 |
| 7/32 | 5.6 | 0.31 |
| 1/4 | 6.3 | 0.35 |
| 9/32 | 7.1 | 0.39 |
| 5/16 | 7.9 | 0.43 |
| 11/32 | 8.7 | 0.47 |
| 3/8 | 9.5 | 0.51 |
| 13/32 | 10.3 | 0.55 |
| 7/16 | 11.1 | 0.59 |
| 15/32 | 11.9 12.7 | 0.63 |
| 1/2 17/32 | 13.5 | 0.67 |
| 9/16 | 14.3 | 0.71 |
| 19/32 | 15.1 | 0.75 0.79 |
| 5/8 | 15.9 | 0.73 |
| 21/32 | 16.7 | 0.83 |
| 11/16 | 17.5 | 0.87 |
| 23/32 | 18.3 | 0.94 |
| 3/4 | 19.0 | 0.98 |
| 25/32 | 19.8 | 1.02 |
| 13/16 | 20.6 | 1.06 |
| 27/32 | 21.4 | 1.10 |
| 7/8 | 22.2 | 1.14 |
| 29/32 | 23.0 | 1.18 |
| 15/16 | 23.8 | 1.22 |
| 31/32 | 24.6 | 1.26 |
| 1 inch | 25.4 | 1.30 |
| - 16.1 | 2.41 | 1.34 |
| i welfths | s, sixths and thirds | 1.38 |

| Twelfths, | sixths | and | thirds | |
|-----------|--------|-----|--------|--|
| | | | | |

| | | 1.34 | 34 |
|-----------|-------------------|-------|-----|
| Twelfths, | sixths and thirds | 1.38 | 35 |
| in | mm | 1.42 | 36 |
| 1/12 | 2.1 | 1.46 | 37 |
| 1/6 | 4.2 | 1.50 | 38 |
| 1/4 | 6.3 | 1.54 | 39 |
| 1/3 | 8.5 | 1.57 | 40 |
| 5/12 | 10.6 | 1.97 | 50 |
| 1/2 | 12.7 | 2.36 | 60 |
| 7/12 | 14.8 | 2.76 | 70 |
| 2/3 | 16.9 | 3.15 | 80 |
| 3/4 | 19.0 | 3.54 | 90 |
| 5/6 | 21.2 | 3.94 | 100 |
| 11/12 | 23.3 | 7.87 | 200 |
| 1 inch | 25.4 | 11.81 | 300 |
| | | 15.75 | 400 |
| NI - 4 - | | 19.68 | 500 |
| Note | | 22.62 | 600 |

Note

Find the Imperial figure you wish to convert in the **heavy** type central column and read off the metric equivalent in the righthand column and vice versa.

For example: 10 inches = 254 millimetres and 10mm = 0.39in.

Imperial measurements are expressed below in yards, feet and inches rather than in decimals for convenience if converting with rulers or measuring tapes which do not include decimal readings.

| Feet | /metres | | | Yards | s/m | etres | 3 | |
|------|---------|-----|-------|--------|-----|-------|-----|------|
| ft | in | | m | yd | ft | in | | m |
| 3 | 3 | 1 | 0.30 | · 1 | 0 | 3 | 1 | 0.9 |
| 6 | 7 | 2 | 0.61 | 2 | 0 | 7 | 2 | 1.8 |
| 9 | 10 | 3 | 0.91 | 2 3 | 0 | 10 | 3 | 2.7 |
| 13 | 1 | 4 | 1.22 | 4 | 1 | 1 | 4 | 3.7 |
| 16 | 5 | 5 | 1.52 | 5 | 1 | 5 | 5 | 4.6 |
| 19 | 8 | 6 | 1.83 | 6 | 1 | 8 | 6 | 5.5 |
| 23 | Ō | 7 | 2.13 | 7 | 2 | 0 | 7 | 6.4 |
| 26 | 3 | 8 | 2.44 | 8 | 2 | 3 | 8 | 7.3 |
| 29 | 6 | 9 | 2.74 | 9 | 2 | 6 | 9 | 8.2 |
| 32 | 10 | 10 | 3.05 | 10 | 2 | 10 | 10 | 9.1 |
| 65 | 7 | 20 | 6.10 | 21 | 2 | 7 | 20 | 18.3 |
| 98 | 5 | 30 | 9.14 | 32 | 2 | 5 | 30 | 27.4 |
| 131 | 3 | 40 | 12.19 | 43 | 2 | 3 | 40 | 36.6 |
| 164 | Ō | 50 | 15.24 | 54 | 2 | 0 | 50 | 45.7 |
| 196 | 10 | 60 | 18.29 | 65 | 1 | 10 | 60 | 54.9 |
| 229 | 8 | 70 | 21.34 | 76 | 1 | 8 | 70 | 64.0 |
| 262 | 6 | 80 | 24.38 | 87 | 1 | 6 | 80 | 73.2 |
| 295 | 3 | 90 | 27.43 | 98 | 1 | 3 | 90 | 82.3 |
| 328 | Ĩ | 100 | 30.48 | 109 | 1 | 1 | 100 | 91.4 |

Quick conversion factors – length

Terms are set out in full in the left-hand column except where clarification is necessary.

1 inch (in) = 25.4 mm/2.54 cm=304.8mm/30.48cm/0.3048m 1 foot (ft)/12in 1 yard (yd)/3ft = 914.4 mm/91.44 cm/0.9144 m1 mile (mi)/1760yd = 1609.344 m/1.609 km1 millimetre (mm) = 0.0394 in1 centimetre (cm)/10mm = 0.394in1 metre (m)/100cm = 39.37 in/3.281 ft/1.094 yd1 kilometre (km)/1000m = 1093.6yd/0.6214mi

Quick conversion factors - area

1 square inch (sq in) = 645.16sg mm/ 6.4516sq cm 1 square foot (sq ft)/144sq in = 929.03sq cm 1 square yard (sq yd)/9sq ft = 8361.3sq cm/ 0.8361sq m 1 acre (ac)/4840sq yd = 4046.9 sg m/0.4047 ha1 square mile (sq mi)640ac = 259ha

1 square centimetre (sq cm)/

100 square millimetre (sq mm) = 0.155sq in

1 square metre (sq m)/

10,000sq cm = 10.764sq ft/1.196sq yd 1 are (a)/100sg m = 119.60sq vd/0.0247ac 1 hectare (ha)/100a = 2.471ac/0.00386sq mi

Quick conversion factors - volume

1 cubic inch (cu in) = 16.3871cu cm 1 cubic foot (cu ft)/

1728cu in = 28.3168cu dm/0.0283cu m

1 cubic yard (cu yd)/

27cu ft = 0.7646cu m

1 cubic centimetre (cu cm)/

1 cubic metre (cu m)/

1000 cubic millimetres = 0.0610cu in (cu mm)

1 cubic decimetre (cu dm)/

= 61.024cu in/0.0353cu ft 1000cu cm

1000cu dm = 35.3146cu ft/1.308cu yd

= 1 millilitre (ml) 1cu cm = 1 litre (lit) See Capacity 1cu dm

Area (square measure) As millimetre numbers would be unwieldy for general use, square or cubic inches have been converted to square or cubic centimetres. Conversion from square inches is only taken up to 150 in the first chart below; see next chart for continuation.

| Square inc | ches/square | е |
|--|--|--|
| sq in 0.2 0.3 0.5 0.6 0.8 0.9 1.1 1.2 1.4 1.6 3.1 4.7 6.2 7.8 9.3 10.9 12.4 14.0 15.5 17.1 18.6 20.2 21.7 23.3 46.5 62.0 77.5 93.0 108.5 124.0 139.5 125.0 | 1 2 3 4 5 6 7 8 9 10 20 30 40 50 60 70 80 90 110 120 130 140 150 200 300 400 500 600 700 800 900 1000 | sq cm 6.5 12.9 19.4 25.8 32.3 38.7 45.2 51.6 58.1 64.5 129.0 193.5 258.1 387.1 451.6 516.1 580.6 645.2 709.7 774.2 838.7 967.7 |
| Square te | et/square r | netres |

| Square fee | et/square me | etres |
|---------------|--------------|-------|
| sq ft | | sq m |
| 10.8 | 1 | Ó.09 |
| 21.5 | | 0.19 |
| 32.3 | 2 3 | 0.28 |
| 43.1 | 4 | 0.37 |
| 53.8 | 5 | 0.46 |
| 64.6 | 6 | 0.56 |
| 75.3 | 7 | 0.65 |
| 86.1 | 8 | 0.74 |
| 96.9 | 9 | 0.84 |
| 107.6 | 10 | 0.93 |
| 215.3 | 20 | 1.86 |
| 322.9 | 30 | 2.79 |
| 430.6 | 40 | 3.72 |
| 538.2 | 50 | 4.65 |
| 645.8 | 60 | 5.57 |
| 753.5 | 70 | 6.50 |
| 861.1 | 80 | 7.43 |
| 968 .8 | 90 | 8.36 |
| 1076.4 | 100 | 9.29 |
| _ | | |

| 1076.4 | 100 | 9.29 |
|----------|-------------|--------|
| Square y | ards/square | metres |
| sq yd | | sq m |
| 1.2 | 1 | 0.8 |
| 2.4 | 2 | 1.7 |
| 3.6 | 2 | 2.5 |
| · 4.8 | 4 | 3.3 |
| 6.0 | 5 | 4.2 |
| 7.2 | 6 | 5.0 |
| 8.4 | 7 | 5.9 |
| 9.6 | 8 | 6.7 |
| 10.8 | Š | 7.5 |
| | 10 | 8.4 |
| 12.0 | | 16.7 |
| 23.9 | 20 | |
| 35.9 | 30 | 25.1 |
| 47.8 | 40 | 33.4 |
| 59.8 | 50 | 41.8 |
| 71.8 | 60 | 50.2 |
| 83.7 | 70 | 58.5 |
| 95.7 | 80 | 66.9 |
| 107.6 | 90 | 75.3 |
| 119.6 | 100 | 83.6 |
| | | |

Volume (cubic measure) Cubic inches/cubic centimetres cu in 16.4 0.06 2 3 4 32.8 0.12 49.2 0.18 0.24 65.5 0.31 5 6 7 8 81.9 0.37 98.3 0.43 114.7 0.49 131.1 0.55 9 147.5 10 0.61 163.9 20 30 1.22 327.7 1.83 491.6 2.44 40 655.5 50 60 3.05 819.4 3.66 983.2 4.27 70 1147.1/1.15cu dm 1311.0/1.31 cu dm 1474.8/1.47 cu dm 1638.7/1.64 cu dm 4.88 5.49 90 6.10 100 12.20 200 3277.4/3.28cu dm 18.31 300 4916.1/4.92cu dm 24.41 400 6554.8/6.55cu dm 30.51 500 8193.5/8.19cu dm 36.61 **600** 9832.2/9.83cu dm 42.72 **700** 11470.9/11.47cu dm 48.82 **800** 13109.7/13.11cu dm 54.92 **900** 14748.4/14.75cu dm 61.02 1000 16387.1/16.39cu dm 122.05 2000 32774.1/32.77cu dm

| Cubic | feet/c | ubis decimetres |
|-------|--------|-----------------|
| cu ft | | cu dm |
| .04 | 1 | 28.3 |
| 0.07 | 2 | 56.6 |
| 0.11 | 3 | 85.0 |
| 0.14 | 4 | 113.3 |
| 0.18 | 5 | 141.6 |
| 0.21 | 6 | 169.9 |
| 0.25 | 7 | 198.2 |
| 0.28 | 8 | 226.5 |
| 0.32 | 9 | 254.9 |
| 0.35 | 10 | 283.2 |
| 0.71 | 20 | 566.3 |
| 1.06 | 30 | 849.5 |
| 1.41 | 40 | 1132.7/1.13cu m |
| 1.77 | 50 | 1415.8/1.42cu m |
| 2.12 | 60 | 1699.0/1.70cu m |
| 2.47 | 70 | 1982.2/1.98cu m |
| 2.83 | 80 | 2265.3/2.27cu m |
| 3.18 | 90 | 2548.5/2.55cu m |
| 3.53 | 100 | 2831.7/2.83cu m |
| | | |

| Cubic yar | ds/cubic me | tres |
|-----------|-------------|------|
| cu yd | | cu m |
| 1.3 | 1 | 0.8 |
| 2.6 | 2 | 1.5 |
| 3.9 | 3 | 2.3 |
| 5.2 | 4 | 3.1 |
| | | 3.8 |
| 6.5 | 5 | |
| 7.8 | <u>6</u> | 4.6 |
| 9.2 | 7 | 5.4 |
| 10.5 | 8 | 6.1 |
| 11.8 | 9 | 6.9 |
| 13.1 | 10 | 7.6 |
| 26.2 | 20 | 15.3 |
| 39.2 | 30 | 22.9 |
| 52.3 | 40 | 30.6 |
| | 50 | 38.2 |
| 65.4 | | |
| 78.5 | 60 | 45.9 |
| 91.6 | 70 | 53.5 |
| 104.6 | 80 | 61.2 |
| 117.7 | 90 | 68.8 |
| 130.8 | 100 | 76.5 |

| Capaci | ty | | Weigh | t | |
|---|--|--|---|---|--|
| | nces/millilit | res | Ounces, | /grams | |
| 0.70 1.06 1.41 | | .8 .2 .6 .1 .5 .9 .3 .7 .7 | 02 0.04 0.07 0.11 0.14 0.18 0.21 0.25 0.28 0.32 0.35 0.39 0.42 0.46 0.49 | 1 2 3 4 5 6 7 8 9 10 11 12 13 | g 28.3 56.7 85.0 113.4 141.7 170.1 198.4 225.1 283.5 311.8 340.2 368.5 396.9 |
| Pints/lite | res | | 0.53 0.56 | 15 16 | 425.2 453.6 |
| pt 1.8 3.5 5.3 7.0 8.8 10.6 12.3 14.1 15.8 | 1 2 3 4 5 6 7 8 | /it 0.6/568ml 1.1 1.7 2.3 2.8 3.4 4.0 4.5 5.1 | 0.71 1.06 1.41 1.76 2.12 2.47 2.82 3.17 3.53 | 20 30 40 50 60 70 80 90 | 567.0 850.5 1134.0 1417.5 1701.0 1984.5 2268.0 2551.5 2835.0 |
| 17.6 | 10 | 5.7 | | /kilograms | 1 |
| Gallons/I gal 0.2 0.4 0.7 0.9 1.1 1.3 1.5 1.8 2.0 2.2 4.4 6.6 8.8 11.0 13.2 15.4 17.6 19.8 22.0 | 1 2 3 4 5 6 7 8 9 10 20 30 40 50 60 70 80 90 100 | /it 4.5 9.1 13.6 18.2 22.7 27.3 31.8 36.4 40.9 45.5 90.9 136.4 181.8 227.3 272.8 318.2 363.7 454.6 | 16 2.2 4.4 6.6 8.8 11.0 13.2 15.4 17.6 19.8 22.0 44.1 66.1 88.2 10.2 132.3 154.3 176.4 198.4 220.5 | 1 2 3 4 5 6 7 8 9 10 20 30 40 50 60 70 80 90 | kg 0.5 0.9 1.4 1.8 2.3 2.7 3.6 4.1 4.5 9.1 13.6 18.1 22.7 27.2 27.2 31.8 36.3 40.8 45.4 |

| 4.0 : 1 | 00.4 |
|-----------------------|---|
| 1 fluid ounce (fl oz) | |
| 1 gill (gi)/5fl oz | |
| | = 568.2ml/0.568 lit |
| 1 quart (qt)/2pt | |
| 1 gallon (gal)/4pt | = 4.546 lit |
| 1 millilitre (ml) | = 0.035fl oz |
| 1 litre (lit) | = 1.76pt/0.22gal |
| 1ml | - 1 aubic contimates (au am) |
| | = 1 cubic centimetre (cu cm) |
| 1 lit | = 1 cubic decimetre (cu dm) See Volume |
| 1 US pint | = 5/6 Imperial pt/473.2ml/0.473 lit |
| 1 US gallon | = 5/6 Imperial gal/3.785 lit |

| Quick conversion fa | actors – weight |
|--|---|
| 1 ounce (oz) 1 pound (lb)/16oz 1 stone/14lb 1 hundredweight (cwt)/ 8 stone/112lb | = 28.35g = 453.59g/0.4536kg = 6.35kg = 50.80kg |
| 1 ton/20cwt | = 1016.05 kg/1.016 t |
| 1 gram (g) 1 kilogram (kg)/1000g | = 0.035oz = 35.274oz/2.2046lb/ 2lb 3.274oz |
| 1 tonne (t)/1000kg | = 2204.61b/0.9842 ton |

| kubik- meter | kubik- decimeter (= liter) | cubic- inch | cubic- foot | fluid ounce (UK) | pint (UK) | gallon (UK) | fluid ounce (US) | liquid pint (US) | gallon (US) |
|-----------------|----------------------------------|----------------|------------------------|------------------------|--------------|----------------|------------------------|------------------------|----------------|
| m³ | dm³ | in³ | ft³ | oz (UK) | pt (UK) | gal (UK) | fl oz (US) | liq pt (US) | gal (US) |
| 1 | 1000 | 61023,7 | 35,3146 | 35195 | 1759,75 | 219,97 | 33817,6 | 2113,6 | 264,2 |
| 10·3 | 1 | 61,0237 | 0,03531 | 35,195 | 1,75975 | 0,21997 | 33,8176 | 2,1136 | 0,26417 |
| 0,016·10·3 | 0,01639 | 1 | 0,579·10 ⁻³ | 0,57674 | 0,02884 | 3,605·10·3 | 0,55417 | 0,03463 | 0,00433 |
| 0,02832 | 28,3168 | 1728 | 1 | 996,607 | 49,8304 | 6,2288 | 957,610 | 59,85 | 7,4805 |
| 0,028 · 10-3 | 0,02841 | 1,73387 | 0,00100 | 1 | 0,05 | 0,00625 | 0,9608 | 0,0601 | 0,00751 |
| 0,568 · 10-3 | 0,56826 | 34,6774 | 0,02003 | 20 | 1 | 0,125 | 19,2167 | 1,2001 | 0,15013 |
| 0,00455 | 4,5461 | 277,42 | 0,16054 | 160 | 8 | 1 | 153,735 | 9,6062 | 1,201 |
| 0,03 · 10-3 | 0,02957 | 1,8045 | 0,00104 | 1,0408 | 0,05204 | 0,00650 | 1 | 0,0625 | 0,00781 |
| 0,473·10·3 | 0,47313 | 28,875 | 0,01688 | 16,652 | 0,83264 | 0,10408 | 16 | 1 | 0,125 |
| 0,00379 | 3,78541 | 231 | 0,13368 | 133,216 | 6,6608 | 0,83267 | 128 | 8 | 1 |

| gram | kilogram | ton | tekma | ounce | pound | short hundred- weight (US) | short ton (US) | hundred- weight (UK) (= long cwt, US) | ton (UK) (= long ton, US) |
|------------------------------|--------------------------------------|--|--|-------------------------------------|---------------------------------------|--------------------------------------|--|---|--|
| g | kg | t | | oz | lb | sh. cwt | sh. ton | cwt | ton |
| 1 1000 1000000 9807 | 0,001 1 1000 9,807 | 10-6 0,001 1 0,00981 | 0,102·10·3 0,102 102 1 | 0,03527 35,274 35274 345,9 | 0,00221 2,205 2204,6 21,6205 | - 0,02205 22,046 0,2162 | - 0,00110 1,1023 0,01081 | - 19,68 · 10·3 19,68 0,193 | - 0,984·10·3 0,9842 0,00965 |
| 28,35 453,592 45359 | 0,02835 0,45359 45,36 907,2 | 0,028 · 10·3 0,454 · 10·3 0,0454 0,9072 | 0,00289 0,04625 4,625 92,507 | 1 16 1600 32000 | 0,0625 1 100 2000 | 0,625·10·3 0,01 1 20 | 0,031·10·3 0,5·10·3 0,05 1 | 0,558·10·3 0,00893 0,8929 17,86 | 0,0279·10·3 0,446·10·3 0,04464 0,8929 |
| 50802 | 50,80 1016 | 0,0508 1,016 | 5,18 103,61 | 1792 35840 | 112 2240 | 1,12 22,4 | 0,056 1,12 | 1 20 | 0,05 1 |

| | | | | | | to a contract and a secondary contract contract | | | | to be an included an included the second of |
|-----------------|--------------|----------------|------------------------|--------------------|-----------|---|--|--|--------------------------------|---|
| 1 10 | == 2,5400 cm | 1 mg in = 6, | ,4516 cm² | 1 901 = 4 | qt | 1 may mile h = 0,5144 m/sec | 1 in Hg = 3,3421 · 10-2 atm | 1 10/1s = 1,7858 · 10 ⁻¹ kg/cm | 1 HK = 0,886 IK = 0,903 cd | = 0,2520 iT kcal |
| 1 ft | = 0,3048 m | 1 sq ft = 9, | ,2903 dm ² | 1 qt = 2 | pt | 1 stat mile/h = 0,4470 m/sec | 1 in $H_2O = 2,4583 \cdot 10^{-3}$ atm | 1 lb/ft = 1,4882 kg/m | 1 cd = 0.981 IK = 1,107 HK | 1 BTU/lb = 0,5555 IT kcal/kg |
| 1 yd | = 0,9144 m | 1 sq yd = 0, | ,8361 m ² | 1 imp gal = 277,42 | cu in | 1 ft/sec = 1.0973 km/h | 1 lb/sq in = 6,8046 · 10 ⁻² atm | 1 1b/yd = $4,9606 \cdot 10^{-1} \text{ kg/m}$ | 1 IK = 1,019 cd = 1,128 HK | 1 BTU/°F == 0,4536 IT kcal/°C |
| 1 fathom | = 1,8288 m | 1 acre = 40, |),4684 a | 1 US gal = 231.00 | cu in | 1 stat mile/h = 1,4666 ft/sec | 1 in Hg = 3,4532 · 10 ⁻² at | | 1 bougie décimale = 1,12 HK | 1 BTU/Ib °F = 1,0000 IT kcal/kg °C |
| 1 stat mile | = 1.6093 km | 1 sq mile = 2. | .5899 km² | 1 imp bu = 8 | imp gal | T sid time; = 1,4000 ii/sec | 1 in H ₂ O = 2,5400 · 10 ⁻³ at | 1 this in $= 2.7680 \cdot 10^{-2} \text{ kg/cm}^3$ | 1 sperm candle = 1,14 HK | 1 BTU/ft *F == 1,4884 IT kcal/m *C |
| 1 naut mile | = 1,8532 km | 1 acre = | 4840 sq yd | 1 US bu == 9,30 | 92 US gal | | 1 lb/sq in = $7,0307 \cdot 10^{-2}$ at | 1 lb/cu ft = 1,6019 · 10 kg/m ³ | 1 pentan candle = 1,11 HK | 1 BTU/in °F = 17,858 1T kcal/m °C |
| 1 int mile | = 1,8520 km | | | 1 cm = 28,34 | 05 0 | 1 sq yd/min = 50,1675 m ² /h | 1 in Hg = 3,3864 · 10 ⁻² bar | 1 lb/cu yd = 5,9328 · 10-1 kg/m ³ | 1 carcel = 10,75 HK | 1 BTU/sq ft *F = 4,8824 IT kcai/m² *C |
| 1 toise (Paris) | | 1 co in = 16. | 5,3871 cm ³ | | 36 kg | 1 sq ft/min == 5,5742 m ² /h | 1 in $H_2O = 2,4909 \cdot 10^{-3}$ bar | 1 oz/cu in = 1,7300 g/cm^3 | 1 VK = 1,20 HK | 1 BTU/sq in °F = 703,07 IT kcal/m² °C |
| | = 2,2558 mm | | | | - | 1 sq in/sec = 2,3226 m ² /h | 1 lb/sq in = 6,8948 · 10 ⁻² bar | 1 oz/cu ft = 1,0012 kg/m^3 | $= \pi \cdot 10^4 \text{ asb}$ | 1 BTU/sq ft = 2,7124 IT kcal/m ² |
| | | | 3,3167 dm ³ | | 24 kg | 1 sq yd/min = 1,3934 dm²/sec | 1 Torr = 1,3158 · 10 ⁻³ atm | 1 lb/imp gal = $9.9779 \cdot 10^{-2} \text{ kg/dm}^3$ | 1 la = 10 ⁴ asb | 1 BTU/in = 9,9211 IT kcal/m |
| 1.0 | = 12 in | 1 cu yd = 0. |),7646 m ³ | 1 ton = 1,01 | 60 1 | ** ' | 1 atm = 1,03323 kg/cm ² | 1 lb/US gal = 1,1983 · 10 ⁻¹ kg/dm ³ | 1 m la = 10 ⁻³ la | |
| 1 yd | = 3 ft | 1 pint == 0, | 0,5683 dm ³ | 1 sh cwt = 45,35 | 92 kg | 1 sq ft/min == 15,4838 cm²/sec | 1 at = 1,0000 kg/cm ² | 1 lb/pint = 7,9823 · 10 ⁻¹ kg/dm ³ | 1 ft la = 10,764 asb | $T_{K} = t_{C} + 273,15 = \frac{3}{7} T_{Rank}$ |
| 1 fathorn | = 2 yd | 1 imp gal = 4. | ,5460 dm ³ | 1 sh ton = 0.90 | 72 t | 1 sq in/min == 0,1075 cm ² /sec | 1 at == 0,9678 atm | 110,000 10 113,000 | 1 ft cd = 10,764 lx | $T_{Rank} = t_F + 459,67 = ^{\circ}/_{S} T_{K}$ |
| 1 stat mile | == 1760 yd | 1 US gal = 3, | 3,7854 dm ³ | 1 sh ton = 2000 | lb | 1 impgal/min = 0,2728 m ³ /h | 1 bar = 1,01972 kg/cm ² | 1 ib/min = 2,7216 · 10 kg/h | 1 ph = 10 ⁴ lx | $t_C = \frac{5}{4} \cdot (t_F - 32) = T_K - 273,15$ |
| 1 naut mile | = 2026,7 yd | 1 US at == 0, | 0,9463 dm ³ | 1 ton = 2240 | lb | 1 US gal/min = 0,2271 m ³ /h | 1 bratm == 30 in Hg | 1 lb/sec = 1,6329 t/h | 1 lx == 1 lm/m ² | $t_F = \frac{1}{5} t_C + 32 = T_{Rank} - 459.67$ |

Metric conversion tables

| | | | Millim Inc | etres to hes | Inches to Millimetre | |
|----------------|---------------------|--------------------|---------------|--------------------|-------------------------|----------------|
| Inches | Decimals | Millimetres | mm | Inches | Inches | mm |
| 1/64 | 0.015625 | 0.3969 | 0.01 | 0.00039 | 0.001 | 0.0254 |
| 1/32 | 0.03125 | 0.7937 | 0.02 | 0.00079 | 0.002 | 0.0508 |
| 3/64 | 0.046875 | 1.1906 | 0.03 | 0.00118 | 0.003 | 0.0762 |
| 1/16 | 0.0625 | 1.5875 | 0.04 | 0.00157 | 0.004 | 0.1016 |
| 5/64 | 0.078125 | 1.9844 | 0.05 | 0.00197 | 0.005 | 0.1270 |
| 3/32 | 0.09375 | 2.3812 | 0.06 | 0.00236 | | 0.1524 |
| 7/64 | 0.109375 | 2.7781 | 0.07 | 0.00276 | | 0.1778 |
| 1/8 | 0.125 | 3.1750 | 0.08 | 0.00315 | | 0.203 |
| 9/64 | 0.140625 | 3.5719 | 0.09 | 0.00354 | | 0.228 |
| 5/32 | 0.15625 | 3.9687 | 0.1 | 0.00394 | | 0.254 |
| 11/64 | 0.171875 0.1875 | 4.3656 4.7625 | 0.2 0.3 | 0.00787 0.01181 | | 0.508 0.762 |
| 3/16 13/64 | 0.1875 | 5.1594 | 0.4 | | | |
| 7/32 | 0.203125 | 5.5562 | 0.4 0.5 | 0.01575 | | 1.016 |
| 15/64 | 0.234375 | 5.9531 | 0.6 | 0.01969 0.02362 | | 1.270 |
| 1/4 | 0.25 | 6.3500 | 0.7 | 0.02362 | 0.06 0.07 | 1.524 1.778 |
| 17/64 | 0.265625 | 6.7469 | 0.7 | 0.02750 | | 2.032 |
| 9/32 | 0.28125 | 7.1437 | 0.9 | 0.03543 | | 2.286 |
| 19/64 | 0.296875 | 7.5406 | 1 | 0.03937 | | 2.54 |
| 5, 16 | 0.3125 | 7.9375 | 2 | 0.07874 | | 5.08 |
| 21/64 | 0.328125 | 8.3344 | 3 | 0.11811 | | 7.62 |
| 11/32 | 0.34375 | 8.7312 | 4 | 0.15748 | | 10.16 |
| 23/64 | 0.359375 | 9.1281 | 5 | 0.19685 | | 12.70 |
| 3/8 | 0.375 | 9.5250 | 6 | 0.23622 | | 15.24 |
| 25/64 | 0.390625 | 9.9219 | 7 | 0.27559 | | 17.78 |
| 13/32 | 0.40625 | 10.3187 | 8 | 0.31496 | | 20.32 |
| 27/64 | 0.421875 | 10.7156 | 9 | 0.35433 | | 22.86 |
| 7/16 | 0.4375 | 11.1125 | 10 | 0.39370 | | 25.4 |
| 29/64 | 0.453125 | 11.5094 | 11 | 0.43307 | 2 | 50.8 |
| 15/32 | 0.46875 | 11.9062 | 12 | 0.47244 | | 76.2 |
| 31/64 | 0.484375 | 12.3031 | 13 | 0.51181 | | 101.6 |
| 1/2 | 0.5 | 12.7000 | 14 | 0.55118 | | 127.0 |
| 33/64 | 0,515625 | 13.0969 | 15 | 0.59055 | | 152.4 |
| 17/32 | 0.53125 | 13.4937 | 16 | 0.62992 | | 177.8 |
| 35/64 | 0.546875 | 13.8906 | 17 | 0.66929 | | 203.2 |
| 9/16 | 0.5625 | 14.2875 | 18 10 | 0.70866 | | 228.6 |
| 37/64 19/32 | 0.578125 0.59375 | 14.6844 15.0812 | 19 20 | 0.74803 0.78740 | | 254.0 279.4 |
| 39/6 4 | 0.609375 | 15.4781 | 21 | 0.82677 | | 304.8 |
| 5/8 | 0.625 | 15.8750 | 22 | 0.86614 | | 330.2 |
| 41/64 | 0.640625 | 16.2719 | 23 | 0.90551 | | 355.6 |
| 21/32 | 0.65625 | 16.6687 | 24 | 0.94488 | | 381.0 |
| 43/64 | 0.671875 | 17.0656 | 25 | 0.98425 | | 406.4 |
| 11/16 | 0.6875 | 17.4625 | 26 | 1.02362 | | 431.8 |
| 15/64 | 0.703125 | 17.8594 | 27 | 1.06299 | | 457.2 |
| 23/32 | 0.71875 | 18.2562 | 28 | 1.10236 | 19 | 482.6 |
| 1 7/64 | 0.734375 | 18.6531 | 29 | 1.14173 | 20 | 508.0 |
| 3/4 | 0.75 | 19.0500 | 30 | 1.18110 | | 533.4 |
| 19/64 | 0.765625 | 19.4469 | 31 | 1.22047 | | 558.8 |
| 25/32 | 0.78125 | 19.8437 | 32 | 1.25984 | | 584.2 |
| 51/64 | 0.796875 | 20.2406 | 33 | 1.29921 | | 609.6 |
| 13/16 | 0.8125 | 20.6375 | 34 | 1.33858 | | 635.0 |
| 53/64 | 0.828125 | 21.0344 | 35 | 1.37795 | | 660.4 |
| 27/32 | 0.84375 | 21.4312 | 36 | 1.41732 | | 685.8 |
| 55/64 | 0.859375 | 21.8281 | 37 | 1.4567 | | 711.2 |
| 7/8 | 0.875 | 22.2250 | 38 | 1.4961 | | 736.6 |
| 57/64 | 0.890625 | 22.6219 | 39 | 1.5354 | | 762.0 |
| 29/32 | 0.90625 | 23.0187 | 40 41 | 1.5748 | | 787.4 |
| 59/64 | 0.921875 | 23.4156 | 41 42 | 1.6142 1.6535 | | 812.8 838.2 |
| 15/16 | 0.9375 | 23.8125 24.2094 | 42 43 | 1.6929 | | 863.6 |
| 31/64 | 0.953125 | | | | | |
| 31/32 | 0.96875 | 24.6062 | 44 | 1.7323 | . <- | 889.0 |

VIII. Decimal Equivalents of Common Fractions

| 8ths | 16ths | 32ds | 64ths | | 8ths | 16ths | 32ds | 64ths | |
|------|-------|------|-------|----------|------|-------|------|-------|----------|
| | | | 1 | . 015625 | | | | 33 | . 515628 |
| | | 1 | 2 | . 03125 | | | 17 | 34 | . 53125 |
| | | | 3 | . 046875 | | | | 35 | . 546875 |
| | 1 | 2 | 4 | . 0625 | | 9 | 18 | 36 | . 5625 |
| - 1 | | | 5 | . 078125 | 1 1 | | | 37 | . 578125 |
| | | 3 | 6 | .09375 | | | 19 | 38 | . 59375 |
| . | | | 7 | . 109375 | | | | 39 | . 609375 |
| 1 | 2 | 4 | 8 | . 125 | 5 | 10 | 20 | 40 | . 625 |
| | ĺ | | 9 | . 140625 | | | | 41 | . 640625 |
| ĺ | ļ | 5 | 10 | . 15625 | | | 21 | 42 | . 65625 |
| ł | | | 11 | . 171875 | | | i | 43 | . 671875 |
| | 3 | 6 | 12 | . 1875 | | 11 | -22 | 44 | . 6875 |
| | | | 13 | . 203125 | | | | 45 | . 703125 |
| 1 | | 7 | 14 | . 21875 | | ŀ | 23 | 46 | .71875 |
| | | | 15 | . 234375 | | | | 47 | .734375 |
| 2 | 4 | 8 | 16 | . 25 | 6 | 12 | 24 | 48 | .75 |
| - 1 | | | 17 | . 265625 | | | ĺ | 49 | .765625 |
| 1 | ĺ | 9 | 18 | . 28125 | i i | 1 | 25 | 50 | . 78125 |
| ļ | i |] | 19 | . 296875 | | | Ì | 51 | 796875 |
| | 5 | 10 | 20 | . 3125 | | 13 | 26 | 52 | .8125 |
| | | J | 21 | .328125 | | | | 53 | .828125 |
| İ | | 11 | 22 | . 34375 | | | 27 | 54 | .84375 |
| | | | 23 | . 359375 | | | | 55 | .859375 |
| 3 | 6 | 12 | 24 | . 375 | 7 | 14 | 28 | 56 | . 875 |
| | | | 25 | . 390625 | | ĺ | | 57 | . 890625 |
| | | 13 | 26 | . 40625 | | ļ | 29 | 58 | . 90625 |
| | 1 | - | 27 | . 421875 | | 1 | | 59 | .921875 |
| İ | 7 | 14 | 28 | . 4375 | - 1 | 15 | 30 | 60 | . 9375 |
| | 1 | | 29 | 453125 | | | 1 | 61 | . 953125 |
| - 1 | | 15 | 30 | 46875 | | I | 31 | 62 | . 96875 |
| | 1 | | 31 | 484375 | | | | 63 | . 984375 |
| 4 | 8 | 16 | 32 | .5 | 8 | 16 | 32 | | 1 |

Table D-1. Fraction, Decimal, and Metric Equivalents

| Fractions | Decimal In. | Metric mm. | Fractions | Decimal In. | Metric mm. |
|-----------|-------------|------------|-----------|-------------|------------|
| 1/64 | .015625 | .397 | 33/64 | .515625 | 13.097 |
| 1/32 | .03125 | .794 | 17/32 | .53125 | 13.494 |
| 3/64 | .046875 | 1.191 | 35/64 | .546875 | 13.891 |
| 1/16 | .0625 | 1.588 | 9/16 | .5625 | 14.288 |
| 5/64 | .078125 | 1.984 | 37/64 | .578125 | 14.684 |
| 3/32 | .09375 | 2.381 | 19/32 | .59375 | 15.081 |
| 7/64 | .109375 | 2.778 | 39/64 | .609375 | 15.478 |
| 1/8 | .125 | 3.175 | 5/8 | .625 | 15.875 |
| 9/64 | .140625 | 3.572 | 41/64 | .640625 | 16.272 |
| 5/32 | .15625 | 3.969 | 21/32 | .65625 | 16.669 |
| 11/64 | .171875 | 4.366 | 43/64 | .671875 | 17.066 |
| 3/16 | .1875 | 4.763 | 11/16 | .6875 | 17.463 |
| 13/64 | .203125 | 5.159 | 45/64 | .703125 | 17.859 |
| 7/32 | .21875 | 5.556 | 23/32 | .71875 | 18.256 |
| 15/64 | .234375 | 5.953 | 47/64 | .734375 | 18.653 |
| 1/4 | .250 | 6.35 | 3/4 | .750 | 19.05 |
| 17/64 | .265625 | 6.747 | 49/64 | .765625 | 19.447 |
| 9/32 | .28125 | 7.144 | 25/32 | .78125 | 19.844 |
| 19/64 | .296875 | 7.54 | 51/64 | .796875 | 20.241 |
| 5/16 | .3125 | 7.938 | 13/16 | .8125 | 20.638 |
| 21/64 | .328125 | 8.334 | 53/64 | .828125 | 21.034 |
| 11/32 | .34375 | 8.731 | 27/32 | .84375 | 21.431 |
| 23/64 | .359375 | 9.128 | 55/64 | .859375 | 21.828 |
| 3/8 | .375 | 9.525 | 7/8 | .875 | 22.225 |
| 25/64 | .390625 | 9.922 | 57/64 | .890625 | 22.622 |
| 13/32 | .40625 | 10.319 | 29/32 | .90625 | 23.019 |
| 27/64 | .421875 | 10.716 | 59/64 | .921875 | 23.416 |
| 7/16 | .4375 | 11.113 | 15/16 | .9375 | 23.813 |
| 29/64 | .453125 | 11.509 | 61/64 | .953125 | 24.209 |
| 15/32 | .46875 | 11.906 | 31/32 | .96875 | 24.606 |
| 31/64 | .484375 | 12.303 | 63/64 | .984375 | 25.003 |
| 1/2 | .500 | 12.7 | 1 | 1.00 | 25.4 |

| Inches | Millimeters | Inches | Millimeters | Inches | Millimeters |
|--------|-------------|--------|-------------|--------|-------------|
| 0.001 | 0.0254 | 0.010 | 0.2540 | 0.019 | 0.4826 |
| 0.002 | 0.0508 | 0.011 | 0.2794 | 0.020 | 0.5080 |
| 0.003 | 0.0762 | 0.012 | 0.3048 | 0.021 | 0.5334 |
| 0.004 | 0.1016 | 0.013 | 0.3302 | 0.022 | 0.5588 |
| 0.005 | 0.1270 | 0.014 | 0.3556 | 0.023 | 0.5842 |
| 0.006 | 0.1524 | 0.015 | 0.3810 | 0.024 | 0.6096 |
| 0.007 | 0.1778 | 0.016 | 0.4064 | 0.025 | 0.6350 |
| 0.008 | 0.2032 | 0.017 | 0.4318 | | |
| 0.009 | 0.2286 | 0.018 | 0.4572 | | |

Table D-4. Feet to Meters Conversion Table

| Table | | | |
|-------|----------|------|--|
| | - w_ | | |

Table D-5. Meters to Feet Conversion

| foot | = 0.3048 m | | | 1 metre = 3.2808 fe | eet |
|------|------------|-----|--------|------------------------|-----------------------|
| ft. | met. | ft. | met. | met. | feet |
| 1 | 0,305 | 31 | 9,449 | 1 | 3,28 |
| 2 | 0,610 | 32 | 9,754 | 2 3 | 6,56 9,84 |
| 3 | 0,914 | 33 | 10,058 | 4 | 9,04 13,12 |
| | | | | 5 | 16,40 |
| 4 | 1,219 | 34 | 10,363 | 6 | 19,69 |
| 5 | 1,524 | 35 | 10,668 | 7 | 22,97 |
| 6 | 1,829 | 36 | 10,973 | 8 9 | 26,25 |
| 7 | 2,134 | 37 | 11,278 | 10 | 29,53 32,81 |
| 8 | 2,438 | 38 | 11,582 | 11 | 36,09 |
| 9 | 2,743 | 39 | 11,887 | 12 | 39,37 |
| | | | | 13 | 42,65 |
| 10 | 3,048 | 40 | 12,192 | 14 15 | 45,93 49,21 |
| 11 | 3,353 | 41 | 12,497 | 16 | 52,49 |
| 12 | 3,658 | 42 | 12,802 | 17 | 55,77 |
| 13 | 3,962 | 43 | 13,106 | 18 | 59,06 |
| 14 | 4,267 | 44 | 13,441 | 19 | 62,34 |
| 15 | 4,572 | 45 | 13,716 | 20 | 65,62 |
| 16 | 4,877 | 46 | 14,021 | | |
| 17 | 5,182 | 47 | 14,326 | | |
| 18 | 5,486 | 48 | 14,630 | | |
| 19 | 5,791 | 49 | 14,935 | Table D-6. Inches to C | entimeters |
| 20 | 6,096 | 50 | 15,240 | Conversion Table | |
| 21 | 6,401 | 51 | 15,545 | | |
| 22 | 6,706 | 52 | 15,850 | Inches – centimetr | es |
| 23 | 7,010 | 53 | 16,154 | 1 inch = 2.54 cm | |
| 24 | 7,315 | 54 | 16,459 | inches | cm |
| 25 | 7,620 | 55 | 16,764 | 4 | |
| 26 | 7,925 | 56 | 17,069 | 1 2 | 2,54 |
| 27 | 8,230 | 57 | 17,374 | 3 | 5,08 7,62 |
| 28 | 8,534 | 58 | 17,678 | 4 | 10,16 |
| 29 | 8,839 | 59 | 17,983 | 5 | 12,70 |
| 30 | 9,144 | 60 | 18,288 | 6 | 15,24 |
| | -,, | | -, | 7 | 17,78 |
| | | | | 8 | 20,32 |
| | | | | 9 | 22,86 |
| | | | | 10 | 25,40 |
| | | | | 11 | 27,94 |
| | | | | 1 | |

12

30,48

Use of the tables: the number to be converted, which is made up by adding the unit at the side of a line to the unit at the head of a column, is converted to the number in the position where line and column meet. For example, 11 in = 10 in + 1 in = 27.940 cm

| | to Centime | | | | | - | | 7 | 8 | ^ | |
|--|---|---|---|--|---|---|--|--|--|--|-------------------------------|
| n → | 0 | 11_ | 2 | 3 | 4 | 5 | 6 | | | 9 | $\stackrel{\leftarrow}{\neg}$ |
| ١ ا | cm | cm | cm | cm | cm | cm | cm | cm | cm | cm | |
|) | 0.000 | 2.540 | 5.080 | 7.620 | 10.160 | 12.700 | 15.240 | 17.780 | 20.320 | 22.860 | |
| | 25.400 | 27.940 | 30.480 | 33.020 | 35.560 | 38.100 | 40.640 | 43.180 | 45.720 | 48.260 | - 1 |
| | 50.800 | 53.340 | 55.880 | 58.420 | 60.960 | 63.500 | 66.040 | 68.580 | 71.120 | 73.660 | |
| ? | | 78.740 | 81.280 | 83.820 | 86.360 | 88.900 | 91.440 | 93.980 | 96.520 | 99.060 | - 1 |
|) | 76.200 | 78.740 | 81.280 | 03.020 | 00.300 | 00.300 | 31.440 | 33.300 | | 33.000 | |
|) | 101.600 | 104.140 | 106.680 | 109.220 | 111.760 | 114.300 | 116.840 | 119.380 | 121.920 | 124.460 | |
|) | 127.000 | 129.540 | 132.080 | 134.620 | 137.160 | 139.700 | 142.240 | 144.780 | 147.320 | 149.860 | - 1 |
|) (| 152.400 | 154.940 | 157.480 | 160.020 | 162.560 | 165.100 | 167.640 | 170.180 | 172.720 | 175.260 | |
|) | 177.800 | 180.340 | 182.880 | 185.420 | 187.960 | 190.500 | 193.040 | 195.580 | 198.120 | 200.660 | |
| 5 | 203.200 | 205.740 | 208.280 | 210.820 | 213.360 | 215.900 | 218.440 | 220.980 | 223.520 | 226.060 | |
| 0 | 228.600 | 231.140 | 233.680 | 236.220 | 238.760 | 241.300 | 243.840 | 246.380 | 248.920 | 251.460 | - 1 |
| 0 | 254.000 | | | | | | | | | | .1 |
| n → | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | <u></u> |
| 1 | cm | cm | cm | cm | cm | cm | cm | cm | cm | cm | |
| | | 25.400 | 50.800 | 76.200 | 101.600 | 127.000 | 152.400 | 177.800 | 203.200 | 228.600 | |
| 0 | 0.000 | 279.400 | | 330.200 | 355.600 | 381.000 | 406.400 | 431.800 | 457.200 | 482.600 | |
| 0 | 254.000 | | 304.800 | | | | | | | | |
| 0 | 508.000 | 533.400 | 558.800 | 584.200 | 609.600 | 635.000 | 660.400 | 685.800 | 711.200 | 736.600 | |
| 9 | 762.000 | 787.400 | 812.800 | 838.200 | 863.600 | 889.000 | 914.400 | 939.800 | 965.200 | 990.600 | |
| 0 | 1016.000 | 1041.400 | 1066.800 | 1092.200 | 1117.600 | 1143.000 | 1168.400 | 1193.800 | 1219.200 | 1244.600 | |
| ŏ | 1270.000 | 1295.400 | 1320.800 | 1346.200 | 1371.600 | 1397.000 | 1422.400 | 1447.800 | 1473.200 | 1498.600 | |
| o | 1524.000 | 1549.400 | 1574.800 | 1600.200 | 1625.600 | 1651.000 | 1676.400 | 1701.800 | 1727.200 | 1752.600 | |
| 0 | 1778.000 | 1803.400 | 1828.800 | 1854.200 | 1879.600 | 1905.000 | 1930.400 | 195 800 | 1981.200 | 2006.600 | |
| 0 | 2032.000 | 2057.400 | 2082.800 | 2108.200 | 2133.600 | 2159.000 | 2184.400 | 2209.800 | 2235.200 | 2260.600 | |
| | | | | 2362.200 | 2387.600 | 2413.000 | 2438.400 | 2463.800 | 2489.200 | 2514.600 | Ī |
| 0 | 2286.000 | 2311.400 | 2336.800 | 2302.200 | 2307.000 | 2413.000 | 2430.400 | 2403.000 | 2403.200 | 2514.000 | - 1 |
| | 2540.000 | iches | | 33 701 in | | | ··· | | | <u></u> | |
| ntin | netres to Ir | | 1 cm = 0.39 | | | 5 | 6 | 7 | Ω | 0 | |
| ntim m → | netres to Ir | 1 | 1 cm = 0.39 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | <u></u> |
| ntin | netres to Ir | 1 in | 1 cm = 0.39 | | in | in | in | in | in | ìn | |
| ntim m· → | netres to Ir | 1 | 1 cm = 0.39 | 3 | | | | | • | | |
| ntim m· → | netres to Ir | in 0.394 | 1 cm = 0.39 2 in 0.787 | 3 in | in | in | in | in | in | ìn | |
| ntim m → ↓ 0 0 | 0 in 0.000 3.937 | 1 in 0.394 4.331 | 1 cm = 0.39 2 in 0.787 4.724 | in 1.181 5.118 | in 1.575 5.512 | in 1.969 5.906 | in 2.362 6.299 | in 2.756 6.693 | in 3.150 | in 3.543 7.480 | |
| m → ↓ 0 0 0 0 | netres to Ir | in 0.394 | 1 cm = 0.39 2 in 0.787 | 3 in 1.181 | in 1.575 | in 1.969 | in 2.362 | in 2.756 | in 3.150 7.087 | in 3.543 | |
| ntim m → 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 | 0.394 4.331 8.268 12.205 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 | 3 in 1.181 5.118 9.055 12.992 | in 1.575 5.512 9.449 13.386 | in 1.969 5.906 9.843 13.780 | in 2.362 6.299 10.236 14.173 | in 2.756 6.693 10.630 14.567 | in 3.150 7.087 11.024 14.961 | 3.543 7.480 11.417 15.354 | |
| o 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 | in 0.394 4.331 8.268 12.205 | 1 cm = 0.39 2 in 0.787 4.724 8.661 12.598 16.535 | 3 in 1.181 5.118 9.055 12.992 16.929 | in 1.575 5.512 9.449 13.386 17.323 | in 1.969 5.906 9.843 13.780 | in 2.362 6.299 10.236 14.173 18.110 | in 2.756 6.693 10.630 14.567 | 3.150 7.087 11.024 14.961 18.898 | in 3.543 7.480 11.417 15.354 19.291 | |
| ntim | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 | in 0.394 4.331 8.268 12.205 16.142 20.079 | 1 cm = 0.39 2 in 0.787 4.724 8.661 12.598 16.535 20.472 | in 1.181 5.118 9.055 12.992 16.929 20.866 | in 1.575 5.512 9.449 13.386 17.323 21.260 | in 1.969 5.906 9.843 13.780 17.717 21.654 | in 2.362 6.299 10.236 14.173 18.110 22.047 | in 2.756 6.693 10.630 14.567 18.504 22.441 | 3.150 7.087 11.024 14.961 18.898 22.835 | in 3.543 7.480 11.417 15.354 19.291 23.228 | |
| ntin | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 | in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 | 3.150 7.087 11.024 14.961 18.898 22.835 26.772 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 | |
| 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 | 1 cm = 0.39 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 | |
| 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 | |
| 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 | 1 cm = 0.39 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 | |
| ntim | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 | |
| ntim 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 | |
| ntim 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 | in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 | 1 cm = 0.39 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 | 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 | - |
| ntim | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 | 1 cm = 0.39 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 | - |
| ntim → ↓ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 | 1 cm = 0.38 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 | - |
| ntim | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 in 7.874 47.244 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 in 19.685 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 | - |
| ntim | 0 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 in 7.874 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 | 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 | - |
| ntim → ↓ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in 7.874 47.244 86.614 125.984 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 | - |
| ntim | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 157.480 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 161.417 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 in 7.874 47.244 86.614 125.984 165.354 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 169.291 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 141.732 181.102 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 185.039 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 149.606 | 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 | - |
| ntim 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 157.480 196.850 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 161.417 200.787 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in 7.874 47.244 86.614 125.984 165.354 204.724 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 169.291 208.661 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 173.228 212.598 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 177.165 216.535 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 141.732 181.102 220.472 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 185.039 224.409 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 149.606 188.976 228.346 | 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 | - |
| ntim | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 157.480 196.850 236.220 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 161.417 200.787 240.157 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in 7.874 47.244 86.614 125.984 165.354 204.724 244.094 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 169.291 208.661 248.031 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 173.228 212.598 251.969 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 177.165 216.535 255.906 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 141.732 181.102 220.472 259.843 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 185.039 224.409 263.780 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 149.606 188.976 228.346 267.717 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 192.913 232.283 271.654 | - |
| m → | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 157.480 196.850 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 161.417 200.787 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in 7.874 47.244 86.614 125.984 165.354 204.724 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 169.291 208.661 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 173.228 212.598 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 177.165 216.535 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 141.732 181.102 220.472 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 185.039 224.409 263.780 303.150 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 149.606 188.976 228.346 267.717 307.087 | 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 | - |
| ntim → ↓ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 0 in 0.000 3.937 7.874 11.811 15.748 19.685 23.622 27.559 31.496 35.433 39.370 0 in 0.000 39.370 78.740 118.110 157.480 196.850 236.220 | 1 in 0.394 4.331 8.268 12.205 16.142 20.079 24.016 27.953 31.890 35.827 10 in 3.937 43.307 82.677 122.047 161.417 200.787 240.157 | 1 cm = 0.35 2 in 0.787 4.724 8.661 12.598 16.535 20.472 24.409 28.346 32.283 36.220 20 in 7.874 47.244 86.614 125.984 165.354 204.724 244.094 | 3 in 1.181 5.118 9.055 12.992 16.929 20.866 24.803 28.740 32.677 36.614 30 in 11.811 51.181 90.551 129.921 169.291 208.661 248.031 | in 1.575 5.512 9.449 13.386 17.323 21.260 25.197 29.134 33.071 37.008 40 in 15.748 55.118 94.488 133.858 173.228 212.598 251.969 | in 1.969 5.906 9.843 13.780 17.717 21.654 25.591 29.528 33.465 37.402 50 in 19.685 59.055 98.425 137.795 177.165 216.535 255.906 | in 2.362 6.299 10.236 14.173 18.110 22.047 25.984 29.921 33.858 37.795 60 in 23.622 62.992 102.362 141.732 181.102 220.472 259.843 | in 2.756 6.693 10.630 14.567 18.504 22.441 26.378 30.315 34.252 38.189 70 in 27.559 66.929 106.299 145.669 185.039 224.409 263.780 | in 3.150 7.087 11.024 14.961 18.898 22.835 26.772 30.709 34.646 38.583 80 in 31.496 70.866 110.236 149.606 188.976 228.346 267.717 | in 3.543 7.480 11.417 15.354 19.291 23.228 27.165 31.102 35.039 38.976 90 in 35.433 74.803 114.173 153.543 192.913 232.283 271.654 | - |

Use of the tables: the number to be converted, which is made up by adding the unit at the side of a line to the unit at the head of a column, is converted to the number in the position where line and column meet. For example, 11 in = 10 in + 1 in = 279.400 mm

Inches to Millimetres 1 in = 25.4 mmNote. This table can also be used for converting milli-inches (mils or 'thou') to micrometres ('microns')

| in - | , 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | ← in |
|---|---|---|---|---|--|--|--|--|--|--|--|
| 1 | mm | mm | mm | mm | mm | mm | mm | mm | mm | mm | → |
| 0 | 0.000 | 25.400 | 50.800 | 76.200 | 101.600 | 127.000 | 152.400 | 177.800 | 203.200 | 228.600 | 0 |
| 10 | 254.000 | 279.400 | 304.800 | 330.200 | 355.600 | 381.000 | 406.400 | 431.800 | 457.200 | 482.600 | 10 |
| 20 | 508.000 | 533.400 | 558.800 | 584.200 | 609.600 | 635.000 | 660.400 | 685.800 | 711.200 | 736.600 | 20 |
| 30 | 762.000 | 787.400 | 812.800 | 838.200 | 863.600 | 889.000 | 914.400 | 939.800 | 965.200 | 990.600 | 30 |
| 40 | 1016.000 | 1041.400 | 1066.800 | 1092.200 | 1117.600 | 1143.000 | 1168.400 | 1193.800 | 1219.200 | 1244.600 | 40 |
| 50 | 1270,000 | 1295,400 | 1320.800 | 1346.200 | 1371.600 | 1397.000 | 1422.400 | 1447.800 | 1473.200 | 1498.600 | 50 |
| 60 | 1524.000 | 1549.400 | 1574.800 | 1600.200 | 1625.600 | 1651.000 | 1676.400 | 1701.800 | 1727,200 | 1752,600 | 60 |
| 70 | 1778.000 | 1803.400 | 1828.800 | 1854.200 | 1879.600 | 1905.000 | 1930.400 | 1955.800 | 1981.200 | 2006.600 | 70 |
| 80 | 2032.000 | 2057.400 | 2082.800 | 2108.200 | 2133.600 | 2159.000 | 2184.400 | 2209.800 | 2235.200 | 2260.600 | 80 |
| 90 | 2286.000 | 2311.400 | 2336.800 | 2362.200 | 2387.600 | 2413.000 | 2438.400 | 2463.800 | 2489.200 | 2514.600 | 90 |
| 100 | 2540.000 | | | | | | | | | | 100 |
| in - | - 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | ← in |
| | | | | | | | | | | | |
| + | mm | mm | mm | mm | mm | mm | mm | mm | mm | mm | 1 |
| 0 | mm 0.000 | mm 254.000 | mm 508.000 | mm 762.000 | mm 1016.000 | mm 1270.000 | mm 1524.000 | mm 1778.000 | mm 2032.000 | mm 2286.000 | |
| 0 | | | | | | | | | | | 1 |
| 100 | 0.000 | 254.000 | 508.000 | 762.000 | 1016.000 | 1270.000 | 1524.000 | 1778.000 | 2032.000 | 2286.000 | 0 100 |
| | 0.000 2540.000 | 254.000 2794.000 | 508.000 3048.000 | 762.000 3302.000 | 1016.000 3556.000 | 1270.000 3810.000 | 1524.000 4064.000 | 1778.000 4318.000 | 2032.000 4572.000 | 2286.000 4826.000 | 0 |
| 100 200 300 | 0.000 2540.000 5080.000 | 254.000 2794.000 5334.000 | 508.000 3048.000 5588.000 | 762.000 3302.000 5842.000 | 1016.000 3556.000 6096.000 | 1270.000 3810.000 6350.000 | 1524.000 4064.000 6604.000 | 1778.000 4318.000 6858.000 | 2032.000 4572.000 7112.000 | 2286.000 4826.000 7366.000 | 0 100 200 300 |
| 100 200 300 400 | 0.000 2540.000 5080.000 7620.000 | 254.000 2794.000 5334.000 7874.000 | 508.000 3048.000 5588.000 8128.000 | 762.000 3302.000 5842.000 8382.000 | 1016.000 3556.000 6096.000 8636.000 | 1270.000 3810.000 6350.000 8890.000 | 1524.000 4064.000 6604.000 9144.000 | 1778.000 4318.000 6858.000 9398.000 | 2032.000 4572.000 7112.000 9652.000 | 2286.000 4826.000 7366.000 9906.000 | 0 100 200 300 400 |
| 100 200 300 400 500 | 0.000 2540.000 5080.000 7620.000 | 254.000 2794.000 5334.000 7874.000 | 508.000 3048.000 5588.000 8128.000 | 762.000 3302.000 5842.000 8382.000 | 1016.000 3556.000 6096.000 8636.000 | 1270.000 3810.000 6350.000 8890.000 | 1524.000 4064.000 6604.000 9144.000 | 1778.000 4318.000 6858.000 9398.000 | 2032.000 4572.000 7112.000 9652.000 | 2286.000 4826.000 7366.000 9906.000 12446.000 14986.000 | 0 100 200 300 400 500 |
| 100 200 300 400 | 0.000 2540.000 5080.000 7620.000 10160.000 12700.000 | 254.000 2794.000 5334.000 7874.000 10414.000 12954.000 | 508.000 3048.000 5588.000 8128.000 10668.000 13208.000 | 762.000 3302.000 5842.000 8382.000 10922.000 13462.000 | 1016.000 3556.000 6096.000 8636.000 11176.000 13716.000 | 1270.000 3810.000 6350.000 8890.000 11430.000 13970.000 | 1524.000 4064.000 6604.000 9144.000 11684.000 14224.000 | 1778.000 4318.000 6858.000 9398.000 11938.000 14478.000 | 2032.000 4572.000 7112.000 9652.000 12192.000 14732.000 | 2286.000 4826.000 7366.000 9906.000 | 0 100 200 300 400 |
| 100 200 300 400 500 600 700 | 0.000 2540.000 5080.000 7620.000 10160.000 12700.000 15240.000 | 254.000 2794.000 5334.000 7874.000 10414.000 12954.000 15494.000 | 508.000 3048.000 5588.000 8128.000 10668.000 13208.000 15748.000 | 762.000 3302.000 5842.000 8382.000 10922.000 13462.000 16002.000 | 1016.000 3556.000 6096.000 8636.000 11176.000 13716.000 16256.000 | 1270.000 3810.000 6350.000 8890.000 11430.000 13970.000 16510.000 | 1524.000 4064.000 6604.000 9144.000 11684.000 14224.000 16764.000 | 1778.000 4318.000 6858.000 9398.000 11938.000 14478.000 17018.000 | 2032.000 4572.000 7112.000 9652.000 12192.000 14732.000 17272.000 | 2286.000 4826.000 7366.000 9906.000 12446.000 14986.000 17526.000 20066.000 | 0 100 200 300 400 500 600 700 |
| 100 200 300 400 500 600 | 0.000 2540.000 5080.000 7620.000 10160.000 12700.000 15240.000 17780.000 | 254.000 2794.000 5334.000 7874.000 10414.000 12954.000 15494.000 18034.000 | 508.000 3048.000 5588.000 8128.000 10668.000 13208.000 15748.000 18288.000 | 762.000 3302.000 5842.000 8382.000 10922.000 13462.000 16002.000 18542.000 | 1016.000 3556.000 6096.000 8636.000 11176.000 13716.000 16256.000 18796.000 | 1270.000 3810.000 6350.000 8890.000 11430.000 13970.000 16510.000 19050.000 | 1524.000 4064.000 6604.000 9144.000 11684.000 14224.000 16764.000 19304.000 | 1778.000 4318.000 6858.000 9398.000 11938.000 14478.000 17018.000 19558.000 | 2032.000 4572.000 7112.000 9652.000 12192.000 14732.000 17272.000 19812.000 | 2286.000 4826.000 7366.000 9906.000 12446.000 14986.000 17526.000 | 0 100 200 300 400 500 600 |

Millimetres to Inches 1 mm = 0.039 370 in

Note. This table can also be used for converting micrometres ('microns') to milli-inches (mils or 'thou')

| mm → | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | ← mm |
|------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|------|
| 1 | in | 7 + |
| 0 | 0.000 | 0.039 | 0.079 | 0.118 | 0.157 | 0.197 | 0.236 | 0.276 | 0.315 | 0.354 | 0 |
| 10 | 0.394 | 0.433 | 0.472 | 0.512 | 0.551 | 0.591 | 0.630 | 0.669 | 0.709 | 0.748 | 10 |
| 20 | 0.787 | 0.827 | 0.866 | 0.906 | 0.945 | 0.984 | 1.024 | 1.063 | 1.102 | 1.142 | 20 |
| 30 | 1.181 | 1.220 | 1.260 | 1.299 | 1.339 | 1.378 | 1.417 | 1.457 | 1.496 | 1.535 | 30 |
| 40 | 1.575 | 1.614 | 1.654 | 1.693 | 1.732 | 1.772 | 1.811 | 1.850 | 1.890 | 1.929 | 40 |
| 50 | 1.969 | 2.008 | 2.047 | 2.087 | 2.126 | 2.165 | 2.205 | 2.244 | 2.283 | 2.323 | 50 |
| 60 | 2.362 | 2.402 | 2.441 | 2.480 | 2.520 | 2.559 | 2.598 | 2.638 | 2.677 | 2.717 | 60 |
| 70 | 2.756 | 2.795 | 2.835 | 2.874 | 2.913 | 2.953 | 2.992 | 3.031 | 3.071 | 3.110 | 70 |
| 80 | 3.150 | 3.189 | 3.228 | 3.268 | 3.307 | 3.346 | 3.386 | 3.425 | 3.465 | 3.504 | 80 |
| 90 | 3.543 | 3.583 | 3.622 | 3.661 | 3.701 | 3.740 | 3.780 | 3.819 | 3.858 | 3.898 | 90 |
| 100 | 3.937 | | | | | | | | | | 100 |
| mm → | . 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | ← mm |
| 1 | in | 7 + |
| o | 0.000 | 0.394 | 0.787 | 1.181 | 1.575 | 1.969 | 2.362 | 2.756 | 3.150 | 3.543 | 0 |
| 100 | 3.937 | 4.331 | 4.724 | 5.118 | 5.512 | 5.906 | 6.299 | 6.693 | 7.087 | 7.480 | 100 |
| 200 | 7.874 | 8.268 | 8.661 | 9.055 | 9.449 | 9.843 | 10.236 | 10.630 | 11.024 | 11.417 | 200 |
| 300 | 11.811 | 12.205 | 12.598 | 12.992 | 13.386 | 13.780 | 14.173 | 14.567 | 14.961 | 15.354 | 300 |
| 400 | 15.748 | 16.142 | 16.535 | 16.929 | 17.323 | 17.717 | 18.110 | 18.504 | 18.898 | 19.291 | 400 |
| 500 | 19.685 | 20.079 | 20.472 | 20.866 | 21.260 | 21.654 | 22.047 | 22.441 | 22.835 | 23 228 | 500 |
| 600 | 23.622 | 24.016 | 24.409 | 24.803 | 25.197 | 25.591 | 25.984 | 26.378 | 26.772 | 27.165 | 600 |
| 700 | 27.559 | 27.953 | 28.346 | 28.740 | 29.134 | 29.528 | 29.921 | 30.315 | 30.709 | 31.102 | 700 |
| 800 | 31.496 | 31.890 | 32.283 | 32.677 | 33.071 | 33.465 | 33:858 | 34.252 | 34.646 | 35.039 | 800 |
| 900 | 35.433 | 35.827 | 36.220 | 36.614 | 37.008 | 37.402 | 37.795 | 38.189 | 38.583 | 38.976 | 900 |
| 1000 | 39.370 | | | | | | | | | | 1000 |

Conversions: length

Use of the table: the number of inches to be converted, which is made up by the number of inches at the head of a column and the fraction at the side of a line, is converted to the number in the position where line and column meet. For example, $1\,1/64$ in = 1 in + 1/64 in = 25.797 mm

| Inches | s and fracti | ions of a | n inch te | o Millim | etres | 1 in = 2 | 25.4 mm | | | | | | |
|------------------|------------------|------------------|------------------------------|------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|----------------|
| in - | → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | ← in |
| ↓ [| mm | mm | mm | mm | mm | mm | mm | mm | mm | mm | mm | mm | 1 |
| o | 0.000 | 25.400 | 50.800 | 76.200 | 101.600 | 127.000 | 152.400 | 177.800 | 203.200 | 228.600 | 254.000 | 279.400 | 0 |
| 1/64 | 0.397 | 25.797 | 51.197 | 76.597 | 101.997 | 127.397 | 152.797 | 178.197 | 203.597 | 228.997 | 254.397 | 279.797 | 1/64 |
| 1/32 | 0.794 | 26.194 | 51.594 | 76.994 | 102.394 | 127.794 | 153.194 | 178.594 | 203.994 | 229.394 | 254.794 | 280.194 | 1/32 |
| 3/64 | 1.191 | 26.591 | 51.991 | 77.391 | 102.791 | 128.191 | 153.591 | 178.991 | 204.391 | 229.791 | 255.191 | 280.591 | 3/64 |
| 1/16 | 1.588 | 26.988 | 52.388 | 77.788 | 103.188 | 128.588 | 153.988 | 179.388 | 204.788 | 230.188 | 255.588 | 280.988 | 1/16 |
| 5/64 | 1.984 | 27.384 | 52.784 | 78.184 | 103.584 | 128.984 | 154.384 | 179.784 | 205.184 | 230.584 | 255.984 | 281.384 | 5/64 |
| 3/32 | 2.381 | 27.781 | 53.181 | 78.581 | 103.981 | 129.381 | 154.781 | 180.181 | 205.581 | 230.981 | 256.381 | 281.781 | 3/32 |
| 7/64 | 2.778 | 28.178 | 53.578 | 78.978 | 104.378 | 129.778 | 155.178 | 180.578 | 205.978 | 231.378 | 256.778 | 282.178 | 7/64 |
| 1/8 | 3.175 | 28.575 | 53.975 | 79.375 | 104.775 | 130.175 | 155.575 | 180.975 | 206.375 | 231.775 | 257.175 | 282.575 | 1/8 |
| 9/64 | 3.572 | 28.972 | 54.372 | 79.772 | 105.172 | 130.572 | 155.972 | 181.372 | 206.772 | 232.172 | 257.572 | 282.972 | 9/64 |
| 5/32 | 3.969 | 29.369 | 54.769 | 80.169 | 105.569 | 130.969 | 156.369 | 181.769 | 207.169 | 232.569 | 257.969 | 283.369 | 5/32 |
| 11/64 | 4.366 | 29.766 | 55.166 | 80.566 | 105.966 | 131.366 | 156.766 | 182.166 | 207.566 | 232.966 | 258.366 | 283.766 | 11/64 |
| 3/16 | 4.762 | 30.162 | 55.562 | 80.962 | 106.362 | 131.762 | 157.162 | 182.562 | 207.962 | 233.362 | 258.762 | 284.162 | 3/16 |
| 13/64 | 5.159 | 30.559 | 55.959 | 81.359 | 106.759 | 132.159 | 157.559 | 182.959 | 208.359 | 233.759 | 259.159 | 284.559 | 13/64 |
| 7/32 | 5.556 | 30.956 | 56.356 | 81.756 | 107.156 | 132.556 | 157.956 | 183.356 | 208.756 | 234.156 | 259.556 | 284.956 | 7/32 |
| 15/64 | 5.953 | 31.353 | 56.753 | 82.153 | 107.553 | 132.953 | 158.353 | 183.753 | 209.153 | 234.553 | 259.953 | 285.353 | 15/64 |
| 1/4 | 6.350 | 31.750 | 57.150 | 82.550 82.947 | 107.950 108.347 | 133.350 133.747 | 158.750 159.147 | 184.150 184.547 | 209.550 209.947 | 234.950 235.347 | 260.350 260.747 | 285.750 286.147 | 1/4 17/64 |
| 17/64 | 6.747 | 32.147 | 57.547 57.944 | 83.344 | 108.347 | 134.144 | 159.147 | 184 944 | 210.344 | 235.744 | 261.144 | 286.544 | 9/32 |
| 9/32 | 7.144 | 32.544 32.941 | 57. 344 58.341 | 83.741 | 109.744 | 134.144 | 159.941 | 185.341 | 210.344 | 236.141 | 261.541 | 286.941 | 19/64 |
| 19/64 | 7.541 7.938 | 33.338 | 58.738 | 84.138 | 109.141 | 134.938 | 160.338 | 185.738 | 210.741 | 236.538 | 261.938 | 287.338 | 5/16 |
| 5/16 21/64 | 8.334 | 33.734 | 59.134 | 84.534 | 109.934 | 135.334 | 160.734 | 186.134 | 211.534 | 236.934 | 262.334 | 287.734 | 21/64 |
| 11/32 | 8.731 | 34.131 | 59.531 | 84.931 | 110.331 | 135.731 | 161.131 | 186.531 | 211.931 | 237.331 | 262.731 | 288.131 | 11/32 |
| 23/64 | 9.128 | 34.528 | 59.928 | 85.328 | 110.728 | 136.128 | 161.528 | 186.928 | 212.328 | 237.728 | 263.128 | 288.528 | 23/64 |
| 3/8 | 9.525 | 34.925 | 60.325 | 85.725 | 111.125 | 136.525 | 161.925 | 187.325 | 212.725 | 238.125 | 263.525 | 288.925 | 3/8 |
| 25/64 | 9.922 | 35.322 | 60.722 | 86.122 | 111.522 | 136.922 | 162.322 | 187.722 | 213.122 | 238.522 | 263.922 | 289.322 | 25/64 |
| 13/32 | 10.319 | 35.719 | 61.119 | 86.519 | 111.919 | 137.319 | 162.719 | 188.119 | 213.519 | 238.919 | 264.319 | 289.719 | 13/32 |
| 27/64 | 10.716 | 36.116 | 61.516 | 86.916 | 112.316 | 137.716 | 163.116 | 188.516 | 213.916 | 239.316 | 264.716 | 290.116 | 27/64 |
| 7/16 | 11.112 | 36.512 | 61.912 | 87.312 | 112.712 | 138.112 | 163.512 | 188.912 | 214.312 | 239.712 | 265.112 | 290.512 | 7/16 |
| 29/64 | 11.509 | 36.909 | 62.309 | 87.709 | 113.109 | 138.509 | 163.909 | 189.309 | 214.709 | 240.109 | 265.509 | 290.909 | 29/64 |
| 15/32 | 11.906 | 37.306 | 62.706 | 88.106 | 113.506 | 138.906 | 164.306 | 189.706 | 215.106 | 240.506 | 265.906 | 291.306 | 15/32 |
| 31/64 | 12.303 | 37.703 | 63.103 | 88.503 | 113.903 | 139.303 | 164.703 | 190.103 | 215.503 | 240.903 | 266.303 | 291.703 | 31/64 |
| 1/2 | 12.700 | 38.100 | 63.500 | 88.900 | 114.300 | 139.700 | 165.100 | 190.500 | 215.900 | 241.300 | 266.700 | 292.100 | 1/2 |
| 33/64 | 13.097 | 38.497 | 63.897 | 89.297 | 114.697 | 140.097 | 165.497 | 190.897 | 216.297 | 241.697 | 267.097 | 292.497 | 33/64 |
| 17/32 | 13.494 | 38.894 | 64.294 | 89.694 | 115.094 | 140.494 | 165.894 | 191.294 | 216.694 | 242.094 | 267.494 | 292.894 | 17/32 |
| 35/64 | 13.891 | 39.291 | 64.691 | 90.091 | 115.491 | 140.891 | 166.291 | 191.691 | 217.091 | 242.491 | 267.891 | 293.291 | 35/64 |
| 9/16 | 14.288 | 39.688 | 65.088 | 90.488 | 115.888 | 141.288 | 166.688 | 192.088 | 217.488 | 242.888 | 268.288 | 293.688 | 9/16 |
| 37/64 | 14.684 | 40.084 | 65.484 | 90.884 | 116.284 | 141.684 | 167.084 | 192.484 | 217.884 | 243.284 | 268.684 | 294.084 | 37/64 |
| 19/32 39/64 | 15.081 15.478 | 40.481 40.878 | 65.881 66.278 | 91.281 91.678 | 116.681 117.078 | 142.081 142.478 | 167.481 167.878 | 192.881 193.278 | 218.281 218.678 | 243.681 244.078 | 269.081 269.478 | 294.481 294.878 | 19/32 39/64 |
| | | | | | | 1 42 075 | | | 210.075 | | | | F/0 |
| 5/8 | 15.875 | 41.275 | 66.675 67.072 | 92.075 92.472 | 117.475 117.872 | 142.875 143.272 | 168.275 168.672 | 193.675 194.072 | 219.075 219.472 | 244.475 244.872 | 269.875 270.272 | 295.275 295.672 | 5/8 41/64 |
| 41/64 | 16.272 | 41.672 | 67.469 | 92.869 | 118.269 | 143.272 | 169.069 | 194.469 | 219.869 | 245.269 | 270.272 | 295.672 | 21/32 |
| 21/32 43/64 | 16.669 17.066 | 42.069 42.466 | 67.866 | 93.266 | 118.666 | 144.066 | 169.466 | 194.866 | 220.266 | 245.666 | 271.066 | 296.466 | 43/64 |
| 11/16 | 17.462 | 42.862 | 68.262 | 93.662 | 119.062 | 144.462 | 169.862 | 195.262 | 220.662 | 246.062 | 271.462 | 296.862 | 11/16 |
| اممنحما | 17.859 | 43.259 | 68.659 | 94.059 | 119.459 | 144.859 | 170.259 | 195.659 | 221.059 | 246.459 | 271.859 | 297.259 | 45/64 |
| 23/32 | 18.256 | 43.656 | 69.056 | 94.456 | 119.856 | 145.256 | 170.656 | 196.056 | 221.456 | 246.856 | 272.256 | 297.656 | 23/32 |
| 47/64 | 18.653 | 44.053 | 69.453 | 94.853 | 120.253 | 145.653 | 171.053 | 196.453 | 221.853 | 247.253 | 272.653 | 298.053 | 47/64 |
| 3/4 | 19.050 | 44.450 | 69.850 | 95.250 | 120.650 | 146.050 | 171.450 | 196.850 | 222.250 | 247.650 | 273.050 | 298.450 | 3/4 |
| 49/64 | 19.447 | 44.847 | 70.247 | 95.647 | 121.047 | 146.447 | 171.847 | 197.247 | 222.647 | 248.047 | 273.447 | 298.847 | 49/64 |
| 25/32 | 19.844 | 45.244 | 70.644 | 96.044 | 121.444 | 146.844 | 172.244 | 197.644 | 223.044 | 248.444 | 273.844 | 299.244 | 25/32 |
| 51/64 | 20.241 | 45.641 | 71.041 | 96,441 | 121.841 | 147.241 | 172.641 | 198.041 | 223.441 | 248.841 | 274.241 | 299.641 | 51/64 |
| 13/16 | 20.638 | 46.038 | 71.438 | 96.838 | 122.238 | 147.638 | 173.038 | 198.438 | 223.838 | 249.238 | 274.638 | 300.038 | 13/16 |
| 53/64 | 21.034 | 46.434 | 71.834 | 97.234 | 122.634 | 148.034 | 173.434 | 198.834 | 224.234 | 249.634 | 275.034 | 300.434 | 53/64 |
| 27/32 | 21.431 | 46.831 | 72.231 | 97.631 | 123.031 | 148.431 | 173.831 | 199.231 | 224.631 | 250.031 | 275.431 | 300.831 | 27/32 |
| 55/64 | 21.828 | 47.228 | 72.628 | 98.028 | 123.428 | 148.828 | 174.228 | 199.628 | 225.028 | 250.428 | 275.828 | 301.228 | 55/64 |
| 7/8 | 22.225 | 47.625 | 73.025 | 98.425 | 123.825 | 149.225 | 174.625 | 200.025 | 225.425 | 250.825 | 276.225 | 301.625 | 7/8 |
| 57/64 | 22.622 | 48.022 | 73.422 | 98.822 | 124.222 | 149.622 | 175.022 | 200.422 | 225.822 | 251.222 | 276.622 | 302.022 | 57/64 |
| 29/32 | 23.019 | 48.419 | 73.819 | 99.219 | 124.619 | 150.019 | 175.419 | 200.819 | 226.219 | 251.619 | 277.019 | 302.419 | 29/32 |
| 59/64 | 23.416 | 48.816 | 74.216 | 99.616 | 125.016 | 150.416 | 175.816 | 201.216 | 226.616 | 252.016 | 277.416 | 302 816 | 59/64 |
| 15/16 | 23.812 | 49.212 | 74.612 | 100.012 | 125.412 | 150.812 | 176.212 | 201.612 | 227.012 | 252.412 | 277.812 | 303.212 | 15/16 |
| 61/64 | 24.209 | 49.609 | 75.009 | 100.409 | 125.809 | 151.209 | 176.609 | 202.009 | 227.409 | 252.809 | 278.209 | 303.609 | 61/64 |
| 31/32 | 24.606 | 50.006 | 75.406 | 100.806 | 126.206 | 151.606 | 177.006 | 202.406 | 227.806 | 253.206 | 278.606 | 304.006 | 31/32 |
| 63/64 | 25.003 | 50.403 | 75.803 | 101.203 | 126.603 | 152.003 | 177.403 | 202.803 | 228.203 | 253.603 | 279.003 | 304.403 | 63/64 |

$Fractions\ to\ Decimals$

| | Decimal equivaler | t | Fraction | Decimal equivalent | | Fraction 1/2's | ns 1/4's | 8ths | 16ths | 32nds | 64ths | Decimal equivalent (all figures are exact |
|--|---|--|--|--|---|----------------|-------------|------|---------------------------|--|--|--|
| 1/2 | 0.5 | | 1/32 | 0.031 25 | | | | | | | 1 | 0.015 625 |
| 1/3 | 0.333 33 | 2 | 1/32 | 0.031 25 | | | | | | 1 | 2 | 0.013 023 |
| | 0.333 33 | , | | 0.029 412 | | | | | | • | 3 | |
| 1/4 | | | 1/34 | | | | | | 1 | 2 | 4 | 0.046 875 |
| 1/5 | 0.2 | , | 1/35 | 0.028 571 | | | | | , | 2 | 5 | 0.062 5 |
| /6 | 0.166 66 | , | 1/36 | 0.027 778 | | | | | | 2 | | 0.078 125 |
| | 0 1 42 DE | , | 1/37 | 0.027 027 | | | | | | 3 | 6 | 0.093 75 |
| /7 | 0.142 85 | ' | | 0.027 027 | | | | | • | | 7 | 0.109 375 |
| 1/8 | 0.125 | 1 | 1/38 | | | | | 1 | 2 | 4 | 8 | 0.125 |
| 1/9 | 0.111 11 | ١. | 1/39 | 0.025 641 | | | | | | | • | 0.4.40.00= |
| 1/10 | 0.1 | | 1/40 | 0.025 | | | | | | _ | 9 | 0.140 625 |
| 1/11 | 0.090 90 | 9 | 1/41 | 0.024 390 | | | | | | 5 | 10 | 0.156 25 |
| | | _ | 4 440 | | | | | | | • | 11 | 0.171 875 |
| 1/12 | 0.083 33 | | 1/42 | 0.023 810 | | | | | 3 | 6 | 12 | 0.187 5 |
| 1/13 | 0.076 92 | | 1/43 | 0.023 256 | | | | | | | 13 | 0.203 125 |
| 1/14 | 0.071 42 | | 1/44 | 0.022 727 | | | | | | 7 | 14 | 0.218 75 |
| 1/15 | 0.066 66 | , | 1/45 | 0.022 222 | | | | • | | | 15 | 0.234 375 |
| 1/16 | 0.062 5 | | 1/46 | 0.021 739 | | | 1 | 2 | 4 | 8 | 16 | 0.25 |
| | 0.050.00 | | 4 / 4 7 | 0.004.077 | | | | | | | 4 - | |
| 1/17 | 0.058 82 | | 1/47 | 0.021 277 | | | | | | | 17 | 0.265 625 |
| 1/18 | 0.055 55 | | 1/48 | 0.020 833 | | | | | | 9 | 18 | 0.281 25 |
| 1/19 | 0.052 63 | 2 | 1/49 | 0.020 408 | | | | | _ | 4.0 | 19 | 0.296 875 |
| 1/20 | 0.05 | _ | 1/50 | 0.02 | | | | | 5 | 10 | 20 | 0.3125 |
| 1/21 | 0.047 61 | 9 | 1/51 | 0.019 608 | | | | | | | 21 | 0.328 125 |
| | | | | | | | | | | 11 | 22 | 0.343 75 |
| 1/22 | 0.045 45 | | 1/52 | 0.019 231 | | | | | | | 23 | 0.359 375 |
| 1/23 | 0.043 47 | | 1/53 | 0.018 868 | | | | 3 | 6 | 12 | 24 | 0.375 |
| 1/24 | 0.041 66 | 7 | 1/54 | 0.018 519 | | | | | | | | |
| 1/25 | 0.04 | | 1/55 | 0.018 182 | | | | | | | 25 | 0.390 625 |
| 1/26 | 0.038 46 | 2 | 1/56 | 0.017 857 | | | | | | 13 | 26 | 0.406 25 |
| | | | | | | | | | | | 27 | 0.421 875 |
| 1/27 | 0.037 03 | 7 | 1/57 | 0.017 544 | | | | | 7 | 14 | 28 | 0.437 5 |
| 1/4/ | | A | 1/58 | 0.017 241 | | | | | | | 29 | 0.453 125 |
| | 0.035 71 | 4 | | | | | | | | | | |
| 1/28 | | | | | | | | | | 15 | | |
| 1/28 1/29 | 0.034 48 | 3 | 1/59 | 0.016 949 | | | | | | 15 | 30 | 0.468 75 |
| 1/27 1/28 1/29 1/30 1/31 | | 3 3 | | | | 1 | 2 | 4 | 8 | 15 16 | | |
| 1/28 1/29 1/30 1/31 | 0.034 48 0.033 33 0.032 25 | 3 3 8 | 1/59 1/60 | 0.016 949 0.016 667 | | 1 | 2 | 4 | 8 | | 30 31 32 | 0.468 75 0.484 375 0.5 |
| 1/28 1/29 1/30 1/31 Note. Fo | 0.034 48 0.033 33 0.032 25 or the decimal | 3 3 8 equivalent c | 1/59 1/60 of other fracti | 0.016 949 0.016 667 ons with | | 1 | 2 | 4 | 8 | 16 | 30 31 32 33 | 0.468 75 0.484 375 0.5 0.515 625 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a | 3 3 8 equivalent o number from | 1/59 1/60 of other fracti 0.01 to 100 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | 8 | | 30 31 32 33 34 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun | 0.034 48 0.033 33 0.032 25 or the decimal | 3 3 8 equivalent o number from | 1/59 1/60 of other fracti 0.01 to 100 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | | 16 17 | 30 31 32 33 34 35 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a | 3 3 8 equivalent o number from | 1/59 1/60 of other fracti 0.01 to 100 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | 8 | 16 | 30 31 32 33 34 35 36 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a | 3 3 8 equivalent o number from | 1/59 1/60 of other fracti 0.01 to 100 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | | 16 17 18 | 30 31 32 33 34 35 36 37 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | 3 3 8 equivalent o number from | 1/59 1/60 f other fracti n 0.01 to 100 es 144–147. | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | | 16 17 | 30 31 32 33 34 35 36 37 38 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | 3 3 8 equivalent c number fron procals, pag | 1/59 1/60 If other fraction 0.01 to 100 es 144–147. | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | | 9 | 16 17 18 19 | 30 31 32 33 34 35 36 37 38 39 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | 3 3 8 equivalent c number fron procals, pag | 1/59 1/60 f other fracti n 0.01 to 100 es 144–147. | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | 4 | | 16 17 18 | 30 31 32 33 34 35 36 37 38 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | 3 3 8 equivalent c number fron procals, pag | 1/59 1/60 of other fracti n 0.01 to 100 es 144–147. Decimal equivale | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | | 9 | 16 17 18 19 | 30 31 32 33 34 35 36 37 38 39 40 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 0.625 |
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| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | 3 3 8 equivalent c number from procals, pag 24ths 1 2 3 4 5 | 1/59 1/60 of other fracti n 0.01 to 100 es 144–147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | 2 | | 9 | 16 17 18 19 20 21 22 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 0.625 0.640 625 0.656 25 0.671 875 |
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| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin Fraction 3rds | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec | agential age | 1/59 1/60 of other fraction 0.01 to 100 es 144–147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 0.25 0.291 66 0.333 33 | 0.016 949 0.016 667 ons with 0.9 as | | | | 5 | 9 10 11 | 16 17 18 19 20 21 22 23 24 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 0.625 0.640 625 0.671 875 0.687 5 0.703 125 0.718 75 0.734 375 0.75 |
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| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin Fraction 3rds | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec 1 1 1 2 3 2 4 5 3 6 | 3 3 8 8 equivalent c number from procals, pag 24ths 1 2 3 4 5 6 7 8 9 10 11 12 13 | 1/59 1/60 of other fracti n 0.01 to 100 es 144–147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 0.25 0.291 66 0.333 33 0.375 0.416 66 0.458 33 0.5 | 0.016 949 0.016 667 ons with 0.9 as | | , | | 5 | 9 10 11 12 | 16 17 18 19 20 21 22 23 24 25 26 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.562 5 0.578 125 0.593 75 0.609 375 0.625 0.640 625 0.671 875 0.687 5 0.703 125 0.718 75 0.734 375 0.75 0.765 625 0.781 25 0.796 875 0.796 875 0.812 5 0.812 5 0.812 5 |
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| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin Fraction 3rds | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec 1 1 2 3 2 4 5 3 6 7 | 3 3 8 8 equivalent on number from procals, pages 24ths 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 | 1/59 1/60 of other fracti in 0.01 to 100 es 144–147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 0.25 0.291 66 0.333 33 0.375 0.416 66 0.458 33 0.5 0.541 66 0.583 33 0.625 0.666 66 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | | 5 | 9 10 11 12 | 16 17 18 19 20 21 22 23 24 25 26 27 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 0.625 0.640 625 0.671 875 0.687 5 0.703 125 0.718 75 0.734 375 0.75 0.765 625 0.791 25 0.791 25 |
| 1/28 1/29 1/30 1/31 Note. Fo 1 as nun denomin Fraction 3rds | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec 1 1 2 3 2 4 5 3 6 7 4 8 | 3 3 8 8 equivalent on number from procals, pages 24ths 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 | 1/59 1/60 of other fraction 0.01 to 100 es 144–147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 0.25 0.291 66 0.333 33 0.375 0.416 66 0.458 33 0.541 66 0.583 33 0.625 0.666 66 | 0.016 949 0.016 667 ons with 0.9 as | | | | 5 | 9 10 11 12 | 16 17 18 19 20 21 22 23 24 25 26 27 28 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 56 57 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 125 0.593 75 0.609 375 0.625 0.640 625 0.671 875 0.687 5 0.703 125 0.718 75 0.734 375 0.75 0.765 625 0.765 625 0.765 625 0.765 625 0.796 875 0.828 125 0.828 125 0.828 125 0.859 375 0.875 |
| 1/28 1/29 1/30 1/31 Note. Fo I as nun denomin Graction 3rds | 0.034 48 0.033 33 0.032 25 or the decimal nerator, and a nator, see rec 1 1 2 3 2 4 5 3 6 7 | 3 3 3 8 equivalent of number from procals, page 24ths 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 16 17 18 | 1/59 1/60 If other fracti n 0.01 to 100 es 144—147. Decimal equivale 0.041 66 0.083 33 0.125 0.166 66 0.208 33 0.25 0.291 66 0.458 33 0.5 0.541 66 0.583 33 0.625 0.666 66 | 0.016 949 0.016 667 ons with 0.9 as | | 1 | | 5 | 9 10 11 12 | 16 17 18 19 20 21 22 23 24 25 26 27 | 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 | 0.468 75 0.484 375 0.5 0.515 625 0.531 25 0.546 875 0.562 5 0.578 1 25 0.609 375 0.609 375 0.625 0.640 625 0.671 875 0.703 1 25 0.718 75 0.703 1 25 0.718 75 0.75 0.765 625 0.778 1 25 0.796 875 0.812 5 0.828 1 25 0.843 75 0.859 375 0.875 0.890 625 0.906 25 |
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Feet to Inches 3 Ft. 4 Ft. 5 Ft. 6 Ft. 2 Ft. 72"

CONVERSION TABLE

36" 48" 60" 24"

0"

1"

2"

3"

4"

5"

6"

7"

8"

9"

10"

11"

MEASURING NUTS AND BOLTS

Nuts and bolts come in a great variety of sizes. The size of the head of a bolt or nut is measured between the flat sides of the hexagon. In standard American nuts and bolts these sizes usually follow one another in 1/16" steps. Thus you have 1/2" (8/16") bolts and 9/16" bolts and 5/8" (10/16") bolts, but you don't find 2/3" bolts. Foreign cars use metric-sized nuts and bolts which are measured in the same way from flat side to flat side. but in millimeters instead of sixteenths of an inch. Some English cars use yet another way of measuring head sizes known as the "Whitworth system." Instead of measuring from flat to flat of the hexagon, Whitworth sizes measure from point to point. Fortunately most British manufacturers have switched over to metric sizes or standard American sizes.

Unfortunately, head size isn't all there is to measuring nuts and bolts. Bolts are also measured by diameter—that is, through the threads. Thus you could have a bolt with a 1/2" head and a diameter of 1/4" or one with a 1/2" head and a 3/16" diameter. Nuts are measured for diameter across the widest opening the threads make.

As if this weren't enough, nuts and bolts (and studs and screws as well) are also measured according to how coarse or fine their threads are. This measurement is made in "threads per inch." A bolt with 16 threads per inch is rather coarsely threaded. Twenty threads per inch is a fine thread.

Once in a while you will run into a nut or a bolt which has left-hand thread. This means it screws in counterclockwise and screws out clockwise. Often left-hand thread nuts and bolts have a little "L" marked on them. Sometimes they don't—then you just have to try turning the "wrong" way and see what happens.

WRENCH SIZES

The size of a wrench refers to the size of the nut or bolt it fits (see Appendix, p. 92, on measuring sizes of nuts and bolts). Most sets of American wrenches start at 3/8" and go up in steps of 1/16". The largest wrench in a set might be anywhere from 3/4" to 1-5/16". (What we call "American" wrenches are also known as SAE [Society of Automotive Engineers] wrenches.) Wrenches smaller than 3/8" are called "miniatures" or "ignition" wrenches. There are also metric wrenches, which you will need if you want to work on foreign cars.

Americans spend a good deal of time in school learning a chaotic system of weights and measures and forget most of it rapidly. Most of us remember that there are 12 inches in a foot and 3 feet in a yard and even that there are 5,280 feet in a mile. Hardly anyone knows how big an acre is or how many pints there are in a gallon or . . .

Most of our units of weight and measure had different origins at different times. An inch was three barleycorns laid end to end. A foot was the length of Charlemagne's foot (he had big feet). A yard was the distance from the tip of Henry I's nose to the tip of his outstretched arm. Roman legions used to count off paces as they marched—a thousand paces (mille passuum) was roughly 5,000 feet and the English changed the name to "mile."

As you can see, our system of measure has its roots in Roman imperialism, feudal class structure and an agricultural economy. Not very relevant to a technological industrial society.

Most countries had different and equally illogical systems of measure until the French Revolution came along. The French revolutionaries decided they needed a more orderly and convenient system and chose the meter (3.28 feet) as the standard unit of measure ("meter" comes from the Greek word for measure). They then derived all other units of measure from the meter in multiples of 10 or 1/10. A centimeter is 1/100 of a meter and a millimeter is 1/1000 of a meter. A kilometer is 1000 meters. A liter is 1000 cubic centimeters and a kilo ("key" for short) is the weight of a liter of water. Neat and easy.

Over the years other countries adopted the metric system or had it forced upon them by imperialist colonizers from one European state or another, until only the English-speaking countries were holding out. Now Great Britain and the Commonwealth are in the middle of a ten-year switch-over, leaving the U.S. as the lone non-metric nation in the world. In every other country school

children can learn their system of measure in a month. In the U.S. we spend years getting a partial grip on our system of measure.

What all this means to you as an auto mechanic is that you may need two sets of wrenches—one for American-built cars and another for foreign makes. Most English cars are using metric nuts and bolts by now (although a few still use the Whitworth system—see Appendix, p. 92).

Metric wrench sets start with 6 or 7 mm. (millimeters) and go up to 19 mm. in 1 mm. intervals. Sixteen and 18 mm. wrenches are not usually included in metric sets. Fortunately, 16 and 18 mm. nuts and bolts are not usually included on cars.

If you are going to do a lot of work on foreign cars you have to get yourself a set of metric combination wrenches and sockets. If it's just a question of tightening one nut on a Volkswagen, you may find that you can fake it with your American wrenches. Several sizes in the American and metric systems are close enough to be almost interchangeable. Unfortunately most of these switches work in one direction only: you can use a wrench which is slightly too big on a bolt, but you can't use one which is a little too small. The table shows you which fakes you can get away with. Try not to use it just because you're too lazy to fetch the right wrench out of your tool box!

MICKEY MOUSE'S METRIC CONVERSION CHART

| | WRENCH SIZE | FITS | BOLT SIZE |
|-----------|-------------|------|-----------|
| American | 3/8 | | 9 mm |
| to metric | 7/16 | | 11 mm |
| | 9/16 | | 14 mm |
| | 11/16 | | 17 mm |
| | 3/4 | | 19 mm |
| Metric to | 10 mm | | 3/8 |
| American | 11 mm | | 7/16* |
| | 13 mm | | 1/2 |
| | 17 mm | | 5/8 |
| | 19 mm | | 3/4* |
| | 21 mm | | 13/16 |
| | * sometim | es | |

Hose Clips

Pipe clips are extremely confusingly sized by the various manufacturers and the list below will be of some help in sorting out the ridiculous situation. Use ONLY stainless steel clips.

| 000 M00 | 3/8" — 1/2" 3/8" — 5/8" | 9 — 13mm 9 — 16mm |
|------------|------------------------------------|----------------------|
| 00 | $\frac{78}{1/2}'' - \frac{3}{4}''$ | 13 — 19mm |
| 0 | 5/8" — 7/8" | 16 — 22mm |
| - | $\frac{98}{34''} - \frac{98}{1''}$ | |
| 0X | | 19 — 25mm |
| 1A | 7⁄8″ — 11∕8″ | 22 — 28mm |
| 1 | 1" — 13/8" | 25 — 35mm |
| 1X | 11/8" — 15/8" | 28 — 41mm |
| 2A | 11/4" — 11/8" | 32 — 48mm |
| 2 | 11/2" — 21/8" | 38 — 54mm |
| 2X · | 13/4" — 23/8" | 44 — 60mm |
| 3 | $2'' - 2^{3/4}''$ | 50 — 70mm |
| 3X | 23/8" — 31/8" | 60 — 80mm |
| | | |

Machine Screws

Due to standardisation over recent years, the metric equivalent of the machine screws listed below should be used as imperial sizes may be more than double the cost.

d

| British Standard | Met | proximate tric Thread uivalent | | 75% Tap Thread Drill Size |
|---|-----|--------------------------------------|--------------------------------------|------------------------------|
| 16 " (.187 1/4" (.25) 1/6 " (.312 3/8" (.375 1/2" (0.5) | 25) | M5 M6 M8 M10 M12 | 7 " 32 " 64 3/8" 7 " 9 " | 32" 37" 32 17" 64 21" 64 7" |

Metal & Wire Gauge Equivalents

It is useful to have the tables to hand as there is nothing more infuriating than being unable to communicate with a supplier or to have gauge numbers with no way of converting them to really useful equivalents, such as thickness. This usually occurs at a weekend according to Murphy's Law.

| Inches | | Imperial Thick | Metric (ness |
|--|---|---|---|
| 2 | 4 | | |
| 3 | | 0.3 | |
| 4 0.232 5.88 5 0.212 5.38 6 0.192 4.87 7 0.176 4.46 8 0.160 4.06 9 0.144 3.66 10 0.128 3.25 11 0.116 2.94 12 0.104 2.64 13 0.092 2.34 14 0.080 2.00 15 0.072 1.83 16 0.064 1.62 17 0.056 1.42 18 0.048 1.22 19 0.040 1.01 20 0.036 0.91 21 0.032 0.81 22 0.028 0.71 23 0.024 0.61 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial Thickness inches mm 30 0.0124 0.314 29 0.0136 0.345 28 0.014 0.36 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial Action Control C | 2 | | |
| 5 0.212 5.38 6 0.192 4.87 7 0.176 4.46 8 0.160 4.06 9 0.144 3.66 10 0.128 3.25 11 0.116 2.94 12 0.104 2.64 13 0.092 2.34 14 0.080 2.00 15 0.072 1.83 16 0.064 1.62 17 0.056 1.42 18 0.048 1.22 19 0.040 1.01 20 0.036 0.91 21 0.032 0.81 22 0.028 0.71 23 0.024 0.61 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 | 3 | | |
| 6 0.192 4.87 7 0.176 4.46 8 0.160 4.06 9 0.144 3.66 10 0.128 3.25 11 0.116 2.94 12 0.104 2.64 13 0.092 2.34 14 0.080 2.00 15 0.072 1.83 16 0.064 1.62 17 0.056 1.42 18 0.048 1.22 19 0.040 1.01 20 0.036 0.91 21 0.032 0.81 22 0.028 0.71 23 0.024 0.61 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial Metric Thickness inches mm 30 0.012 0.30 Standard Wire Gauge Imperial Metric Thickness inches 0.345 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial 0.314 29 0.0136 0.345 29 0.013 0.33 30 0.012 0.30 Standard Wire 1 0.0164 0.416 26 0.018 0.467 29 0.036 0.914 29 0.036 0.914 29 0.036 0.914 29 0.036 0.914 29 0.0136 0.345 29 0.0136 0.345 29 0.0136 0.345 29 0.0136 0.345 29 0.018 0.467 29 0.028 0.711 21 0.032 0.812 20 0.036 0.914 19 0.040 1.016 18 0.048 1.219 17 0.056 1.422 16 0.064 1.625 15 0.072 1.828 14 0.080 2.032 13 0.092 2.336 14 0.080 2.032 13 0.092 2.336 14 0.080 2.032 13 0.092 2.336 14 0.080 2.032 13 0.092 2.336 14 0.080 2.032 13 0.092 2.336 15 0.160 4.064 7 0.176 4.470 6 0.192 4.876 6 0.192 5.884 | 4 | | |
| 7 | 5 | | |
| 8 0.160 4.06 9 0.144 3.66 10 0.128 3.25 11 0.116 2.94 12 0.104 2.64 13 0.092 2.34 14 0.080 2.00 15 0.072 1.83 16 0.064 1.62 17 0.056 1.42 18 0.048 1.22 19 0.040 1.01 20 0.036 0.91 21 0.032 0.81 22 0.028 0.71 23 0.024 0.61 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 0.013 0.33 30 0.0124 0.314 29 0.0136 0.345 28 0.014 0.36 29 0.0136 0.345 | 7 | | |
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| 22 0.028 0.71 23 0.024 0.61 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial Metric Thickness inches mm 30 0.0124 0.314 29 0.0136 0.345 28 0.0148 0.375 27 0.0164 0.416 26 0.018 0.457 25 0.020 0.508 24 0.022 0.558 23 0.024 0.609 22 0.028 0.711 21 0.032 0.812 20 0.036 0.914 19 0.040 1.016 18 0.048 1.219 17 0.056 1.422 16 0.064 1.625 | | | |
| 23 | | | |
| 24 0.022 0.56 25 0.020 0.51 26 0.018 0.46 27 0.016 0.41 28 0.014 0.36 29 0.013 0.33 30 0.012 0.30 Standard Wire Gauge Imperial Metric Thickness inches mm 30 0.0124 0.314 29 0.0136 0.345 28 0.0148 0.375 27 0.0164 0.416 26 0.018 0.457 25 0.020 0.508 24 0.022 0.558 23 0.024 0.609 22 0.028 0.711 21 0.032 0.812 20 0.036 0.914 19 0.040 1.016 18 0.048 1.219 17 0.056 1.422 16 0.064 1.625 15 0.072 1.828 14 0.080 2.032 | | | |
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| inches mm 30 | | - | |
| 29 0.0136 0.345 28 0.0148 0.375 27 0.0164 0.416 26 0.018 0.457 25 0.020 0.508 24 0.022 0.558 23 0.024 0.609 22 0.028 0.711 21 0.032 0.812 20 0.036 0.914 19 0.040 1.016 18 0.048 1.219 17 0.056 1.422 16 0.064 1.625 15 0.072 1.828 14 0.080 2.032 13 0.092 2.336 12 0.104 2.640 11 0.116 2.946 10 0.128 3.251 9 0.144 3.657 8 0.160 4.064 7 0.176 4.470 6 0.192 5.384 4 0.232 5.892 | | inches | |
| 28 0.0148 0.375 27 0.0164 0.416 26 0.018 0.457 25 0.020 0.508 24 0.022 0.558 23 0.024 0.609 22 0.028 0.711 21 0.032 0.812 20 0.036 0.914 19 0.040 1.016 18 0.048 1.219 17 0.056 1.422 16 0.064 1.625 15 0.072 1.828 14 0.080 2.032 13 0.092 2.336 12 0.104 2.640 11 0.116 2.946 10 0.128 3.251 9 0.144 3.657 8 0.160 4.064 7 0.176 4.470 6 0.192 5.384 4 0.232 5.892 | | | |
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| 10 0.128 3.251 9 0.144 3.657 8 0.160 4.064 7 0.176 4.470 6 0.192 4.876 5 0.212 5.384 4 0.232 5.892 | 26 25 24 23 22 21 20 19 18 17 16 15 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 |
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| | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 |
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| | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 |
| | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 0.324 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 8.229 |
| 4/0 0.400 10.16 | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0 2/0 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 0.324 0.348 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 8.229 8.839 |
| 5/0 0.432 10.97 | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0 2/0 3/0 3/0 3/0 3/0 3/0 3/0 3/0 3/0 3/0 3 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 0.324 0.348 0.372 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 8.229 8.839 9.448 |
| 6/0 0.464 11.8 | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0 2/0 3/0 4/0 5/0 5/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 0.324 0.348 0.372 0.400 0.432 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 8.229 8.839 9.448 10.16 10.97 |
| 7/0 0.500 12.70 | 26 25 24 23 22 21 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0 2/0 3/0 4/0 5/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6/0 6 | 0.018 0.020 0.022 0.024 0.028 0.032 0.036 0.040 0.048 0.056 0.064 0.072 0.080 0.092 0.104 0.116 0.128 0.144 0.160 0.176 0.192 0.212 0.232 0.252 0.276 0.300 0.324 0.348 0.372 0.400 0.432 0.464 | 0.457 0.508 0.558 0.609 0.711 0.812 0.914 1.016 1.219 1.422 1.625 1.828 2.032 2.336 2.640 2.946 3.251 3.657 4.064 4.470 4.876 5.384 5.892 6.400 7.010 7.620 8.229 8.839 9.448 10.16 10.97 11.8 |

| Pipe & Hoses General Types Clear PVC, non toxic pipe | Bore Sizes 13mm-38mm (½"-1½") | Outside dia. 19mm-48mm (34"-178") | Comments & Usage Water supply and occasionally delivery. Kinks and collapses, so must not be used on suction runs. Also cannot be used where fluids are hot, nor should fuels be piped in this hose. Can be 'persuaded' to distort. |
|---|-------------------------------------|---|---|
| Spiral reinforced plastic pipe | (3/4"-11/2") | | Three general types. Very and medium stiff, with moulded in spiralling, and flexible, thin wall with external spiralling. Does not kink but conversely can be difficult to get round tight bends. Used for both suction and delivery pipe runs. Heat must be used to ensure pipe clips have properly tightened down. Will not easily distort. |
| Low pressure rubber pipe | 13mm, 19 & 25mm (½"; ¾", & 1") | | Calor gas piping from a bibcock to, say, a gimballed cooker. |
| Seamless copper tube | 1/8"-3/4" | | Calor gas and fuel pipe runs. |
| Reinforced, clear fuel pipe | 1/4", 5", 3/8" & 1/2" | | Suitable for petrol or diesel fuels. |
| Synthetic delivery pipe | 13mm-25mm — (½"-1") | | Hot water supply. |
| Reinforced rubber heater hose | 13mm-25mm (½"-1") | | Engine water cooling inlet pipe. |

Water pipe equivalents:-3/8" 12mm) 34" 22mm)not inter-1/2" 15mm) inter-11/4" 35mm)changeable &

Note Gas & fuel pipe sizes are still measured in Imperial

1" 28mm) changeable 11/2" 42mm) require a 54mm)

sizes.

conversion coupling

| | , • | |
|------------------------------------|---------------|------------|
| | 3/4″ | 19mm |
| | 7⁄8″ | 22mm |
| | 1" | 25mm |
| | 11/4" | 32mm |
| | 11/2" | 38mm |
| | 13⁄4″ | 44mm |
| | 2" | 50mm |
| | 21/2" | 63mm |
| | 3" | 75mm |
| | 4" | 100mm |
| | 5" | 125mm |
| | 6" | 150mm |
| Note. The above sizes are for sawr | n timber. Pla | ned timber |
| looses about 1½mm (1/18") per | planed sur | face, so a |

board ordered '25mm (1") planed thickness' finishes up

* To ascertain a screw's gauge, measure the diameter of the head of the screw, using a ruler marked in sixteenths (of an inch), multiply the measurement by two

Screw gauges* 8

pilot drill - $\frac{1}{16}$ " $\frac{5}{64}$ " $\frac{5}{64}$ " clearance drill - $\frac{3}{32}$ " $\frac{3}{32}$ " $\frac{5}{32}$ " $\frac{5}{32}$ " pilot drill $\frac{5}{64}$ " $\frac{3}{32}$ " $\frac{1}{8}$ " $\frac{1}{8}$ " clearance drill $\frac{5}{32}$ " $\frac{3}{16}$ " $\frac{7}{32}$ " $\frac{1}{4}$ "

10

1/2"

5/8"

Plywood board equivalents:-

Skin fitting equivalents 1/2"

3/4"

1"

11/4"

11/2"

at about 22mm (%")

Hardwoods, pilot drill

Softwoods.

Woodscrew drilling sizes:-

and subtract two from the result.

2"

13mm

19mm

25mm

38mm

50mm

Timber thickness:- (approx.)

32mm

1/8"

1/4"

3/8"

4mm

6mm

9_{mm} ½" 12mm 3/4" 18mm

13mm

16mm

VII. Weights and Measures: Conversion Ratios

WEIGHTS AND MEASURES*

Tables of United States Customary Weights and Measures

Linear Measure

```
12 inches (in.) = 1 foot (ft.)

3 feet = 1 yard (yd.)

5^{1}/_{2} yards = 1 rod (rd.), pole, or perch (16^{1}/_{2}) ft.)

40 rods = 1 furlong (fur.) = 220 yards = 660 feet

8 furlongs = 1 statute mile (mi.) = 1760 yards = 5280 feet

3 miles = 1 league = 5280 yards = 15,840 feet

5280 feet = 1 statute or land mile
```

6076.11549 feet = 1 international nautical mile

Area Measure

Squares and cubes of units are sometimes abbreviated by using "superior" figures. For example, ft² means square foot, and ft³ means cubic foot.

```
144 square inches = 1 square foot (sq. ft.)
9 square feet = 1 square yard (sq. yd.) = 1296 square inches
30½ square yards = 1 square rod (sq. rd.) = 272½ square feet
160 square rods = 1 acre = 4840 square yards = 43,560 square
feet
640 acres = 1 square mile (sq. mi.)
1 mile square = 1 section (of land)
6 miles square = 1 township = 36 sections = 36 square miles
```

Cubic Measure

```
1728 cubic inches (cu. in.) = 1 cubic foot (cu. ft.)
27 cubic feet = 1 cubic yard (cu. yd.)
```

Gunter's or Surveyor's Chain Measure

```
7.92 inches (in.) = 1 link (li.)

100 links = 1 chain (ch.) = 4 rods = 66 feet

80 chains = 1 statute mile (mi.) = 320 rods = 5280 feet
```

Liquid Measure

When necessary to distinguish the liquid pint or quart from the dry pint or quart, the word "liquid" or the abbreviation "liq" should be used in combination with the name or abbreviation of the liquid unit.

```
4 gills (gi.) = 1 pint (pt.) (= 28.875 cubic inches)

2 pints = 1 quart (qt.) (= 57.75 cubic inches)

4 quarts = 1 gallon (gal.) (= 231 cubic inches)

= 8 pints = 32 gills
```

^{*} Source: National Bureau of Standards, U.S. Department of Commerce.

Anothecaries' Fluid Measure

```
60 minims (min.) = 1 fluid dram (fl. dr.) (= 0.2256 cubic inch)
                  = 1 fluid ounce (fl. oz.) (= 1.8047 cubic inches)
8 fluid drams
                  = 1 pint (pt.) (=28.875 cubic inches)
16 fluid ounces
                       = 128 fluid drams
                  = 1 quart (qt.) (= 57.75 cubic inches)
2 pints
                       = 32 fluid ounces = 256 fluid drams
                 = 1 gallon (gal.) (= 231 cubic inches) = 128 fluid
4 quarts
                      ounces = 1024 fluid drams
```

Dry Measure

When necessary to distinguish the dry pint or quart from the liquid pint or quart, the word "dry" should be used in combination with the name or abbreviation of the dry unit.

```
2 pints (pt.) = 1 quart (qt.) (= 67.2006 cubic inches)
            = 1 peck (pk.) (= 537.605 cubic inches) = 16 pints
4 pecks
            = 1 bushel (bu.) (= 2150.42 cubic inches) = 32 quarts
```

Avoirdupois Weight

When necessary to distinguish the avoirdupois dram from the apothecaries' dram, or to distinguish the avoirdupois dram or ounce from the fluid dram or ounce, or to distinguish the avoirdupois ounce or pound from the troy or apothecaries' ounce or pound, the word "avoirdupois" or the abbreviation "avdp" should be used in combination with the name or abbreviation of the avoirdupois unit.

(The "grain" is the same in avoirdupois, troy, and apothecaries'

```
weight.)
  2711/32 grains
                     = 1 dram (dr.)
                     = 1 ounce (oz.) = 437^{1}/_{2} grains
  16 drams
  16 ounces
                     = 1 pound (lb.) = 256 drams = 7000 grains
                     = 1 hundredweight (cwt.) †
  100 pounds
  20 hundredweights = 1 ton (tn.) = 2000 pounds†
  In "gross" or "long" measure, the following values are recognized:
     112 pounds
                       = 1 gross or long hundredweight†
     20 gross or long
```

†When the terms "hundredweight" and "ton" are used unmodified, they are commonly understood to mean the 100-pound hundredweight and the 2,000-pound ton, respectively; these units may be designated "net" or "short" when necessary to distinguish them from the corresponding units in gross or long measure.

hundredweights = 1 gross or long ton = 2240 pounds†

Trov Weight

```
= 1 pennyweight (dwt.)
24 grains
20 pennyweights = 1 ounce troy (oz. t.) = 480 grains
                = 1 pound troy (lb. t.) = 240 pennyweights
12 ounces trov
                     = 5760 grains
```

Apothecaries' Weight

= scruple (s. ap.) 20 grains

= 1 dram apothecaries' (dr. ap.) = 60 grains 3 scruples

= 1 ounce apothecaries' (oz. ap.) = 24 8 drams apothecaries'

scruples = 480 grains

12 ounces apothecaries' = 1 pound apothecaries' (lb. ap.) = 96 drams apothecaries' = 288 scruples

= 5760 grains

Tables of Metric Weights and Measures

Linear Measure

10 millimeters (mm.) = 1 centimeter (cm.)

= 1 decimeter (dm.) = 100 millimeters 10 centimeters

= 1 meter (m.) = 1000 millimeters10 decimeters

= 1 dekameter (dkm.) 10 meters

= 1 hectometer (hm.) = 100 meters 10 dekameters

= 1 kilometer (km.) = 1000 meters 10 hectometers

Area Measure

100 square millimeters (mm²) = 1 square centimeter (cm²)

 $= 1 \text{ square meter } (m^2) = 1,000,000$ 10,000 square centimeters

square millimeters

100 square meters = 1 are (a.)

= 1 hectare (ha.) = 10,000 square 100 ares

meters

= 1 square kilometer (km²) 100 hectares = 1.000,000 square meters

Volume Measure

10 milliliters (ml.) = 1 centiliter (cl.)

= 1 deciliter (dl.) = 100 milliliters 10 centiliters

= 1 liter (l.) = 1000 milliliters 10 deciliters

= 1 dekaliter (dkl.) 10 liters

= 1 hectoliter (hl.) = 100 liters 10 dekaliters

10 hectoliters = 1 kiloliter (kl.) = 1000 liters

The liter is defined as the volume occupied, under standard conditions, by a quantity of pure water having a mass of 1 kilogram. This volume is very nearly equal to 1000 cubic centimeters or 1 cubic decimeter; the actual metric equivalent is, 1 liter = 1,000028 cubic decimeters. Thus the milliliter and the liter are larger than the cubic centimeter and the cubic decimeter, respectively, by 28 parts in 1,000,000.

Cubic Measure

1000 cubic millimeters (mm³) = 1 cubic centimeter (cm³) = 1 cubic decimeter (dm³)

1000 cubic centimeters

= 1.000.000 cubic millimeters = 1 cubic meter (m^3) = 1 stere 1000 cubic decimeters

= 1,000,000 cubic centimeters

= 1.000.000.000 cubic millimeters

Weight

10 milligrams (mg.) = 1 centigram (cg.)
10 centigrams = 1 decigram (dg.) = 100 milligrams
10 decigrams = 1 gram (g.) = 1000 milligrams
10 grams = 1 dekagram (dkg.)
10 dekagrams = 1 hectogram (hg.) = 1000 grams
10 hectograms = 1 kilogram (kg.) = 1000 grams
1000 kilograms = 1 metric ton (t.)

Tables of Equivalents

When the name of a unit is enclosed in brackets thus: [1 hand], this indicates (1) that the unit is not in general current use in the United States, or (2) that the unit is believed to be based on "custom and usage" rather than on formal definition.

Equivalents involving decimals are, in most instances, rounded off to the third decimal place except where they are exact, in which

cases these exact equivalents are so designated.

Lengths

```
0.1 millimicron (exactly)
                      0.0001 micron (exactly)
1 Angstrom (A.)
                       0.0000001 millimeter (exactly)
                      0.000000004 inch
                      120 fathoms
                       720 feet
1 cable's length
                      219.456 meters (exactly)
                       0.3937 inch
1 centimeter (cm.)
                                            66 feet
1 chain (ch.) (Gunter's or surveyor's)
                                            20.1168 meters (exactly)
                         100 feet
1 chain (engineer's)
                        30.48 meters (exactly)
                       3.937 inches
I decimeter (dm.)
                         32,808 feet
1 dekameter (dkm.)
               6 feet
1 fathom
               1.8288 meters (exactly)
               0.3048 meters (exactly)
1 foot (ft.)
                      10 chains (surveyor's)
                      660 feet
1 furlong (fur.)
                      220 yards
                      1/e statute mile
                      201.168 meters
             4 inches
[l hand]
                2.54 centimeters (exactly)
1 inch (in.)
                      0.621 mile
1 kilometer (km.)
                     13 statute miles
1 league (land)
                     1 4.828 kilometers
                                          7.92 inches
1 link (li.) (Gunter's or surveyor's)
                                          0.201 meter
                            1 foot
1 link (li.) (engineer's)
                             0.305 meter
```

```
39.37 inches
1 meter (m.)
                  1.094 vards
                                           0.001 millimeter (exactly)
1 micron (µ [the Greek letter mu])
                                          1 0.00003937 inch
           (0.001 \text{ inch (exactly)})
1 mil
          0.0254 millimeter (exactly)
                                     5280 feet
1 mile (mi.) (statute or land)
                                    1.609 kilometers
                                       1.852 kilometers (exactly)
1 mile (mi.) (nautical, interna-
                                       1.150779 statute miles
  tional, and new U.S. value)
                                       6076.11549 feet
1 millimeter (mm.)
                        0.03937 inch
1 millimicron (mu [the English
                                       0.001 micron (exactly)
  letter m in combination with
                                       0.00000003937 inch (exactly)
  the Greek letter mul)
                            0.013837 inch (exactly)
1 point (typography)
                           0.351 millimeter
                                 161/2 feet
                                  5^{1}/_{2} yards
1 rod (rd.), pole, or perch
                                 5.029 meters
l yard (yd.)
                 0.9144 meter (exactly)
                         Areas or Surfaces
             43,560 square feet
             4840 square yards
l acre
             0.405 hectare
                119.599 square vards
1 are (a.)
                0.025 acre
                    2.471 acres
1 hectare (ha.)
                          100 square feet
[1 square (building)]
1 square centimeter (cm<sup>2</sup>)
                                0.155 square inch
1 square decimeter (dm<sup>2</sup>)
                               15.500 square inches
                           929.030 square centimeters
1 square foot (sq. ft.)
                           6.452 square centimeters
1 square inch (sq. in.)
                                 247.105 acres
1 square kilometer (km²)
                                0.386 square mile
                            1.196 square yards
1 square meter (m²)
                           10.764 square feet
                            258.999 hectares
1 square mile (sq. mi.)
1 square millimeter (mm<sup>2</sup>)
                                0.002 square inch
                                                 25.293 square meters
1 square rod (sq. rd.), sq. pole, or sq. perch
1 square yard (sq. yd.)
                            0.836 square meter
                      Capacities or Volumes
                           31 to 42 gallons*
1 barrel (bbl.), liquid
1 barrel (bbl.), standard, for
                                        7056 cubic inches
  fruits, vegetables, and other
                                        105 dry quarts
  dry commodities except
```

cranberries

3.281 bushels, struck measure

[•] There are a variety of "barrels," established by law or usage. For example, federal taxes on fermented liquors are based on a barrel of 31 gallons; many state laws fix the "barrel for liquids" at 311/2, gallons; one state fixes a 36-gallon barrel for cistern measurement; federal law recognizes a 40-gallon barrel for "proof spirits"; by custom, 42 gallons comprise a barrel of crude oil or petroleum products for statistical purposes, and this equivalent is recognized "for liquids" by four states.

```
5826 cubic inches
 1 barrel (bbl.), standard.
                                  8645/64 dry quarts
   cranberry
                                 2.709 bushels, struck measure
                             2150.42 cubic inches (exactly)
 1 bushel (bu.) (U.S.)
   (struck measure)
                            35.238 liters
                                  2747.715 cubic inches
[1 bushel, heaped (U.S.)]
                                1.278 bushels, struck measuret
  † Frequently recognized as 11/4 bushels, struck measure.
[1 bushel (bu.) (British
                                  1.032 U.S. bushels, struck measure
   Imperial) (struck measure)]
                                  1 2219.36 cubic inches
 l cord (cd.) (firewood)
                             128 cubic feet
1 cubic centimeter (cm<sup>3</sup>)
                               0.061 cubic inch
1 cubic decimeter (dm³)
                               61.023 cubic inches
                             7.481 gallons
1 cubic foot (cu. ft.)
                            28.317 cubic decimeters
                            0.554 fluid ounce
l cubic inch (cu. in.)
                             4.433 fluid drams
                            16.387 cubic centimeters
l cubic meter (m³)
                         1.308 cubic yards
1 cubic yard (cu. yd.)
                            0.765 cubic meter
l cup, measuring
                          8 fluid ounces
                          1/2 liquid pint
                         2.642 gallons
l dekaliter (dkl.)
                         1.135 pecks
                                                1/a fluid ounce
1 dram, fluid (or liquid) (fl. dr.) (U.S.)
                                                0.226 cubic inch
                                               3.697 milliliters
                                         0.961 U.S. fluid dram
[1 dram, fluid (fl. dr.) (British)]
                                         0.217 cubic inch
                                        3.552 milliliters
                             231 cubic inches
                             3.785 liters
l gallon (gal.) (U.S.)
                             0.833 British gallon
                             128 U.S. fluid ounces
                                           277.42 cubic inches
                                           1.201 U.S. gallons
[1 gallon (gal.) (British Imperial)]
                                           4.546 liters
                                           160 British fluid ounces
                  7.219 cubic inches
1 gill (gi.)
                 4 fluid ounces
                 0.118 liter
                       ( 26.418 gallons
1 hectoliter (hl.)
                      2.838 bushels
             1.057 liquid quarts
1 liter
             0.908 dry quart
             61.025 cubic inches
                        0.271 fluid dram
1 milliliter (ml.)
                        0.061 cubic inch
                                                1.805 cubic inches
                                                29.573 milliliters
1 ounce, fluid (or liquid) (fl. oz.) (U.S.)
                                                1.041 British fluid
```

```
0.961 U.S. fluid ounce
1.734 cubic inches
28.412 milliliters
[1 ounce, fluid (fl. oz.) (British)]
1 peck (pk.)
                             8.810 liters
                                     33.600 cubic inches
1 pint (pt.), dry
                                           28.875 cubic inches (exactly)
1 pint (pt.), liquid
                                                      67.201 cubic inches
1 quart (qt.), dry (U.S.)
                                                      1.101 liters
0.969 British quart
                                                         57.75 cubic inches (exactly)
0.946 liter
0.833 British quart
1 quart (qt.), liquid (U.S.)
                                                  69.354 cubic inches
1.032 U.S. dry quarts
1.201 U.S. liquid quarts
[1 quart (qt.) (British)]
                           \begin{cases} 3 \text{ teaspoons} \\ 4 \text{ fluid drams} \\ ^{1}/_{2} \text{ fluid ounce} \\ ^{1}/_{3} \text{ tablespoon} \\ ^{1}/_{3} \text{ fluid drams} \end{cases} 
l tablespoon
l teaspoon
```

 $[\]ddagger$ The equivalent "1 teaspoon = $1^1/_8$ fluid drams" has been found by the Bureau to correspond more closely with the actual capacities of "measuring" and silver teaspoons than the equivalent "1 teaspoon = 1 fluid dram" which is given by a number of dictionaries.

Weights or Masses

1 assay ton* (AT) 29.167 grams

200 milligrams

* Used in assaying. The assay ton bears the same relation to the milligram that a ton of 2000 pounds avoirdupois bears to the ounce troy; hence the weight in milligrams of precious metal obtained from one assay ton of ore gives directly the number of troy ounces to the net ton.

```
1 carat (c.)
                 3.086 grains
                                      60 grains
1 dram, apothecaries' (dr. ap.)
                                      3.888 grams
                                       27^{11}/_{39} (= 27.344) grains
1 dram. avoirdupois (dr. avdp.)
                                      1.772 grams
 gamma, see microgram
           64.799 milligrams
                 ( 15.432 grains
                 0.035 ounce, avoirdupois
                                                    112 pounds
1 hundredweight, gross or long† (gross cwt.)
                                                    50.802 kilograms
 † The gross or long ton and hundredweight are used commercially in the United
States to only a limited extent, usually in restricted industrial fields. These units are
the same as the British "ton" and "hundredweight."
1 hundredweight, net or short
                                      100 pounds
                                     45.359 kilograms
  (cwt. or net cwt.)
                     2.205 pounds
l kilogram (kg.)
1 microgram (y [the Greek letter gamma])
                                              0.000001 gram (exactly)
1 milligram (mg.)
                       0.015 grain
                                         437.5 grains (exactly)
                                         0.911 troy or apothecaries'
I ounce, avoirdupois (oz. avdp.)
                                           ounce
                                        28.350 grams
                                      480 grains
1 ounce, troy or apothecaries'
                                      1.097 avoirdupois ounces
  (oz. t. or oz. ap.)
                                      31.103 grams
                           1.555 grams
1 pennyweight (dwt.)
                             7000 grains
1 pound, avoirdupois
                             1.215 troy or apothecaries' pounds
  (lb. avdp.)
                             453.59237 grams (exactly)
                                      5760 grains
1 pound, troy or apothecaries'
                                       0.823 avoirdupois pound
  (lb. t. or lb. ap.)
                                      373.242 grams
                        20 grains
1 scruple (s. ap.)
                        1.296 grams
                                        2240 pounds
                                        1.12 net tons (exactly)
1 ton, gross or long (gross tn.)
                                         .016 metric tons
                         2204.623 pounds
                         0.984 gross ton
l ton, metric (t.)
                          .102 net tons
                                          2000 pounds
                                          0.893 gross ton
1 ton, net or short (tn. or net tn.)
```

0.907 metric ton

Tables of Interrelation of Units of Measurement Bold face type indicates exact values

Units of Length

4.970 970

= 39.37

1 meter

| Units | | Inches | Links | Feet | Yards | Rods | Chains | Miles | Cm. | Meters |
|------------------|---|------------------|-----------------------|--------------------------|--------------------------|---------------------------------------|---------------------------------------|--|-------------------------|---------------------------------|
| l inch l link | | 7.92 | 0.126 333 | 0.083 333 0.66 | 0.027 778 0.22 | 0.005 051 0.04 0.060 606 | 0.001 263 0.01 0.015 152 | 0.000 016 0.000 125 0.000 189 | 2.54 20.117 30.48 | 0.025 4 0.201 168 0.304 8 |
| l foot l yard | = | 12 36 | 1.515 152 4.545 45 | 3 | 0.333 333 | 0.060 606 0.181 818 | 0.045 455 | 0.000 568 | 91.44 | 0.914 4 5.029 2 |
| l rod l chain | = | 198 792 | 25 100 | 66 | 5.5 | 4 | 0.25 | 0.003 125 0.012 5 | 502.92 2011.68 | 20.116 8 |
| 1 mile 1 cm. | = | 63 360 0.3937 | 8000 0.049 710 | 5280 0.032 808 | 0.010 936 | 0.001 988 | 0.000 497 | 0.000 006 | 160 934.4 | 1609.344 0.01 |

3.280 840 | 1.093 613 | 0.198 839 | 0.049 710 | 0.000 621

100

Units of Area

| Units | Square inches | Square links | Squai feet | | Square yards | Square rods | Square chains |
|--|--|---|---|--|---|---|--|
| 1 sq. inch = 1 sq. link = 1 sq. foot = 1 sq. yard = 1 sq. rod = 1 sq. chain = 1 acre = 1 sq. mile = 1 sq. cm. = 1 sq. meter = 1 hectare = 1 | 1 62.726 4 144 . 1296 39 204 627 264 6 272 640 4 014 489 600 0.155 000 3 1550.003 15 500 031 | .015 942 3 1 2.295 684 20.661 16 625 10 000 100 000 64 000 000 0.002 471 05 24.710 54 247 105 | | 1 9 4356 560 400 076 91 | 0.000 771 60 0.0484 0.111 111 1 30.25 484 3 097 60 0.000 119 58 1.195 990 11 959.90 | 0.0016 0.003 673 09 0.033 057 85 1 160 160 102 400 109 0.000 003 954 0.039 536 86 | 10 6400 |
| Units | Acres | Square miles | • | C | Square entimeters | Square meters | Hectares |
| l sq. inch = 1 sq. link = 1 sq. link = 1 sq. foot = 1 sq. yard = 1 sq. chain = 1 acre = 1 sq. mile = 1 sq. cm. = 1 sq. meter = 1 hectare = 1 | 0.000 01 0.000 022 956 84 0.000 206 611 6 0.006 25 0.1 1 640 0.000 000 024 711 0.000 247 105 4 | 0.000 000 000 0.000 000 015 0.000 000 035 0.000 000 322 0.000 009 765 0.000 156 25 0.001 562 5 0.000 000 000 0.000 000 386 0.003 861 022 | 625 870 06 830 6 625 1 038 610 | 8 252 | 6.451 6 .685 642 24 929.030 4 361.273 6 928.526 4 4 046 856 40 468 654 899 881 103 1 10 000 100 000 000 | 0.000 645 16 0.040 468 56 0.092 903 04 0.836 127 36 25,292 852 64 404.685 642 24 4046.856 422 4 2 589 988.11 0.0001 | 0.000 000 065 0.000 004 047 0.000 009 290 0.000 083 613 0.002 529 285 0.040 468 564 0.404 685 642 258.998 811 034 0.000 000 01 0.0001 |

Units of Volume

| Units | | Cubic inches | Cubic feet | Cubic yards | Cubic centimeters | Cubic decimeters | Cubic meters |
|---|---------|---|--|---|---|--|---|
| l cubic inch l cubic foot l cubic yard l cubic cm. l cubic dm. l cubic meter | = = = = | 1 1728 46 656 0.061 023 74 61.023 74 61 023.74 | 0.000 578 704 1 27 0.000 035 315 0.035 314 67 35.314 67 | 0.000 021 433 0.037 037 04 1 0.000 001 308 0.001 307 951 1.307 951 | 16.387 064 28 316.846 592 764 554.857 984 1 1000 1 000 000 | 0.016 387 28.316 847 764.554 858 0.001 1 | 0.000 016 387 0.028 316 847 0.764 554 858 0.000 001 0.001 |

Units of Capacity (Liquid Measure)

| Units | | Minims | Fluid drams | Fluid ounces | Gills | Liquid pints |
|--|---|---|--|--|--|---|
| I minim I fluid dram I fluid ounce I gill I liquid pint I liquid quart I gallon I milliliter I titer I cubic inch I cubic foot | = | 1 60 480 1920 7680 15 360 61 440 16.231 16 231.19 265.974 459 603.1 | 0.016 666 7 1 8 32 128 256 1024 0.270 519 8 270.519 8 4.432 900 7660.052 | 0.002 083 33 0.125 1 4 16 32 128 0.033 814 97 0.554 112 6 957.506 5 | 0.000 520 833 0.031 25 0.25 1 4 8 32 0.008 453 742 8.453 742 0.138 528 1 239.376 6 | 0.000 130 208 0.007 812 5 0.062 5 0.25 1 2 8 0.002 113 436 2.113 436 0.034 632 03 59.844 16 |

Units of Capacity (Liquid Measure) Continued. Bold face type indicates exact values

| Units | Liquid quarts | Gallons | Milliliters | Liters | Cubic inches | Cubic feet |
|-------|--|---|---|--|---|---|
| minim | 0.000 065 104 0.003 906 25 0.031 25 0.125 0.5 1 4 0.001 056 718 1.056 718 0.017 316 02 29.922 08 | 0.000 016 276 0.000 976 562 0.007 812 5 0.031 25 0.125 0.25 1 0.000 264 179 0.264 179 4 0.004 329 004 7.480 519 | 0.061 610 3.696 588 29.572 70 118.290 8 473.163 2 946.326 4 3785.306 1 1000 16.386 61 28 316.05 | 0.000 061 610 0.003 696 588 0.029 572 7 0.118 290 8 0.473 163 2 0.946 326 4 3.785 306 0.001 1 0.016 386 61 28.316 05 | 0.003 760 0.225 586 1.804 687 7.218 75 28.875 57.75 231 0.061 025 61.025 45 | 0.000 002 176 0.000 130 547 0.001 044 379 0.004 177 517 0.016 710 07 0.033 420 14 0.133 680 6 0.000 035 316 0.035 315 66 0.000 578 704 |

Units of Capacity (Dry Measure)

| Units | Dry pints | Dry quarts | Pecks | Bushels | Liters | Dekaliters | Cubic inches |
|---|---|--|---|---|--|--|--|
| 1 dry pint = 1 dry quart = 1 peck = 1 bushel = 1 liter = 1 dekaliter = 1 cubic inch = | 1 2 16 64 1.816 217 18.162 17 0.029 762 | 0.5 1 8 32 0.908 108 9.081 084 0.014 881 | 0.062 5 0.125 1 4 0.113 514 1.135 136 0.001 860 | 0.015 625 0.031 25 0.25 1 0.028 378 0.283 784 0.000 465 | 0.550 595 1.101 190 8.809 521 35.238 08 1 10 0.016 386 | 0.055 060 0.110 119 0.880 952 3.523 808 0.1 1 0.001 639 | 33.600 312 5 67.200 625 537.605 2150.42 61.025 45 610.254 5 |

Units of Mass not Greater than Pounds and Kilograms

| Units | | Grains | Apothecaries' scruples | Pennyweights | Avoirdupois drams | Apothecaries' drams | Avoirdupois ounces |
|---------------|-----|------------------------------------|------------------------------------|-----------------------|----------------------|------------------------|--------------------|
| grain | _ | 1 | 0.05 | 0.041 666 67 | 0.036 571 43 | 0.016 666 67 | 0.002 285 71 |
| scruple | _ [| 20 | 1 | 0.833 333 3 | 0.731 428 6 | 0.333 333 3 | 0.045 714 29 |
| | _ | 24 | 1.2 | 1 | 0.877 714 3 | 0.4 | 0.054 857 14 |
| dram avdp. | = | 27.343 75 | 1.367 187 5 | 1.139 323 | 1 | 0.455 729 2 | 0.062 5 |
| dram ap. | _ | 60 | 3 | 2.5 | 2.194 286 | 1 | 0.137 142 9 |
| oz. avdp. | _ | 437.5 | 21.875 | 18.229 17 | 16 | 7.291 667 | 1 |
| oz. avup. | _ | 480 | 24 | 20 | 17.554 29 | 8 | 1.097 143 |
| lb. ap. or t. | _ | 5760 | 288 | 240 | 210.651 4 | 96 | 13.165 71 |
| lb. avdp. | = | 7000 | 350 | 291.666 7 | 256 | 116.6667 | 16.100 11 |
| milligram | = | 0.015 432 | 0.000 771 618 | 0.000 643 015 | 0.000 564 383 | 0.000 257 206 | 0.000 035 274 |
| | _ | 15.432 36 | 0.771 617 9 | 0.643 014 9 | 0.564 383 4 | 0.257 206 0 | 0.035 273 96 |
| gram | _ | 15 432.36 | 771.617 9 | 643.014 9 | 564.383 4 | 257.206 0 | 35.273 96 |
| kilogram | - | 10 402.00 | 111.011 8 | 040.014 8 | 004.000 4 | 201.2000 | 210 00 |
| Units | | Apothecaries' or troy ounces | Apothecaries' or troy pounds | Avoirdupois pounds | Milligrams | Grams | Kilograms |
| grain | _ | 0.002 083 33 | 0.000 173 611 | 0.000 142 857 | 64,798 91 | 0.064 798 91 | 0.000 064 799 |
| scruple | _ | 0.041 666 67 | 0.003 472 222 | 0.002 857 143 | 1295.978 2 | 1.295 978 2 | 0.001 295 978 |
| pennyweight | = | 0.05 | 0.004 166 667 | 0.003 428 571 | 1555,173 84 | 1.555 173 84 | 0.001 555 174 |
| dram avdp. | _ | 0.056 966 15 | 0.004 747 179 | 0.003 906 25 | 1771.845 195 | 1.771 845 195 | 0.001 771 845 |
| dram ap. | _ | 0.125 | 0.010 416 67 | 0.008 571 429 | 3887.934 6 | 3.887 934 6 | 0.003 887 935 |
| oz. avdp. | _ | 0.911 458 3 | 0.075 954 86 | 0.062 5 | 28 349.523 125 | 28.349 523 125 | 0.028 349 52 |
| oz. ap. or t. | = | 1 | 0.083 333 333 | 0.068 571 43 | 31 103.476 8 | 31.103 476 8 | 0.031 103 47 |
| lb. ap. or t. | = | 12 | | 0.822 857 1 | 373 241.721 6 | 373.241 721 6 | 0.373 241 722 |
| lb. avdp. | _ | 14.583 33 | 1.215 278 | 1 | 453 592.37 | 453,592 37 | 0.453 592 37 |
| milligram | _ | 0.000 032 151 | 0.000 002 679 | 0.000 002 205 | 1 | 0.001 | 0.000 001 |
| gram | _ | 0.032 150 75 | 0.002 679 229 | 0.002 204 623 | 1000 | 1 | 0.001 |
| kilogram | | 32.150 75 | 2.679 229 | 2.204 623 | 1 000 000 | 1000 | 1 |

Units of Mass not Less than Avoirdupois Ounces Avoir-Avoir-Short Units dupois dupois hundred-Short tons Long tons Kilograms Metric tons ounces pounds weights

| 1 oz. avdp. = 1 0.0625 0.000 625 0.000 031 25 0.000 027 902 0.028 349 523 0.000 028 1 lb. avdp. = 16 1 0.01 0.0005 0.000 446 429 0.453 592 37 0.000 453 | | · | - | , | weights | pounds | ounces | | |
|---|---|--------------------------------------|-------------------------------|-----|-----------------|------------------|----------------|---|--|
| 1 short cwt. = 1600 100 1 0.05 0.044 642 86 45.359 237 0.045 359 1 short ton = 32 000 2000 200 1 0.892 857 1 907.184 74 0.907 184 | l lb. avdp. == l short cwt. == l short ton == | 0.453 592 37 0.00 45.359 237 0.04 | 0.000 446 429 0.044 642 86 | 1 (| 0.01 1 20 | 1 100 2000 | 1600 32 000 | = | l lb. avdp. l short cwt. l short ton |

| oz. avdp. | = | .1 | 0.0625 | 0.000 625 | 0.000 031 25 | 0.000 027 902 | 0.028 349 523 | 0.00 |
|------------|----|--------|--------|-----------|--------------|---------------|----------------|------|
| lb. avdp. | == | 16 | 1 | 0.01 | 0.0005 | 0.000 446 429 | 0.453 592 37 | 0.00 |
| short cwt. | = | 1600 | 100 | 1 | 0.05 | 0.044 642 86 | 45.359 237 | 0.04 |
| short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.90 |
| long ton | = | 35 840 | 2240 | 22.4 | 1 12 | | 101(04(000 0 | 0.70 |

| i oz. avdp. | = | 1 | 0.0625 | 0.000 625 | 0.000 031 25 | 0.000 027 902 | 0.028 349 523 | 0.000.09 |
|--------------|-----|--------|--------|-----------|--------------|---------------|------------------|------------|
| l lb. avdp. | === | 16 | 1 | 0.01 | 0.0005 | 0.000 446 429 | 0.453 592 37 | 0.000 45 |
| l short cwt. | = | 1600 | 100 | 1 | 0.05 | 0.044 642 86 | 45.359 237 | 0.045 35 |
| l short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.907 18 |
| l long ton | = | 35 840 | 2240 | 22.4 | 1.12 | 1 | 1016.046 908 8 | 1.016 04 |
| , ~ | | | | | | | TO 00 C DEC 10 C | . I.VIO U4 |

| u. up. | | 1 20 | | . 0.01 | 0.0000 | 1 0.000 440 429 | U.453 592 37 | 1 0.000 453 592 |
|--------------|-----|-----------|-----------|--------------|---------------|-----------------|--|-----------------|
| l short cwt. | = | 1600 | 100 | 1 | 0.05 | 0.044 642 86 | 45.359 237 | 0.045 359 237 |
| l short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.907 184 74 |
| l long ton | - 1 | 35 840 | 2240 | 22.4 | 1.12 | 1 | 1016.046 908 8 | 1.016 046 909 |
| l kilogram | | 35 973 08 | 9 904 692 | 0.000.048.00 | 0.001 100 011 | 0 000 004 00= | 1 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 | 1.010 040 808 |

| I snort cwt. | = | 1600 | 100 | 1 | 0.05 | 0.044 642 86 | 45.359 237 | 0.045 359 237 |
|--------------|----|-----------|-----------|--------------|---------------|---------------|----------------|---------------|
| l short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.907 184 74 |
| l long ton | = | 35 840 | 2240 | 22.4 | 1.12 | 1 | 1016.046 908 8 | 1.016 046 909 |
| l kilogram | == | 35.273 96 | 2.204 623 | 0.022 046 23 | 0.001 102 311 | 0.000 094 207 | 1010.010 700 0 | A AA1 |

| I SHOLL CWL. | _ | 1000 | 100 | 1 | 0.05 | 1 0.044 642 86 | 45.359 237 | 0.045 359 |
|--------------|---|-----------|-----------|--------------|---------------|----------------|----------------|-----------|
| l short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.907 184 |
| l long ton | = | 35 840 | 2240 | 22.4 | 1.12 | 1 | 1016.046 908 8 | 1.016 046 |
| l kilogram | = | 35.273 96 | 2.204 623 | 0.022 046 23 | 0.001 102 311 | 0.000 094 207 | 1010.010 700 0 | 0.001 |
| 1 metric ton | = | 35 273.96 | 2204.623 | | 1.102.311 | 0 984 206 5 | 1000 | 0.001 |

| I SHOLL CWL. | _ | 1000 | 100 | 1 | i U.U. | 1 0.044 642 86 | 45.359 237 | 0.045 359 237 |
|--------------|---|-----------|-----------|--------------|---------------|----------------|----------------|---------------|
| l short ton | = | 32 000 | 2000 | 20 | 1 | 0.892 857 1 | 907.184 74 | 0.907 184 74 |
| l long ton | = | 35 840 | 2240 | 22.4 | 1.12 | | 1016.046 908 8 | 1.016 046 909 |
| l kilogram | - | 35.273 96 | 2.204 623 | 0.022 046 23 | 0.001 102 311 | 0 000 094 207 | 10101010 700 0 | 0.001 |

| I SHOLL CWL. | _ | 1000 | IUU | 1 1 | 0.05 | | 0.044 642 86 | 45.359 237 | 0.045 359 237 |
|--------------|-----|-----------|-----------|--------------|------|-------|---------------|----------------|---------------|
| l short ton | = | 32 000 | 2000 | 20 | | 1 | 0.892 857 1 | 907.184 74 | 0.907 184 74 |
| l long ton | = | 35 840 | 2240 | 22.4 | 1.12 | - | 1 | 1016.046 908 8 | 1.016 046 909 |
| l kilogram | === | 35.273 96 | 2.204 623 | 0.022.046.23 | | 2 211 | 0.000.004.907 | 1010.040 700 0 | 1.010 040 909 |

1.102 311

0.984 206 5

1000

IX. Greek Alphabet; Roman Numerals

GREEK ALPHABET

| A | α | alpha | I | ι | iota | P | ρ | rho |
|-----------|-----------------------|---------|-----|---|---------|--------------|--------|----------------|
| В | β | beta | K | κ | kappa | Σ | σ | sigma |
| Г | γ | gamma | Λ | λ | lambda | T | τ | tau |
| Δ | δ | delta | . M | μ | mu | Υ | υ | upsilon |
| ${f E}$ | E | epsilon | N | ν | nu | Φ | φ | phi |
| ${\bf Z}$ | ζ | zeta | Ξ | ξ | xi | \mathbf{x} | x | chi . |
| H | η | eta | O | o | omicron | . Ψ | ψ | \mathbf{psi} |
| θ | $\boldsymbol{\theta}$ | theta | П | π | pi | Ω | ω | omega |

ROMAN NUMERALS

| I | 1 | XI | 11 | XXX | 30 | CD | 400 |
|--------------|----|------------------------|----|---------------|-----|-------------------------|-------|
| II | 2 | XII | 12 | XL | 40 | D | 500 |
| III | 3 | XIII | 13 | \mathbf{L} | 50 | DC | 600 |
| IV | 4 | XIV | 14 | LX . | 60 | DCC | 700 |
| \mathbf{V} | 5 | XV | 15 | LXX | 70 | DCCC | 800 |
| VI | 6 | XVI | 16 | LXXX | 80 | CM | 900 |
| VII | 7 | XVII | 17 | \mathbf{XC} | 90 | M | 1,000 |
| VIII | 8 | XVIII | 18 | C | 100 | MCM | 1,900 |
| IX | 9 | XIX | 19 | CC | 200 | MM | 2,000 |
| \mathbf{X} | 10 | $\mathbf{X}\mathbf{X}$ | 20 | CCC | 300 | $\overline{\mathbf{v}}$ | 5,000 |

A dash line over a numeral multiplies the value by 1,000: thus, $\overline{X} = 10,000$; $\overline{L} = 50,000$; $\overline{C} = 100,000$; $\overline{D} = 500,000$; $\overline{M} = 1,000,000$; $\overline{CLIX} = 159,000$; $\overline{DLIX} = 559,000$.

Other general rules for Roman numerals are as follows: (1) Repeating a letter repeats its value: XX = 20; CCC = 300. (2) A letter placed after one of greater value adds thereto: VI = 6; DC = 600. (3) A letter placed before one of greater value subtracts therefrom: IV = 4.

TABLE 2-5

Conversion factors between the British FPSR (foot, pound, second, rankine) system and SI

(Système International) units

| | FPSR | Multiply | To obtain SI | Multiply | To obtain FPSR |
|-----------------------|--|------------------------|-----------------------|------------------------|--|
| Quantity | Units | by | Units | by | Units |
| Mass (M) | slug | 1.459 × 10 | kg | 6.852×10^{-2} | slug |
| Length (L) | ft | 3.048×10^{-1} | m | 3.281 | ft |
| Density (ρ) | slug/ft ³ | 5.155×10^{2} | kg/m^3 | 1.940×10^{-3} | slug/ft ³ |
| Temperature (T) | °F + 460 | 5.56×10^{-1} | $^{\circ}$ C + 273 | 1.8 | °F + 460 |
| (· ·) | °R | | ۰K | | °R |
| Velocity (V) | ft/sec | 3.048×10^{-1} | m/sec | 3.281 | ft/sec |
| , 525 525 (*) | mph | 1.609 | kph | 6.214×10^{-1} | mph |
| | knot | 1.853 | kph | 5.396×10^{-1} | knot |
| | | 0.515 | m/sec | 1.942 | |
| Force (F) | lbf | 4.448 | , | 2.248×10^{-1} | lbf |
| 1 0100 (1) | slug ft/sec ² | | kg m/sec ² | | slug ft/sec ² |
| Work | slug ft ² /sec ² | 1.356 | Nm | 7.376×10^{-1} | slug ft ² /sec ² |
| Energy (J) | BTU | | (joule) | 7.0707 | BTU |
| Power (W) | slug ft ² /sec ³ | 1.356 | Nm/sec | 7.376×10^{-1} | slug ft ² /sec ³ |
| | hp (550 ft lbf/sec) | | (Watt) | 1.341×10^{-3} | hp (550 ft lbf/sec) |
| Pressure (p) | slug/ft sec ² | 4.788×10 | N/m^2 | 2.088×10^{-2} | slug/ft sec ² |
| r ressure (p) | lbf/ft ² | 11.700 / 10 | (pascal) | 2.000 / 10 | lbf/ft ² |
| | 101/10 | 4.788×10^{-4} | bar | 2.088×10^{3} | 101/10 |
| Specific | ft lbf/slug | 9.290×10^{-2} | Nm/kg | 1.076×10^{-1} | ft lbf/slug |
| Energy, etc | it ioi/siug | J.270 / 10 | TVIII/ Kg | 1.070 / 10 | it ioi/siug |
| Gas Constant | ft lbf/slug° R | 1.672×10^{-1} | Nm/kg° K | 5.981 | ft lbf/slug ^o R |
| Coef of | slug/ft sec | 4.788×10^{-1} | kg/m sec | 2.088×10^{-2} | slug/ft sec |
| Viscosity (μ) | siug/it sec | 4.700 × 10 | kg/III sec | 2.000 \(\tau \) | siug/it sec |
| Kinematic | ft²/sec | 9.290×10^{-2} | m ² /sec | 1.076×10 | f+2/202 |
| | 11-7 800 | 9.290 \ 10 - | 111-/ SEC | 1.070 \(\times 10 | ft ² /sec |
| Viscosity (ν) Thermal | lbf/sec° R | 8.007 | N/sec° K | 1.249×10^{-1} | 11. f / 0 D |
| | idi/sec K | 6.007 | N/Sec K | 1.249 × 10 1 | lbf/sec° R |
| Conductivity (k) | lbf/ft sec° R | 2.627×10 | N/m ago V | 2 907 > 10-2 | 11.f/f4 an =0.D |
| Heat Transfer | 101/11 Sec K | 2.02/ \ 10 | IN/III Sec K | 3.807×10^{-2} | lbf/ft sec° R |
| Transfer | | | | | |
| Coefficient | 0/000 | 1.0 | II.a. (14) | 1.0 | -1 |
| Frequency | c/sec | 1.0 | Hz (hertz) | 1.0 | c/sec |

TABLE 2-6
Conversion Factors (mixed FPSR, metric and SI)

| Multiply | Ву | To obtain |
|--|------------------------|-------------------------------|
| acres | 0.4047 | ha (= 10^4 m^2) |
| | 43 560 | ft ² |
| | 0.0015625 | mi² |
| standard atmospheres (atm) | 76 | cm Hg |
| - | 29.92 | in Hg |
| | 1.01325 | bar (= 10^5 N/m^2) |
| | 1.033 | kgf/cm ² |
| | 14.70 | lbf/in ² |
| | 2116 | lbf/ft ² |
| | 101 325 | N/m^2 |
| bars (bar) | 0.98692 | atm |
| | 14.5038 | lbf/in ² |
| British Thermal Unit (BTU) | 0.5556 | CHU |
| , | 1055 | J |
| | 0.2520 | kcal (kilocalorie) |
| centimetres (cm) | 0.3937 | in |
| (, | 0.032808 | ft |
| centimetres of mercury at | 0.01316 | atm |
| 0°C (cm Hg) | 0.3937 | in Hg |
| 0 0 (0 1.8) | 0.1934 | lbf/in ² |
| | 27.85 | lbf/ft ² |
| | 135.95 | kgf/m ² |
| centimetres per second (cm/s) | 0.032808 | ft/s |
| continuous per second (em, s) | 1.9685 | ft/min |
| | 0.02237 | mph |
| cubic centimetres (cm ³) | 0.06102 | in ³ |
| cubic continuous (em) | 3.531×10^{-5} | ft ³ |
| | 0.001 | litre |
| | 2.642×10^{-4} | US gal |
| cubic feet (ft ³) | 28317 | cm ³ |
| eable feet (it) | 0.028317 | m ³ |
| | 1728 | in ³ |
| | 0.037037 | yd ³ |
| | 7.481 | US gal |
| | 28.32 | litre |
| cubic feet per minute (ft ³ /min) | 0.472 | litre/s |
| cubic reet per minute (requim) | 0.028317 | m ³ / min |
| cubic inches (in ³) | 16.39 | cm ³ |
| cubic menes (m ²) | 1.639×10^{-5} | m ³ |
| | 5.787×10^{-4} | ft ³ |
| | 0.5541 | fl oz |
| | 0.01639 | litre |
| | 4.329×10^{-3} | |
| | | US gal |
| aulia matura (1) | 0.01732 | US qt |
| cubic metres (m³) | 61024 | in ³ |
| | 1.308 | yd³ |
| | 35.3147 | ft ³ |
| | 264.2 | US gal |

TABLE 2-6 - continued

| Multiply | Ву | To obtain |
|------------------------------------|------------------------|--------------------------------|
| cubic metres per minute | 35.3147 | ft³/ min |
| (m^3/\min) | | _ |
| cubic yards (yd³) | 27 | ft ³ |
| | 0.7646 | m ³ |
| | 202 | US gal |
| degrees (arc) | 0.01745 | radians |
| degrees per second (deg/s) | 0.01745 | radians/s |
| erg | 1.0×10^{-7} | J |
| feet (ft) | 30.48 | cm |
| | 0.3048 | m |
| | 12 | in |
| | 0.33333 | yd |
| | 0.0606061 | rod |
| | 1.894×10^{-4} | stm |
| | 1.646×10^{-4} | nm (international) |
| feet per minute (ft/min) | 0.01136 | mph |
| | 0.01829 | km/h |
| | 0.508 | cm/s |
| | 0.00508 | m/s |
| feet per second (ft/s) | 0.6818 | mph |
| , , | 1.097 | km/h |
| | 30.48 | cm/s |
| | 0.5925 | knot (international) |
| foot-pounds (ft lbf) | 0.138255 | kgf m |
| root pounds (iv ioi) | 3.24×10^{-4} | kcal |
| | 1.356 | Nm (J) |
| foot-pounds per minute (ft lbf/min | | hp |
| foot-pounds per second (ft lbf/s) | 1.818×10^{-3} | hp |
| gallons, Imperial (Imp gal) | 277.4 | in ³ |
| ganons, imperiar (imp gan) | 1.201 | US gal |
| | 4.546 | litre |
| | 153.707 | fl oz |
| gallons, US dry (US gal dry) | 268.8 | in ³ |
| ganons, os dry (os gar dry) | 1.556×10^{-1} | ft ³ |
| | 1.164 | US gal |
| | 4.405 | litre |
| gallons, US liquid (US gal) | 231 | in ³ |
| ganons, OS nquid (OS gai) | 0.1337 | ft ³ |
| | 4.951×10^{-3} | yd ³ |
| | 3785.4 | cm ³ |
| | 3.785×10^{-3} | m ³ |
| | 3.785 | litre |
| | 0.83267 | |
| | 133.227 | Imp gal fl oz |
| 11G 11 (701/00mg) | 9.353 | litre/ha |
| US gallons per acre (gal/acre) | 0.001 | |
| grams (g) | 2.205×10^{-3} | kg lb |
| (-1 | 0.1 | kg/m |
| grams per centimetre (g/cm) | 6.720×10^{-2} | - |
| | 5.600×10^{-3} | lb/ft |
| 1.1 | | lb/in |
| grams per cubic centimetre | 1000 | $\frac{\text{kg}}{\text{m}^3}$ |
| (g/cm^3) | 0.03613 | lb/in ³ |
| | 62.43 | lb/ft ³ |

| Multiply | Ву | To obtain |
|--|--------------------------|----------------------|
| hectares (ha) | 2.471 | acres |
| | 107 639 | ft ² |
| | 10000 | m^2 |
| horsepower (hp) | 33 000 | ft lbf/min |
| | 550 | ft lbf/s |
| | 0.7457 | kW |
| | 76.04 | kgf m/s |
| | 1.014 | metric hp |
| | 745.70 | Nm/s (W) |
| horsepower, metric | 75 | kgf m/s |
| • , | 0.9863 | hp |
| inches (in) | 25.40 | mm |
| | 2.540 | cm |
| | 0.0254 | m |
| | 0.08333 | ft |
| | 0.027777 | yd |
| inches of mercury at 0°C | 0.033421 | atm |
| (in Hg) | 0.4912 | lb/in ² |
| (8) | 70.73 | lb/ft ² |
| | 345.3 | kg/m ² |
| | 2.540 | cm Hg |
| | 25.40 | mm Hg |
| · | 3.386×10^{3} | N/m^2 |
| inch-pounds (in lbf) | 0.011521 | kgf m |
| J (joule) | 0.27778×10^{-6} | kWh |
| 3 (Joule) | 1 | Nm |
| | 1 | Ws |
| kilograms (kg) | 2.204623 | lb |
| Knograms (Kg) | 35.27 | oz avdp |
| | 1000 | g |
| kilogram-calories (kcal) | 3.9683 | BTU |
| (kilocalories) | 3088 | ft lbf |
| (Kirocarories) | 426.9 | kgf m |
| kilogram-metre ² (kg m ²) | 3417 | lb in ² |
| knogram metre (kg m) | 23.729 | lb ft ² |
| | 0.7376 | slug ft ² |
| kilograms per cubic metre | 0.06243 | lb/ft ³ |
| (kg/m³) | 0.001 | g/cm ³ |
| kilograms per hectare (kg/ha) | 0.892 | lb/acre |
| kilograms per square centimetre | 0.9678 | atm |
| (kg/cm ²) | 28.96 | in Hg |
| (kg/cm²) | 14.22 | lbf/in ² |
| | 2048 | lbf/ft ² |
| kilograms per square metre | 2.896×10^{-3} | in Hg |
| (kg/m ²) | 1.422×10^{-3} | lb/in ² |
| (v2\ m_) | 0.2048 | lb/ft ² |
| kilometres (km) | 1×10^{5} | • |
| kilometres (km) | | cm fr |
| | 3280.8 | ft |
| | 0.6214 | stm |
| kilometers nor have (11-) | 0.53996 | nm (international |
| kilometers per hour (kph) | 0.9113 | ft/s |
| | 58.68 | ft/min |

TABLE 2-6 - continued

| Multiply | Ву | To obtain |
|---------------------------------------|-------------------------|-----------------------|
| | 0.53996 | knot (international) |
| | 0.6214 | mph |
| | 0.27778 | m/s |
| | 16.67 | m/min |
| kilowatt | 1.34 | hp |
| knots (knot) (international) | 1 | nm/h |
| Mioto (Miot) (miotimos sum) | 1.688 | ft/s |
| | 1.1508 | mph |
| | 1.852 | km/h |
| | 0.5144 | m/s |
| litres (litre) | 1000 | cm ³ |
| nties (ntie) | 61.02 | in ³ |
| | 0.03531 | ft ³ |
| | 33.814 | fl oz |
| | 0.2642 | US gal |
| | 0.2200 | Imp gal |
| | 1.0568 | US qt |
| lituas man haatara (litra/ha) | 13.69 | fl oz/acre |
| litres per hectare (litre/ha) | 0.107 | US gal/acre |
| liture was seemed (liture to) | 2.12 | ft ³ / min |
| litres per second (litre/s) | 39.37 | |
| metres (m) | | in ft |
| | 3.280840 | |
| | 1.0936 | yd |
| | 0.198839 | rod |
| | 6.214×10^{-4} | stm |
| 4.0. | 5.3996×10^{-4} | nm (international) |
| metre-kilogram (kgf/m) | 7.23301 | ft lbf |
| | 86.798 | in lbf |
| metres per minute (m/min) | 0.06 | km/h |
| metres per second (m/sec) | 3.280840 | ft/s |
| | 196.8504 | ft/min |
| | 2.237 | mph |
| | 3.6 | km/h |
| microns | 3.937×10^{-5} | in |
| miles (stm) | 5280 | ft |
| | 1.6093 | km |
| | 1609.3 | m |
| | 0.8690 | nm (international |
| miles per hour (mph) | 44.704 | cm/s |
| • | 0.4470 | m/s |
| | 1.467 | ft/s |
| | 88 | ft/min |
| | 1.6093 | km/h |
| | 0.8690 | knot (international |
| millibars | 2.953×10^{-2} | in Hg |
| | 0.1 | kN/m^2 |
| millimetres (mm) | 0.03937 | in |
| millimetres of mercury at 0°C (mm Hg) | 0.03937 | in Hg |
| international nautical miles (nm) | 6076 | ft |
| morning madreal miles (mile) | 1.1508 | stm |
| | 1852 | m |
| | 1.852 | km |

| Multiply | Ву | To obtain |
|--|------------------------|----------------------|
| Newton (N) | 0.2248 | lbf |
| ounces, fluid (fl oz) | 8 | dr fl |
| ounces, ridia (ii oz) | 29.57 | cm^3 |
| | 1.805 | in ³ |
| | 0.0296 | litre |
| | 0.0078 | US gal |
| fluid nor core (flor/scre) | | litre/ha |
| ounces, fluid per acre (fl oz/acre) | 453.6 | • |
| pounds (lb): mass | 0.453592 | g log |
| | 3.108×10^{-2} | kg |
| | | slug N |
| pounds force (lbf) | 4.4482 | |
| | 0.45359 | kgf |
| pounds-feet (lbf ft) | 1.356 | Nm |
| pounds-feet² (lb ft²) | 0.421 | kg m ² |
| | 144 | lb in ² |
| | 0.0311 | slug ft ² |
| pounds per acre (lb/acre) | 1.121 | kg/ha |
| pounds per cubic foot (lb/ft ³) | 16.02 | kg/m^3 |
| pounds per cubic inch (lb/in ³) | 1728 | lb/ft³ |
| | 27.68 | g/cm^3 |
| pounds per hour per pound force (lb/h/lbf) | 28.3 | mg/Ns |
| pounds per hour per horsepower (lb/h/hp) | 169 | $\mu { m g}/{ m J}$ |
| pounds-force per square foot | 0.1414 | in Hg |
| (lbf/ft²) | 4.88243 | kgf/m² |
| (101/10) | 4.725×10^{-4} | atm |
| | 0.048 | kN/m^2 |
| pounds per square inch | 5.1715 | cm Hg |
| (psi or lbf/in ²) | 2.036 | in Hg |
| (psi or ior/in-) | 0.06805 | atm |
| | 0.0689476 | bar |
| | | |
| | 703.1 | kg/m ² |
| ************************************** | 6.89476 | kN/m ² |
| quart, US (qt) | 0.94635 | litre |
| | 57.750 | in ³ |
| madia na | 3.342×10^{-2} | ft ³ |
| radians | 57.30 | deg (arc) |
| 1. 1. 1. | 0.1592 | rev |
| radians per second (radians/s) | 57.296 | deg/s |
| | 0.1592 | rev/s |
| | 9.549 | rpm |
| revolutions (rev) | 6.283 | radians |
| revolutions per minute | 0.1047 | radians/s |
| (rpm or rev/min) | | |
| revolutions per second (rev/s) | 6.283 | radians/s |
| rod | 16.5 | ft |
| | 5.5 | yd |
| | 5.0292 | m |
| slug | 14.594 | kg |
| U | 32.174 | lb |
| slug feet ² (slug ft ²) | 1.3559 | kg m ² |
| | 4633.1 | lb in ² |
| | | |

TABLE 2-6 - continued

| Multiply | Ву | To obtain |
|--|-------------------------|------------------|
| square centimetres (cm ²) | 0.1550 | in ² |
| | 0.001076 | ft ² |
| quare feet (ft²) | 929.03 | cm ² |
| | 0.092903 | m^2 |
| | 144 | in² |
| | 0.1111 | yd² |
| | 2.296×10^{-5} | acres |
| uare inches (in²) | 6.4516 | cm ² |
| | 6.944×10^{-3} | ft² |
| juare kilometres (km²) | 0.3861 | stm ² |
| luare metres (m²) | 10.76391 | ft² |
| | 1.196 | yd² |
| | 0.0001 | ha |
| uare miles (mi²) | 2.590 | km² |
| | 640 | acres |
| uare rods (rod²) | 30.25 | yd² |
| uare yards (yd²) | 0.8361 | m² |
| | 9 | ft ² |
| | 0.0330579 | rod^2 |
| n | 2240 | lb |
| | 1016 | kg |
| | 1.016 | t (tonne) |
| n-force (tonf) | 9.964×10^{3} | N |
| ns per square foot (tonf/ft ²) | 107.252×10^{3} | kN/m^2 |
| att (W) | 1.34×10^{-3} | hp |
| | 10^{-3} | kW |
| rds (yd) | 0.9144 | m |
| | 3 | ft |
| | 36 | in |
| | 0.181818 | rod |

TABLE 2-7
General Notation*

| v | | |
|---------------|------------------|---------|
| X | Y | Z |
| ϕ (bank) | θ (pitch) | Ψ (yaw) |
| u | v | w |
| p | q | r |
| L (roll) | M (pitch) | N (yaw) |
| A | В | C |
| | u p L (roll) A | u v p q |

Table D-3. Torque Conversion Table, Pound Feet to Newton Meters

| Pound-Feet (lbft.) | Newton Metres (Nm) | Newton Metres (Nm) | Pound-Feet (lbft.) |
|--------------------|-----------------------|-----------------------|-----------------------|
| 1 | 1.356 | 1 | 0.7376 |
| 2 | 2.7 | 2 | 1.5 |
| 3 | 4.0 | 3 | 2.2 |
| 4 | 5.4 | 4 | 3.0 |
| 5 | 6.8 | 5 | 3.7 |
| 6 | 8.1 | 6 | 4.4 |
| 7 | 9.5 | 7 | 5.2 |
| 8 | 10.8 | 8 | 5.9 |
| 9 | 12.2 | 9 | 6.6 |
| 10 | 13.6 | 10 | 7.4 |
| 15 | 20.3 | 15 | 11.1 |
| 20 | 27.1 | 20 | 14.8 |
| 25 | 33.9 | 25 | 18.4 |
| 30 | 40.7 | 30 | 22.1 |
| 35 | 47.5 | 35 | 25.8 |
| 40 | 54.2 | 40 | 29.5 |
| 45 | 61.0 | 50 | 36.9 |
| 50 | 67.8 | 60 | 44.3 |
| 55 | 74.6 | 70 | 51.6 |
| 60 | 81.4 | 80 | 59.0 |
| 65 | 88.1 | 90 | 66.4 |
| 70 | 94.9 | 100 | 73.8 |
| 75 | 101.7 | 110 | 81.1 |
| 80 | 108.5 | 120 | 88.5 |
| 90 | 122.0 | 130 | 95.9 |
| 100 | 135.6 | 140 | 103.3 |
| 110 | 149.1 | 150 | 110.6 |
| 120 | 162.7 | 160 | 118.0 |
| 130 | 176.3 | 170 | 125.4 |
| 140 | 189.8 | 180 | 132.8 |
| 150 | 203.4 | 190 | 140.1 |
| 160 | 216.9 | 200 | 147.5 |
| 170 | 230.5 | 225 | 166.0 |
| 180 | 244.0 | 250 | 184.4 |

TABLE OF CONVERSION FACTORS

Because different conventions historically have been used to measure various quantities, the following tables have been compiled to sort out the different units. This first table identifies the units typically used for describing a particular quantity. For example, speed might be measured in "miles/hour".

Most quantities can also be described in terms of the following three basic dimensions:

length L mass M time T

For example, speed is given in terms of length divided by time, which can be written as "L/T". This description, called "dimensional analysis", is useful in

determining whether an equation is correct. The product of the dimensions on each side of the equal sign must match. For example:

Distance = Speed
$$\times$$
 Time
L = $L/T \times T$

The dimension on the left side of the equal sign is length, L. On the right side of the equal sign, the product of L/T times T is L, which matches the left side of the equation.

The second table is a Conversion Table, showing how to convert from one set of units to another. It might be necessary to take the reciprocal of the conversion factor or to make more than one conversion to get the desired results.

Measured Quantities and Their Common Units

Table of Conversion Factors

| Length(L) | Area(L²) | Volume(L³) | MULTIPLY | ВУ | TO OBTAIN: |
|----------------------|----------------------|----------------------------------|---|--------------------------|---------------------------------|
| mile(mi.) | sq. mile(mi²) | gallon(gal.) | Acres | 43560 | Sq. feet |
| yard(yd.) | sq. yard(yd²) | quart(qt.) | " | 0.004047 | Sq. kilometers |
| foot(ft.) | sq. foot(ft²) | pint(pt.) | " | 4047 | Sq. meters |
| inch(in.) | sq. inch(in²) | ounce(oz.) | , , | 0.0015625 | Sq. miles |
| fathom(fath.) | асте | cu. foot(ft³) | • | 4840 | Sq. yards |
| kilometer(km.) | sq. kilometer(km²) | cu. yard(yd³) | Acre-feet | 43560 | Cu. feet |
| meter(m.) | sq. meter(m²) | cu. inch(in³) | , , | 1233.5 | Cu. meters |
| centimeter(cm.) | sq. centimeter(cm²) | liter(1) | • | 1613.3 | Cu. yards |
| $micron(\mu)$ | oq. commotor(cm / | cu. centimeter(cm ³) | Angstroms(Å) | 1×10^{-6} | Centimeters |
| angstrom(Å) | | acre-foot | , | 3.937 × 10 ⁻⁹ | Inches |
| a300(1.1.) | | cord(cd) | - | 0.0001 | Microns |
| | | cord-foot | Atmospheres(atm.) | 76 | Cm. of Hg(O°C) |
| | | barrel(bbl.) | " | · 1033.3 | Cm. of H ₂ O(4°C) |
| | | oures, ooi., | • | 33.8995 | Ft. of H ₂ O(39.2°F) |
| Mass(M) | Speed(L/T) | Flow Rate(L3/T) | • | 29.92 | In. of Hg(32°F) |
| | • | | , | 14.696 | Pounds/sq. inch(psi) |
| pound(lb.) | feet/minute | cu. feet/min. | Barrels(petroleum, | 11.070 | r odridsystj. mentpsi) |
| | (ft./min.) | | U.S.)(bbl.) | 5.6146 | Cu. feet |
| ton(short) | feet/sec. | cu. meter/min. | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | 35 | Gallons(Imperial) |
| ton(long) | mile/hour | liters/sec. | | 42 | Gallons(U.S.) |
| ton(metric) | mile/min. | gallons/min. | | 158.98 | Liters |
| gram(g.) | kilometer/hr. | gallons/sec. | British Thermal | 100.70 | Lifetz |
| kilogram(kg.) | kilometer/min. | | Unit(Btu) | 251.99 | Calories, gm |
| | kilometer/sec. | | " | 777.649 | Foot-pounds |
| D | | | , | 0.00039275 | Horsepower-hours |
| Pressure(M/L/T²) | Energy(ML²/T²) | Power(ML^2/T^3) | - | 1054.35 | Joules |
| atmosphere(atm.) | British thermal | Btu./min. | | 0.000292875 | Kilowatt-hours |
| pounds/sq. inch(psi) | unit(Btu.) | Btu./hour | - | 1054.35 | Watt-seconds |
| inches of mercury | calories(cal.) | watt | Btu/hr. | 4.2 | Calories/min. |
| cm. of mercury | foot-pound | joule/sec. | " | 777.65 | Foot-pounds/hr. |
| feet of water | joule | cal./min. | " | 0.0003927 | Horsepower |
| | kilowatt-hour | horsepower(hp.) | " | 0.0003927 | Kilowatts |
| | (kw-hr.) | | * | 0.292875 | Watts(or joule/sec.) |
| | horsepower-hour | | Btu/lb. | 7.25 × 10 ⁻⁴ | Cal/gram |
| | (hphr.) | | Btu/sq. ft. | 0.271246 | Calories/sq. cm. |
| Time(T) | From: Donait (M/TZ) | Day on Day 11 (MCD) | | | (or langleys) |
| time(t) | Energy Density(M/T2) | Power Density(M/T³) | " | 0.292875 | Watt-hour/sq. foot |
| year(yr) | calories/sq. cm. | cal./sq. cm./min. | Btu/sq. ft./hour | 3.15×10^{-7} | Kilowatts/sq. meter |
| month | Btu./sq. foot | Btu./sq. foot/hr | " | 4.51×10^{-3} | Cal./sq. cm./min(or |
| day | langley | langley/min. | | | langleys/min) |
| hour(hr.) | watthr./sq. foot | watt/sq. cm. | " | 3.15×10^{-8} | Watts/sq. cm. |
| minute(min.) | - | - - | Calories(cal.) | 0.003968 | Btu. |
| second(sec.) | | | " | 3.08596 | Foot-pounds |
| | | | | | |

| Conversion Factors—Co | ······································ | | Furlong | 220 | Yards |
|-------------------------------|--|----------------------------------|------------------------------------|---------------------------------------|-----------------------------|
| " | 1.55857×10^{-6} | Horsepower-hours | Gallons(U.S., dry) | 1.163647 | Gallons(U.S., liq.) |
| • | 4.184 | Joules (or watt-secs) | Gallons(U.S., liq.) | 3785.4 | Cu. centimeters |
| " | 1.1622×10^{-6} | Kilowatt-hours | " | 0.13368 | Cu. feet |
| Calories, food unit | | | " | 231 | Cu. inches |
| (Cal.) | 1000 | Calories | " | 0.0037854 | Cu. meters |
| Calories/min. | 0.003968 | Btu/min. | " | 3.7854 | Liters |
| 7 · -/ | 0.06973 | Watts | " | 8 | Pints(U.S., liq.) |
| Calories/sq. cm. | 3.68669 1.0797 | Btu/sq. ft. | | 4 | Quarts(U.S., liq.) |
| 0-1/ /min | 1.0797 796320. | Watt-hr/sq. foot | Gallons/min. | 2.228 × 10 ⁻³ | Cu. feet/sec. |
| Cal./sq. cm./min. | 796320. 251.04 | Btu/sq. foot/hr. Watts/sq. cm | " | 0.06308 | Liters/sec. |
| Candle power | 251.04 | Watts/sq. cm. | Grams | 0.035274 | Ounces(avdp.) |
| (spherical) | 12.566 | Lumens | Grams-cm. | 0.002205 9.3011 × 10 ⁻⁸ | Pounds(avdp.) |
| Centimeters(cm.) | 0.032808 | Feet | Grams-cm. Grams/meter ² | 9.3011 × 10 ⁻⁴ | Btu. Short ton/acre |
| # | 0.3937 | Inches | Granis/meter | 3.98 8.92 | Short ton/acre lbs./acre |
| • | 0.01 | Meters | Horsepower | 8.92 42.4356 | ibs./acre Btu./min. |
| * | 10.000 | Microns | 1 loisepower | 550 | Foot-pounds/sec. |
| Cm. of Hg(O°C) | 0.0131579 | Atmospheres | 1 | 745.7 | root-pounds/sec. Watts |
| # | 0.44605 | Ft. of H ₂ O(4°C) | Horsepower-hrs. | 2546.14 | Watts Btu. |
| | 0.19337 | Pounds/sq. inch | # # | 641616 | Calories |
| Cm. of H ₂ O(4°C) | 0.0009678 | Atmospheres | ,, | 1.98 × 10° | Foot-pounds |
| VIII. OI 11201, | 0.003078 | Pounds/sq. inch | * | 0.7457 | Kilowatt-hours |
| Cm./sec. | 0.032808 | Feet/sec. | Inches | 2.54 | Centimeters |
| " | 0.022369 | Miles/hr. | " | 0.83333 | Feet |
| Cords | 8 | Cord-feet | In. of Hg(32°F) | 0.03342 | Atmospheres |
| " | 128(or 4×4×8) | Cu. feet | # | 1.133 | Feet of H ₂ O |
| Cu. centimeters | 3.5314667 | Cu. feet | | 0.4912 | Pounds/sq. inch |
| W | 0.06102 | Cu. inches | In. of Water(4°C) | 0.002458 | Atmospheres |
| " | 1 × 10 ⁻⁶ | Cu. meters | # " | 0.002436 | In. of Mercury(32°F) |
| * | 0.001 | Liters | | 0.03613 | Pounds/sq. inch |
| * | 0.0338 | Ounces(U.S. fluid) | Joules | 0.0009485 | Btu. |
| Cu. feet(ft.3) | 0.02831685 | Cu. meters | " | 0.73756 | Foot-pounds |
| * | 7.4805 | Gallons(U.S., liq.) | " | 0.0002778 | Watt-hours |
| " | 28.31685 | Liters | " | 1 | Watt-sec. |
| er . | 29.922 | Quarts(U.S., liq.) | Kilo calories/gram | 1378.54 | Btu/lb |
| Cu. ft. of H₂O | | | Kilograms | 2.2046 | Pounds(avdp.) |
| (60°F) | 62.366 | Pounds of H ₂ O | Kilograms/hectare | .893 | lbs/acre |
| Cu. feet/min. | 471.947 | Cu. cm./sec. | Kilograms/hectare | .0004465 | Short ton/acre |
| Cu. inches(in.3) | 16.387 | Cu. cm. | Kilometers | 1000 | Meters |
| w | 0.0005787 | Cu. feet | * | 0.62137 | Miles(statute) |
| * | 0.004329 | Gallons(U.S., liq.) | Kilometer/hr. | 54.68 | Feet/min. |
| • | 0.5541 | Ounces(U.S., fluid) | Kilowatts - | 3414.43 | Btu./hr. |
| Cu. meters | 1×10^6 | Cu. centimeters | , , | 737.56 | Foot-pounds/sec. |
| * | 35.314667 | Cu. feet | " | 1.34102 | Horsepower |
| | 264.172 | Gallons(U.S., liq.) | Kilowatt-hours | 3414.43 | Btu. |
| · - | 1000 | Liters | " | 1.34102 | Horsepower-hours |
| Cu. yard | 27 | Cu. feet | Knots | 51.44 | Centimeter/sec. |
| * | 0.76455 | Cu. meters | " | 1 | Mile(nautical)/hr. |
| | 201.97 | Gallons(U.S., liq.) | " | 1.15078 | Miles(Statute)/hr. |
| Cubits | 18 | Inches | Langleys | 1 | Calories/sq. cm. |
| Fathoms | 6 | Feet | Liters | 1000 | Cu. centimeters |
| | 1.8288 | Meters | " | 0.0353 | Cu. feet |
| Feet(ft.) | 30.48 | Centimeters | " | 0.2642 | Gallons(U.S., liq.) |
| # | 12 | Inches | " | 1.0567 | Quarts(U.S., liq.) |
| # | 0.00018939 | Miles(statute) | Lbs./acre | .0005 | Short ton/acre |
| Feet of H ₂ O(4°C) | 0.029499 | Atmospheres | Liters/min. | 0.0353 | Cu. feet/min. |
| " | 2.2419 | Cm. of Hg(0°C) | " | 0.2642 | Gallons(U.S., liq.)/min. |
| н | 0.433515 | Pounds/sq. inch | Lumens | 0.079577 | Candle power(spherica |
| Feet/min. | 0.508 | Centimeters/second | Lumens(at 5550Å) | | Watts |
| ~ | 0.018288 | Kilometers/hr. | Meters | 3.2808 | Feet |
| | 0.0113636 | Miles/hr. | " | 39.37 | Inches |
| Foot-candles | 1 | Lumens/sq. foot | | 1.0936 | Yards |
| Foot-pounds | 0.001285 | Btu. | Meters/sec. | 2.24 | Miles/hr. |
| * | 0.324048 | Calories | Micron | 10000 | Angstroms |
| " | 5.0505×10^{-7} | Horsepower-hours | " | 0.0001 | Centimeters |
| " | 3.76616×10^{-7} | Kilowatt-hours | Miles(statute) | 5280 | Feet |
| | | | | | |

| Conversion Factors—Co | ontinued | | " | 0.09290 | Sq. meters |
|-----------------------|-------------------------|----------------------|---|------------------------|-------------------|
| " | 1.6093 | Kilometers | Sq. inches | 6.4516 | Sq. centimeters |
| * | 1760 | Yards | • " | 0.006944 | Sq. feet |
| Miles/hour | 44.704 | Centimeter/sec. | Sq. kilometers | 247.1 | Acres |
| , | 88 | Feet/min. | , | 1.0764×10^{7} | Sq. feet |
| * | 1.6093 | Kilometer/hr. | ,, | 0.3861 | Sq. miles |
| " | 0.447 | Meters/second | Sq. meters | 10.7639 | Sq. feet |
| Milliliter | 1 | Cu. centimeter | | 1.196 | Sq. yards |
| Millimeter | 0.1 | Centimeter | Sq. miles | 640 | Acres |
| Ounces(avdp.) | 0.0625 | Pounds(avdp.) | · " | 2.788×10^{7} | Sa. feet |
| Ounces(U.S., liq.) | 29.57 | Cu. centimeters | , , | 2.590 | Sq. kilometers |
| * | 1.8047 | Cu. inches | Sq. yards | 9(or 3×3) | Sq. feet |
| ~ | 0.0625(or 1/16) | Pint(U.S., liq.) | 1 . | 0.83613 | Sq. meters |
| Pints(U.S., liq.) | 473.18 | Cu. centimeters | Tons, long | 1016 | Kilograms |
| * | 28.875 | Cu. inches | " | 2240 | Pounds(avdp.) |
| * | 0.5 | Quarts(U.S., liq.) | Tons(metric) | 1000 | Kilograms |
| Pounds(avdp.) | 0.45359 | Kilograms | " | 2204.6 | Pounds(avdp.) |
| * | 16 | Ounces(avdp.) | Tons, | | , |
| Pounds of water | 0.01602 | Cu. feet of water | metric/hectare | 0.446 | Short ton/acre |
| • | 0.1198 | Gallons(U.S., liq.) | Tons(short) | 907.2 | Kilograms |
| Pounds/acre | 0.0005 | Short ton/acre | " | 2000 | Pounds(avdp.) |
| Pounds/sq. inch | 0.06805 | Atmospheres | Watts | 3.4144 | Btu./hr. |
| * | 5.1715 | Cm. of mercury(O°C) | " | 0.05691 | Btu./min. |
| * | 27.6807 | In. of water(39.2°F) | " | 14.34 | Calories/min. |
| Quarts(U.S., liq.) | 0.25 | Gallons(U.S., liq.) | " | 0.001341 | Horsepower |
| * | 0.9463 | Liters | , " | 1 | Joule/sec. |
| • | 32 | Ounces(U.S., liq.) | Watts/sq. cm. | 3172 | Btu./sq. foot/hr. |
| * | 2 | Pints(U.S., liq.) | Watt-hours | 3.4144 | Btu. |
| Radians | 57.30 | Degrees | " | 860.4 | Calories |
| Sq. centimeters | 0.0010764 | Sq. feet | " | 0.001341 | Horsepower-hours |
| • | 0.1550 | Sq. inches | Yards | 3 | Feet |
| Sq. feet | 2.2957×10^{-5} | Acres | " | 0.9144 | Meters |

Gravitational or Engineer's System of Units

The other system of units is called the "gravitational" or "engineer's system." The unit of force is taken as the 1b., and the unit of mass is called the slug. (You see, all masses have a tendency "to stay put"; they are all reluctant to move; they are very sluggish.)

A mass of I slug is that which when acted upon by a force of I lb. will move with an acceleration of I ft. per sec.².

But we have already seen that a force of r lb. will cause a mass of g lb. to move with an acceleration of r ft. per sec.².

Therefore, a mass of I slug is equivalent to a mass of g lb.

The mass of a body in slugs is equal to $\frac{its \ weight \ in \ lb}{\sigma}$.

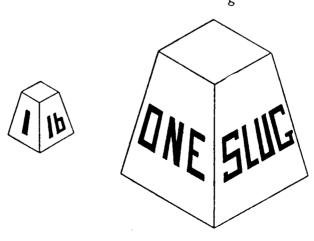


Fig. 29—The Two Units of Mass

If a force of 1 lb. were applied to the mass of 1 lb., it would move with an acceleration of 32.2 ft. per sec.2. If a force of 1 lb. were applied to the mass of 1 slug, it would move with an acceleration of 1 ft. per sec.2. The slug is approximately 32.2 times as big as the pound.

Useful equations and Conversion Factors

- Areas of a rectangle = Length x width
 Areas of a circle = π x (radius)²
 Surface area of a cylinder = 2π x radius x height + 2π x (radius)²
 Surface area of a sphere = 4π (radius)²
- 2. Volumes of a rectangular tank

 Volumes of a cylinder

 Volumes of a sphere $\begin{aligned}
 &= \text{Length} \times \text{Width} \times \text{Height} \\
 &= \pi \times (\text{radius})^2 \times \text{Height} \\
 &= \frac{4}{3}\pi \times (\text{radius})^3
 \end{aligned}$
- 3. Retention time = $\frac{\text{Volume of Tank}}{\text{Rate of flow of liquid or gas}}$
- 4. 1 inch = 2.54 cms. 1 foot = 0.305 m. 1 sq. m. = 10.76 sq. ft. 1 m. = 3.28 feet 1 sq. ft. = 0.093 sq. m. 1 cu. ft. = 28 litres = 0.028 m³.
- 5. 1 gallon = 4.55 litres 1 litre = 0.22 gallons 1 m³ = 220 gallons
- 6. 1 gallon occupies 0.161 cu. ft. 1,000 litres in 1 cu. m. 1 cu. ft. = 6.23 gallons
- 7. 1 gallon of water weighs 10 lbs. 1 litre of water weighs 1 kg.
- 8. 1 lb. = 0.454 kg. 1 kg. = 0.221 lb. 2240 lb. = 1 ton = 1.02 tonnes 1000 kg. = 1 tonne = 0.984 tonne
- 9. 1 part per million = 1 milligram/litre = 1 gm/m³ 1% = 10,000 ppm = 10,000 mgm/litre = 10 gm/litre
- 10. 1 cu. ft./lb. = $0.062 \,\mathrm{m}^3/\mathrm{kg}$. 1 m³/kg. = $16.1 \,\mathrm{cu}$. ft./lb.
- 11. 1 lb./cu. ft. = 16.2 kg./m^3 . 1 kg./m³. = 0.062 lb./cu. ft.
- 12. 1 acre = 4,840 sq. yards = 0.405 hectares 1 hectare = 10,000 sq. metres = 2.47 acres
- 13. $T^{\circ}F = \frac{5}{9} (T 32)^{\circ}C$ $T^{\circ}C = \frac{9}{5} T + 32^{\circ}F$
- 14. Pressure: 1 in. of water = 0.25 m. bar 1 lb/sq. in. (psi) = 68.95 m.bar 1 atmosphere = 1.013 m.bar
- 15. 1 British Thermal Unit = 0.252 Kcals. 1 BTU = 1,055 Joules 1 Kcal = 3.97 BTU 1 Joule = 9.5 x 10⁻⁴ BTU 1 Kcal = 4.19 kJ.
- 16. 100,000 BTU = 1 Therm = 29.3 kilowatt hours
- 17. 1 BTU/cu. ft. = 0.038 J/cm^3 (or Mega Joules/m³) 1 J/cm³ = 27.0 BTU/cu. ft.
- 18. 1 BTU/lb. = 2320 J/kg. $1J/kg. = 4.29 \times 10^{-3}$ BTU/lb.
- 19. 1 BTU/hr. = 0.0011 mJ/hr.
- 20. Heat transfer coefficient: 1 BTU/ft.²/° F/hr. = 20.44 kJ/m²/° C/hr.

APPENDIX: Conversion Factors

| To convert from: | То: | Multiply by: | | |
|--------------------------------------|-------------------|--------------|--|--|
| Length | | | | |
| centimeters (cm) | inches | 0.394 | | |
| feet (ft) | centimeters | 30.5 | | |
| inches (in) | centimeters | 2.54 | | |
| kilometers (km) | miles | 0.621 | | |
| meters (m) | feet | 3.28 | | |
| meters (m) | yards | 1.094 | | |
| miles (mi) | kilometers | 1.609 | | |
| millimeters (mm) | inches | 0.0394 | | |
| yards (yd) | meters | 0.914 | | |
| Area | | | | |
| acres | hectares | 0.405 | | |
| acres | sq. meters | 4047 | | |
| hectares (ha) | acres | 2.47 | | |
| hectares (ha) | sq. meters | 10,000 | | |
| sq. centimeters (cm ²) | sq. inches | 0.155 | | |
| sq. feet (ft ²) | sq. meters | 0.0929 | | |
| sq. inches (in ²) | sq. centimeters | 6.45 | | |
| sq. kilometers (km²) | sq. miles | 0.386 | | |
| sq. kilometers (km²) | hectares | 100 | | |
| sq. meters (m²) | sq. feet | 10.76 | | |
| sq. yards (yd²) | sq. meters | 0.836 | | |
| Volume | | | | |
| barrels (petroleum, bbl) | liters | 159 | | |
| cubic centimeters (cm ³) | cubic inches | 0.0610 | | |
| cubic feet (ft ³) | cubic meters | 0.0283 | | |
| cubic inches (in ³) | cubic centimeters | 16.39 | | |
| cubic meters (m ³) | cubic feet | 35.3 | | |
| cubic meters (m ³) | cubic yards | 1.308 | | |
| cubic yards (yd³) | cubic meters | 0.765 | | |
| gallons (gal) US | liters | 3.79 | | |
| gallons (gal) Imp. | liters | 4.545 | | |
| gallons (gal) Imp. | gallons, US | 1.20 | | |
| Weight | | | | |
| grams (g) | ounces, avdp. | 0.0353 | | |
| kilograms (kg) | pounds | 2.205 | | |
| ounces avdp. (oz) | grams | 28.3 | | |
| pounds (lb) | kilograms | 0.454 | | |
| tons (long) | pounds | 2240 | | |
| tons (long) | kilograms | 1016 | | |
| tons (metric) | pounds | 2205 | | |
| tons (metric) | kilograms | 1000 | | |
| tons (short) | pounds | 2000 | | |
| tons (short) | kilograms | 907 | | |

| To convert from: | То: | Multiply by: |
|-----------------------------|------------------------|--------------------|
| Pressure | | |
| atmosphere | grams/sq.cm | 1033 |
| atmosphere | pounds/sq.in | 14.7 |
| pounds/sq.in (psi) | grams/sq.cm | 70.3 |
| Energy | | |
| British thermal units (Btu) | kilojoules | 1.054 |
| calories (cal) | joules | 4.19 |
| ergs | joules | 1×10^{-7} |
| kilojoules (kJ) | Btu | 0.948 |
| joules (J) | calories | 0.239 |
| kilowatt-hours (kWh) | megajoules | 3.6 |
| megajoules (MJ) | kilojoules | 1000 |
| gigajoules (GJ) | megajoules | 1000 |
| terajoules (TJ) | gigajoules | 1000 |
| Energy Density | | |
| Btu/gal | joules/cm ³ | 0.27 |
| Btu/ft ³ | kJ/m³ | 36.5 |
| Power | | |
| horsepower (hp) | Btu/min | 42.4 |
| horsepower (hp) | horsepower (metric) | 1.014 |
| horsepower (hp) | kilowatts | 0.746 |
| kilowatts (kW) | horsepower | 1.341 |
| watts (W) | Btu/hour | 3.41 |
| watts (W) | joules/sec | 1 |
| Miscellaneous | • | |
| liter petrol | megajoules | 35 |
| kilogram oil | megajoules | 43.2 |
| barrel oil equivalent | gigajoules | 6.1 |
| ton coal equivalent | gigajoules | 29.3 |
| ton coal equivalent | barrels oil equivalent | 4.8 |
| pounds/acre | kilograms/hectare | 1.1 |

:

A. Conversions

Speed

1 m/s = 2.24 mph 1 mph = 0.446 m/s 1 knot = 1.15 mph 1 mph = 0.870 knots

Length

1 meter = 3.28 feet
1 foot = 0.305 meters
1 kilometer = 0.620 miles
1 mile = 1.61 kilometers

Area

1 square kilometer 0.386 square miles 1 square kilometer 1,000,000 square meters 1 square kilometer 100 hectares 1 square mile 2.59 square kilometers 1 square foot 0.093 square meters 1 square meter 10.76 square feet 1 hectare 10,000 square meters 1 hectare 2.47 acres 0.405 hectares 1 acre 1 acre 4049 square meters

Volume

1 cubic meter = 35.3 cubic feet

1 cubic feet = 0.028 cubic meters

1 liter = 0.264 gallons

1 gallon = 3.78 liters

1 cubic meter = 1000 liters

1 cubic meter = 264 gallons

1 gallon = 0.0038 cubic meters

Flow Rate

1 liter/second = 0.0044 gallons/minute

1 gallon/minute = 227 liters/second

1 cubic meter/minute = 264 gallons/minute

1 gallon/minute = 0.0038 cubic meters/minute

Weight

1 metric ton = 1.10 tons

1 kilogram = 2.20 pounds

1 pound = 0.454 kilograms

Energy Equivalency of Common Fuels

1 kWh = 3413 BTU

= 3.41 ft³ of natural gas

= 0.034 gallon of oil

= 0.00017 cord of wood

1 Therm = 105 BTU

= 100 ft³ of natural gas

= 1 gallon of oil

= 29.3 kWh of electricity

= 0.005 cord of wood

1 gallon of oil = 1 x 10⁵ BTU

 $1 \text{ cord of wood} = 2 \times 10^7 \text{ BTU}$

 $1000 \text{ ft}^3 \text{ (Mcf) natural gas} = 1 \times 10^6 \text{ BTU}$

| | , [| int J | mkg | ff lb | int kWh | IT kcal | BTU | ft³ lb/in² | atm dm³ | PSh | HPh | R · grd | Ī | | int kW | PS | нр |
|--------------|--------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|-----|---------------|---------------------------|----------------------------|----------------|
| 1.1 | 1 | 9,9981 · 10 ⁻¹ | 1,0197 - 10-1 | 7,3756 10-1 | 2,7772 · 10-7 | 2,3884 · 10·4 | 9,4782 - 10-4 | 5,1220 · 10 ⁻³ | 9,8692 · 10 ⁻³ | 3,7767 · 10 ⁻⁷ | 3,7251 · 10 ⁻⁷ | 1,2027 · 10 ⁻¹ | 1 | 1 erg/sec | 9,9981 - 10-11 | 1,3596 · 10 ⁻¹⁰ | 1,3410 - 10-10 |
| 1 int J | 1,0002 | 1 | 1,0199 · 10 ⁻¹ | 7,3770 · 10 ⁻¹ | 2,7778 · 10 ⁻⁷ | 2,3889 - 10-4 | 9,4800 - 10-4 | 5,1229 · 10 ⁻³ | 9,8711 · 10 ⁻³ | 3,7774 · 10-7 | 3,7258 10 ⁻⁷ | 1,2029 - 10-1 | | 1 int J/sec | 1,0000 - 10-3 | 1,3599 - 10-3 | 1,3413 - 10-3 |
| 1 mkg | 9,8066 | 9,8048 | 1 | 7,2330 | 2,7236 10-6 | 2,3422 · 10 ⁻³ | 9,2949 · 10 ⁻³ | 5,0229 · 10-2 | 9,6784 · 10-2 | 3,7037 - 10-6 | 3,6530 - 10-6 | 1,1794 | | 1 mkg/sec | 9.8048 10-3 | 1.3333 - 10-2 | 1,3151 - 10-2 |
| 1 ft lb | 1,3558 | 1,3556 | 1,3825 · 10 ⁻¹ | 1 | 3.7655 · 10-7 | 3,2383 - 10-4 | 1,2851 · 10 ⁻³ | 6.9444 - 10-3 | 1,3381 - 10-2 | 5,1206 · 10 ⁻⁷ | 5,0505 10 ⁻⁷ | 1,6306 - 10-1 | - | 1 ft lb/sec | 1,3556 · 10 ⁻³ | 1,8434 - 10-3 | 1,8182 - 10-3 |
| 1 int kWh | 3,6007 · 10 ⁶ | 3,6000 - 106 | 3,6717 · 105 | 2,6557 106 | 1 | 8,6000 · 10 ² | 3,4128 · 10 ³ | 1,8442 - 104 | 3,5536 - 104 | 1,3599 | 1,3413 | 4,3305 · 105 | | 1 int kW | 1 | 1,3599 | 1,3413 |
| 1 IT kcal | 4,1868 10 ³ | 4,1860 · 10 ³ | 4,2694 · 10 ² | 3,0884 · 10 ³ | 1.1628 · 10-3 | 1 | 3,9684 | 2,1445 - 10 | 4,1321 - 10 | 1,5813 · 10 ⁻³ | 1,5596 · 10 ⁻³ | 5,0355 · 10 ² | - | 1 IT kcal/sec | 4,1860 | 5,6925 | 5,6147 |
| 1 BTU | 1.0551 10 ³ | 1,0549 · 10 ³ | 1,0759 · 10 ² | 7,7817 102 | 2,9302 - 10-4 | 2,5199 · 10 ⁻¹ | 1 | 5,4040 | 1,0413 · 10 | 3,9847 - 10-4 | 3,9302 - 10-4 | 1,2689 · 10 ² | ı | 1 BTU/sec | 1,0549 | 1,4345 | 1,4149 |
| 1 ft³ lb/in² | 1,9524 · 10 ² | 1,9520 10 ² | 1,9909 - 10 | 1,4400 · 10 ² | 5,4223 · 10-5 | 4,6631 · 10 ⁻² | 1,8505 · 10 ⁻¹ | 1 | 1,9268 | 7,3736 - 10-5 | 7,2727 - 10-5 | 2,3481 - 10 | - 1 | 1 ft³ lb/in²h | 5,4223 - 10-5 | 7,3736 - 10-5 | 7,2727 - 10-5 |
| 1 atm dm³ | 1,0132 · 10 ² | 1,0131 10 ² | 1,0332 10 | 7,4734 10 | 2,8140 · 10 ⁻⁵ | 2,4201 · 10 ⁻² | 9,6038 - 10-2 | 5,1898 · 10 ⁻¹ | 1 | 3,8268 · 10 ⁻⁵ | 3,7744 - 10-5 | 1,2186 - 10 | - 1 | 1 atm dm³/h | 2,8140 - 10-5 | 3,8268 - 10-5 | 3,7744 - 10-5 |
| 1 PSh | 2,6478 - 106 | 2,6473 106 | 2,7000 · 105 | 1,9529 106 | 7.3536 · 10 ⁻¹ | 6,3241 · 10 ² | 2,5096 · 10 ³ | 1,3562 - 104 | 2,6132 - 104 | 1 | 9,8632 - 10-1 | 3,1845 - 105 | -1 | 1 PS | 7,3536 · 10 ⁻¹ | 1 | 9,8632 - 10-1 |
| 1 HPh | 2,6845 - 106 | 2,6840 - 106 | 2,7374 · 10 ⁵ | 1,9800 - 106 | 7,4556 · 10 ⁻¹ | 6,4118 · 10 ² | 2,5444 · 10 ³ | 1,3750 - 104 | 2,6494 - 104 | 1.0139 | 1 | 3,2287 · 10 ⁵ | - 1 | 1 HP | 7,4556 · 10 ⁻¹ | 1,0139 | 1 |
| 1 R · grd | 8,3147 | 8,3131 | 8,4786 - 10-1 | 6,1326 | 2,3092 - 10-6 | 1,9859 - 10-3 | 7,8808 10 ⁻³ | 4,2588 10-2 | 8,2060 - 10-2 | 3,1402 - 10-6 | 3,0973 - 10-6 | 1 | - 1 | 1 R grd/h | 2,3092 - 10-6 | 3,1402 - 10-6 | 3,0973 - 10-6 |

Table D-9. Kilowatts to Horsepower Conversion Table

| Kilowa 1 kW = | tts (kW) 1.3596 | into Ho HP | orsepov | ver (HP) |) | | | | | | | |
|------------------|--|---------------|---------|----------|--------|--------|--------|--------|--------|--------|-----|--|
| kW | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | kW | |
| 0 | 0 | 1,3596 | 2,72 | 4,08 | 5,44 | 6,80 | 8,16 | 9,52 | 10,88 | 12,24 | 0 | |
| 10 | 13,60 | 14,96 | 16,32 | 17,67 | 19,03 | 20,39 | 21,75 | 23,11 | 24,47 | 25,83 | 10 | |
| 20 | 27.19 | 28,55 | 29,91 | 31,27 | 32,63 | 33,99 | 35,35 | 36,71 | 38,07 | 39,43 | 20 | |
| 30 | 40,79 | 42,15 | 43,51 | 44,87 | 46,23 | 47,59 | 48,95 | 50,31 | 51,66 | 53,02 | 30 | |
| 40 | 54,38 | 55,74 | 57,10 | 58,46 | 59,82 | 61,18 | 62,54 | 63,90 | 65,26 | 66,62 | 40 | |
| 50 | 67,98 | 69,34 | 70,70 | 72,06 | 73,42 | 74,78 | 76,14 | 77,50 | 78,86 | 80,22 | 50 | |
| 60 | 81,58 | 82,94 | 84,30 | 85,65 | 87,01 | 88,37 | 89,73 | 91,09 | 92,45 | 93,81 | 60 | |
| 70 | 95,17 | 96,53 | 97,89 | 99,25 | 100,61 | 101,97 | 103,33 | 104,69 | 106,05 | 107,41 | 70 | |
| 80 | 108.77 | 110,13 | 111,49 | 112,85 | 114,21 | 115,57 | 116,93 | 118,29 | 119,64 | 121,00 | 80 | |
| 90 | 122,36 | 123,72 | 125,08 | 126,44 | 127,80 | 129,16 | 130,52 | 131,88 | 133,24 | 134,60 | 90 | |
| 100 | 135,96 | 137,32 | 138,68 | 140,04 | 141,40 | 142,76 | 144,12 | 145,48 | 146,84 | 148,20 | 100 | |
| | Horsepower (HP) into Kilowatts 1 HP = 0.7355 kW | | | | | | | | | | | |
| HP | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | HP | |
| 0 | 0 | 0,7355 | 1,47 | 2,21 | 2,94 | 3,68 | 4,41 | 5,15 | 5,88 | 6,62 | 0 | |
| 10 | 7,36 | 8,09 | 8,83 | 9,56 | 10,30 | 11,03 | 11,77 | 12,50 | 13,24 | 13,97 | 10 | |
| 20 | 14,71 | 15,45 | 16,18 | 16,92 | 17,65 | 18,39 | 19,12 | 19,86 | 20,59 | 21,33 | 20 | |
| 30 | 22,07 | 22,80 | 23,54 | 24,27 | 25,01 | 25,74 | 26,48 | 27,21 | 27,95 | 28,68 | 30 | |
| 40 | 29,42 | 30,16 | 30,89 | 31,63 | 32,36 | 33,10 | 33,83 | 34,57 | 35,30 | 36,04 | 40 | |
| 50 | 36,78 | 37,51 | 38,25 | 38,98 | 39,72 | 40,45 | 41,19 | 41,92 | 42,66 | 43,39 | 50 | |
| 60 | 44,13 | 44,87 | 45,60 | 46,34 | 47,07 | 47,81 | 48,54 | 49,28 | 50,01 | 50,75 | 60 | |
| 70 | 51,49 | 52,22 | 52,96 | 53,69 | 54,43 | 55,16 | 55,90 | 56,63 | 57,37 | 58,10 | 70 | |
| 80 | 58,84 | 59,58 | 60,31 | 61,05 | 61,78 | 62,52 | 63,25 | 63,99 | 64,72 | 65,46 | 80 | |
| 90 | 66,20 | 66,93 | 67,67 | 68,40 | 69,14 | 69,87 | 70,61 | 71,34 | 72,08 | 72,81 | 90 | |
| 100 | 73,55 | 74.29 | 75,02 | 75,76 | 76,49 | 77,23 | 77.96 | 78,70 | 79,43 | 80,17 | 100 | |

This table is very simple to use. Read off the tens in the vertical scale and the units in the hori-

Example (above): convert 63 kW into HP. Go down the first column until you find 60 and the across until you come to 3. The result is where the two rows join. 63 kW = 85.65 HP.

zontal scale. The answer is where the two lines meet.

For values of over 100, the decimal point should be adjusted. Example (below): Convert 65 HP into kW. Go down the first column until you find 60 and then

across until you come to 3. The result is where the two rows join. 63 HP = 46.34 kW. For values of over 100, the decimal point should be adjusted.

| One of: of these | For e | For example: 1 BTU has the energy of .00029 Kilo-watt-hours | | | | | | | | |
|---|------------|---|------------------|-------------------------|--------------------------|--|--|--|--|--|
| ** | BTU | K-watt hour | Kilo- Calorie | Horse- power hour | Gallon of gasoline | | | | | |
| BTU (British Thermal Unit) | 1 | .00029 | . 252 | .00039 | 7.4x10 ⁻⁶ | | | | | |
| Kilo-watt-hour | 3412 | 1 | 859 | 1.34 | .025 | | | | | |
| Kilo-calorie | 3.97 | .0016 | 1 | .00156 | 2.5x10 ⁻⁵ | | | | | |
| Horse-power hour | 2544 | .745 | 640 | 1 | .0188 | | | | | |
| Gallon of gasoline | 135,000 | 39.5 | 34,000 | 53.0 | 1 | | | | | |
| One pound raised one foot (one foot-pound) | .000128 | 3.7x10 ⁻⁷ | .00032 | 5.0x10 ⁻⁷ | 9.5x10 ⁻⁹ | | | | | |
| Joule (a metric unit) | .000948 | 2.8x10 ⁻⁷ | .00024 | 9.3x10 ⁻⁸ | 7.0x10 ⁻⁹ | | | | | |
| Energy collected by 40 sq. ft. S-rotor in 15 mph wind for one hour (see prob. 1. 1 on page 12) | 282 | . 0828 | 71.0 | .110 | .0021 | | | | | |
| Energy converted to electricity in line above (see prob. 1. 2 on page 12) | 127 | . 0374 | 32.0 | .050 | .00094 | | | | | |
| One gallon of water lifted 100 feet | 1.06 | .00031 | . 267 | .00041 | 7.8x10 ⁻⁶ | | | | | |
| Solar energy hitting one sq. * ft. for one hour | 442 | .129 | 111 | .173 | .0033 | | | | | |
| One gallon of water heated from 70 F to 212 F | 1184 | .347 | 298 | . 465 | .0088 | | | | | |
| One gallon of water at 212 F boiled away | 8078 | 2.36 | 2034 | 3.17 | .060 | | | | | |
| One cu. ft. natural gas | 1000 | . 29 | 252 | .39 | .0074 | | | | | |
| One gallon ethyl alcohol | 84,000 | 24.6 | 21,100 | 33.0 | .622 | | | | | |
| One cord of wood (average) | 12,000,000 | 3,660 | 3,150,000 | 4,910 | 92.5 | | | | | |
| One ton of coal | 25,000,000 | 7,327 | 6,300,000 | 9,830 | 185 | | | | | |
| One ton vehicle moving at 55 mph | 257 | .075 | 64.7 | .101 | .00257 | | | | | |

WARNING: These conversion factors refer to the total energy available and not to useful work. There will always be losses in converting one form of energy into work. That is part of the Second Law of Thermodynamics. That is also why you can't expect one gallon of boiling water to move a car at over 55 mph!

Note on scientific notation: The superscript above the 10 refers to where the decimal point goes. For example, $7.4 \times 10^{-6} = 0.0000074$ and $2.5 \times 10^{-5} = 0.000025$

^{*}This is the solar energy available above the earth's atmosphere. There is considerable loss in going through the air.

Conversion Tables

1. Conversion Factors

| To Convert From | То | Multiply By | | |
|-------------------------|-------------------------------|------------------------|--|--|
| Btu | Gram calories | 251.9958 | | |
| Btu | Kilogram calories | .00397 | | |
| Btu | Cubic centimeters atmospheres | 10405.6 | | |
| Btu | Cubic foot atmospheres | .36747 | | |
| Btu | Foot pounds | 777,649 | | |
| Btu | Horsepower hours | .0003927 | | |
| Btu | Kilowatt hours | .00029287 | | |
| Btu/square foot | Langleys | .271 | | |
| Btu/hour/square foot/°F | Watts/CM ² /°C | 5.6820×10 ⁴ | | |
| Cubic foot atmospheres | Btu | 2.721 | | |
| Cubic feet of water | Gallons | 7.4805 | | |
| Cubic feet of water | Pounds | 62.366 | | |
| Foot pounds | Btu | .001285 | | |
| Gallons of water | Cubic feet | 0.13368 | | |
| Gallons of water | Pounds | 8.3453 | | |
| Gram calories | Btu | .00397 | | |
| Horsepower | Foot pounds/hour | 1,980,000. | | |
| Horsepower | Foot pounds/minute | 33,000. | | |
| Horsepower | Foot pounds/second | 550. | | |
| Horsepower | Kilowatts | .7457 | | |
| Horsepower | Watts | 745.7 | | |
| Horsepower hours | Btu | 2546.14 | | |

| To Convert From | То | Multiply By |
|-------------------------|----------------------|--------------|
| Horsepower years | Btu | 22,304,186.4 |
| Kilogram calories | Btu | 3.97 |
| Kilowatts | Horsepower | 1.34102 |
| Kilowatt hours | Btu | 3414.43 |
| Langleys | Btu/square foot | 3.69 |
| Lumens (at 5,550 Å) | Watts | 0.0014706 |
| Months (mean calendar) | Hours | 730.1 |
| Pints (U.S., liq) | Cubic centimeters | 473.18 |
| Pints | Cubic inches | 28.875 |
| Pounds of water | Cubic feet of water | 0.01602 |
| Pounds of water | Gallons (U.S., liq) | 0.1198 |
| Watts | Btu/hour | 3.4144 |
| Watts | Btu/minute | 0.05691 |
| Watts | Calories/minute | 14.34 |
| Watts | Horsepower | 0.001341 |
| Watts/square centimeter | Btu/square feet/hour | 3,172. |
| Watt-hours | Btu | 3.4144 |
| Watt-hours | Calories | 860.4 |
| Watt-hours | Horsepower hours | 0.001341 |

2. Fahrenheit-Centigrade Conversion Table

The numbers in the center column, in boldface type, refer to the temperature in either Fahrenheit or Centigrade degrees. If it is desired to convert from Fahrenheit to Centigrade degrees, consider the center column as a table of Fahrenheit temperatures and read the corresponding Centigrade temperature in the column at the left. If it is desired to convert from Centigrade to Fahrenheit degrees, consider the center column as a table of Centigrade values, and read the corresponding Fahrenheit temperature on the right.

For conversions not covered in the table, the following formulas are used:

F = 1.8 C + 32

 $C = (F - 32) \div 1.8$

| Deg C | | Deg F | Deg C | | Deg F |
|----------------|--------|--------------|--------------|----------|----------------|
| -46 | - 50 | - 58 | 8.9 | 48 | 118.4 |
| -4 0 | - 40 | - 40 | 9.4 | 49 | 120.2 |
| -34 | - 30 | - 22 | 10.0 | 50 | 122.0 |
| -29 | - 20 | - 4 | 10.6 | 51 | 123.8 |
| -23 | - 10 | 14 | 11.1 | 52 | 125.6 |
| -17.8 | 0 | 32- | 11.7 | 53 54 | 127.4 |
| -17.2 | 1 | 33.8 | 12.2 | 54 | 129.2 |
| -16.7 | 2 | 35.6 | 12.8 13.3 | 55 56 | 131.0 |
| -16.1 | 3 | 37.4 39.2 | 13.9 | 56 57 | 132.8 |
| -15.6 | 4 | 41.0 | 14.4 | 58 | 134.6 136.4 |
| -15.0 | 5 6 | 42.8 | 15.0 | 59 | 138.2 |
| -14.4 | 7 | 44.6 | 15.6 | 60 | 140.0 |
| -13.9 -13.3 | 8 | 46.4 | 16.1 | 61 | 141.8 |
| -13.3 -12.8 | 9 | 48.2 | 16.7 | 62 | 143.6 |
| -12.0 | 10 | 50.0 | 17.2 | 63 | . 145.4 |
| -12.2 | 11 | 51.8 | 17.8 | 64 | 147.2 |
| -11.1 | 12 | 53.6 | 18.3 | 65 | 149.0 |
| -10.6 | 13 | 55.4 | 18.9 | 66 | 150.8 |
| -10.0 | 14 | 57.2 | 19.4 | 67 | 152.6 |
| - 9.4 | 15 | 59.0 | 20.0 | 68 | 154.4 |
| - 8.9 | 16 | 60.8 | 20.6 | 69 | 156.2 |
| - 8.3 | 17 | 62.6 | 21.1 | 70 | 158.0 |
| - 7.8 | 18 | 64.4 | 21.7 | 71 | 159.8 |
| - 7.2 | 19 | 66.2 | 22.2 | 72 | 161.6 |
| - 6.7 | 20 | 68.0 | 22.8 | 73 | 163.4 |
| - 6.1 | 21 | 69.8 | 23.3 | 74 | 165.2 |
| - 5.6 | 22 | 71.6 | 23.9 | 75 | 167.0 |
| - 5.0 | 23 | 73.4 | 24.4 | 76 | 168.8 |
| - 4.4 | 24 | 75.2 | 25,0 | 77 | 170.6 |
| - 3.9 | 25 | 77.0 | 25.6 | 78 | 172.4 |
| - 3.3 | 26 | 78.8 | 26.1 | 79 | 174.2 |
| - 2.8 | 27 | 80.6 | 26.7 | 80 | 176.0 |
| - 2.2 | 28 | 82.4 | 27.2 | 81 | 177.8 |
| - 1.7 | 29 | 84.2 | 27.8 | 82 | 179.6 |
| - 1.1 | 30 | 86.0 | 28.3 | 83 | 181.4 |
| - 0.6 | 31 | 87.8 | 28.9 | 84 | 183.2 |
| 0- | 32 | 89.6 | 29.4 | 85 | 185.0 |
| 0.6 | 33 | 91.4 | 30.0 | 86 | 186.8 |
| 1.1 | 34 | 93.2 | 30.6 | 87 | 188.6 |
| 1.7 | 35 | 95.0 | 31.1 | 88 | 190.4 |
| 2.2 | 36 | 96.8 | 31.7 | 89 | 192.2 |
| 2.7 | 37 | 98.6 | 32.2 | 90 | 194.0 |
| 3.3 | 38 | 100.4 | 32.8 | 91 | 195.8 |
| 3.9 | 39 | 102.2 | 33.3 | 92 | 197.6 |
| 4.4 | 40 | 104.0 | 33.9 | 93 | 199.4 |
| 5.0 | 41 | 105.8 | 34.4 | 94 | 201.2 |
| 5.6 | 42 | 107.6 | 35.0 | 95 | 203.0 |
| 6.1 | 43 | 109.4 | 35.6 | 96 07 | 204.8 |
| 6.7 | 44 | 111.2 | 36.1 | 97 | 206.6 |
| 7.2 | 45 | 113.0 | 36.7 | 98 | 208.4 |
| 7.8 | 46 | 114.8 | 37.2 | 99 | 210.2 |
| 8.3 | 47 | 116.6 | 37.8 | 100 | 212.0 |

Wind Chill Temperature Factor

| Knots | Meters/Sec. | | Ai | r Temper | ature | | | | | | | | |
|-------|-------------|----|----|-----------|-------|-----|-----|-----|-----|-----|-----|-----|-----|
| 0.0 | 0.0 | 25 | 20 | 15 | 10 | 5 | 0 | -5 | -10 | -15 | -20 | -25 | -30 |
| | | | Fe | lt Temper | ature | | | | | | | | |
| 5.0 | 2.5 | 25 | 19 | 14 | 9 | 3 | -2 | -7 | -12 | -17 | -23 | -28 | -33 |
| 9.0 | 4.5 | 22 | 16 | 10 | 4 | -2 | -8 | -14 | -20 | -26 | -32 | -36 | -44 |
| 13.0 | 7.0 | 21 | 15 | 8 | 2 | -4 | -11 | -18 | -25 | -32 | -38 | -45 | -52 |
| 19.0 | 9.5 | 21 | 14 | 7 | 0 | -7 | -14 | -21 | -29 | -36 | -43 | -50 | -57 |
| 24.0 | 12.5 | 21 | 13 | 5 | -2 | -9 | -17 | -24 | -32 | -39 | -47 | -54 | -61 |
| 30.0 | 15.5 # | 20 | 13 | 5 | -3 | -11 | -18 | -26 | -34 | -42 | -49 | -57 | -65 |
| 37.0 | 19.0 | 20 | 12 | 4 | -4 | -11 | -19 | -27 | -35 | -43 | -51 | -59 | -68 |
| 44.0 | 22.5 | 20 | 12 | 4 | -4 | -12 | -20 | -28 | -36 | -44 | -52 | -60 | -69 |

Notes:

Upper limit of safe crane operation.

^{- 21} degrees is the temperature for frozen meat in cold storage

Tables

9,87 % ~{~~~~1

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Table C Areas under the normal curve

Fractional parts of the total area (10,000) under the normal curve, corresponding to distances between the mean and ordinates which are Z standard-deviation units from the mean.

| | tne mean. | · · · · · · · · · · · · · · · · · · · | i | ī | i | 1 | 1 | 1 | 1 | 1 |
|--|--|---------------------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| Z | .00 | .01 | .02 | 03 | 04 | .05 | 06 | .07 | .08 | .09 |
| $\begin{array}{c} 0.0 \\ 0.1 \\ 0.2 \\ 0.3 \\ 0.4 \end{array}$ | 0000 | 0040 | 0080 | 0120 | 0159 | 0199 | 0239 | 0279 | 0319 | 0359 |
| | 0398 | 0438 | 0478 | 0517 | 0557 | 0596 | 0636 | 0675 | 0714 | 0753 |
| | 0793 | 0832 | 0871 | 0910 | 0948 | 0987 | 1026 | 1064 | 1103 | 1141 |
| | 1179 | 1217 | 1255 | 1293 | 1331 | 1368 | 1406 | 1443 | 1480 | 1517 |
| | 1554 | 1591 | 1628 | 1664 | 1700 | 1736 | 1772 | 1808 | 1844 | 1879 |
| 0.5 | 1915 | 1950 | 1985 | 2019 | 2054 | 2088 | 2123 | 2157 | 2190 | 2224 |
| 0.6 | 2257 | 2291 | 2324 | 2357 | 2389 | 2422 | 2454 | 2486 | 2518 | 2549 |
| 0.7 | 2580 | 2612 | 2642 | 2673 | 2704 | 2734 | 2764 | 2794 | 2823 | 2852 |
| 0.8 | 2881 | 2910 | 2939 | 2967 | 2995 | 3023 | 3051 | 3078 | 3106 | 3133 |
| 0.9 | 3159 | 3186 | 3212 | 3238 | 3264 | 3289 | 3315 | 3340 | 3365 | 3389 |
| 1.0 | 3413 | 3438 | 3461 | 3485 | 3508 | 3531 | 3554 | 3577 | 3599 | 3621 |
| 1.1 | 3643 | 3665 | 3686 | 3718 | 3729 | 3749 | 3770 | 3790 | 3810 | 3830 |
| 1.2 | 3849 | 3869 | 3888 | 3907 | 3925 | 3944 | 3962 | 3980 | 3997 | 4015 |
| 1.3 | 4032 | 4049 | 4066 | 4083 | 4099 | 4115 | 4131 | 4147 | 4162 | 4177 |
| 1.4 | 4192 | 4207 | 4222 | 4236 | 4251 | 4265 | 4279 | 4292 | 4306 | 4319 |
| 1.5 | 4332 | 4345 | 4357 | 4370 | 4382 | 4394 | 4406 | 4418 | 4430 | 4441 |
| 1.6 | 4452 | 4463 | 4474 | 4485 | 4495 | 4505 | 4515 | 4525 | 4535 | 4545 |
| 1.7 | 4554 | 4564 | 4573 | 4582 | 4591 | 4599 | 4608 | 4616 | 4625 | 4633 |
| 1.8 | 4641 | 4649 | 4656 | 4664 | 4671 | 4678 | 4686 | 4693 | 4699 | 4706 |
| 1.9 | 4713 | 4719 | 4726 | 4732 | 4738 | 4744 | 4750 | 4758 | 4762 | 4767 |
| 2.0 2.1 2.2 2.3 2.4 | 4773 | 4778 | 4783 | 4788 | 4793 | 4798 | 4803 | 4808 | 4812 | 4817 |
| | 4821 | 4826 | 4830 | 4834 | 4838 | 4842 | 4846 | 4850 | 4854 | 4857 |
| | 4861 | 4865 | 4868 | 4871 | 4875 | 4878 | 4881 | 4884 | 4887 | 4890 |
| | 4893 | 4896 | 4898 | 4901 | 4904 | 4906 | 4909 | 4911 | 4913 | 4916 |
| | 4918 | 4920 | 4922 | 4925 | 4927 | 4929 | 4931 | 4932 | 4934 | 4936 |
| 2.5 | 4938 | 4940 | 4941 | 4943 | 4945 | 4946 | 4948 | 4949 | 4951 | 4952 |
| 2.6 | 4953 | 4955 | 4956 | 4957 | 4959 | 4960 | 4961 | 4962 | 4963 | 4964 |
| 2.7 | 4965 | 4966 | 4967 | 4968 | 4969 | 4970 | 4971 | 4972 | 4973 | 4974 |
| 2.8 | 4974 | 4975 | 4976 | 4977 | 4977 | 4978 | 4979 | 4980 | 4980 | 4981 |
| 2.9 | 4981 | 4982 | 4983 | 4984 | 4984 | 4984 | 4985 | 4985 | 4986 | 4986 |
| 3.0 3.1 3.2 3.3 3.4 3.5 | 4986.5 4990.0 4993.129 4995.166 4996.631 4997.674 | 4987 4991 | 4987 4991 | 4988 4991 | 4988 4992 | 4988 4992 | 4989 4992 | 4989 4992 | 4989 4993 | 4990 4993 |
| 3.6 3.7 3.8 3.9 4.0 | 4998.409 4998.922 4999.277 4999.519 4999.683 | | | | | | | | | |
| $\begin{array}{c} 4.5 \\ 5.0 \end{array}$ | 4999.966 4999.997133 | | | | | | | | | |

SOURCE: Harold O. Rugg, Statistical Methods Applied to Education, Houghton Mifflin Company, Boston, 1917, appendix table III, pp. 389-390, with the kind permission of the publisher.

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Tables

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Table D Distribution of t

| able D | Distributio | | | | | | |
|--------|-------------|-------|---------------|----------------|-----------|---------|----|
| | | Level | of significan | ce for one-tai | iled test | | |
| | .10 | .05 | .025 | .01 | .005 | .0005 | |
| df | | Level | of significan | ce for two-tai | iled test | • | |
| | .20 | .10 | .05 | .02 | .01 | .001 | |
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 636.619 | |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 31.598 | |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 12.941 | |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 8.610 | |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 6.859 | |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 5.959 | |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 5.405 | |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 5.041 | |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 4.781 | |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 4.587 | |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 4.437 | |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 4.318 | |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 4.221 | |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 4.140 | |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 4.073 | |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 4.015 | |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 3.965 | |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 3.922 | |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 3.883 | |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 3.850 | |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 3.819 | |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 3.792 | |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 3.767 | |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 3.745 | |
| 25 | 1.316 | 1.708 | 2.060 | 2 .485 | 2.787 | 3.725 | |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 3.707 | |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 3.690 | |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 3.674 | |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 3.659 | |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 3.646 | |
| 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 | 3.551 | |
| 60 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 | 3.460 | 1 |
| 120 | 1.289 | 1.658 | 1.980 | 2.358 | 2.617 | 3.373 | k. |
| 00 | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | 3.291 | - |

source: Table D is abridged from Table III of R. A. Fisher and F. Yates, Statistical Tables for Biological, Agricultural and Medical Research (1948 ed.), published by Oliver & Boyd, Ltd., Edinburgh and London, by permission of the authors and publishers.

det name normal Kuru 196 = 47.50%

Table I Distribution of χ^2

(Sundsynlighed)

| | | | | | | P | robabi | lity | | 10% | 5 % | | ٠% | |
|----------|----------|----------|--------|----------|--------|--|----------|----------|--------|----------|----------|--|----------|--------|
| df | .99 | .98 | .95 | .90 | .80 | .70 | .50 | .30 | .20 | .10 | .05 | .02 | .01 | .001 |
| 1 | .03157 | .03628 | .00393 | .0158 | .0642 | .148 | . 455 | 1.074 | 1.642 | 2.706 | 3.841 | 5.412 | 6.635 | 10.827 |
| 2 | .0201 | .0404 | .103 | .211 | .446 | .713 | 1.386 | 2.408 | 3.219 | 4.605 | 5.991 | 7.824 | 9.210 | 13.815 |
| 3 | .115 | .185 | .352 | .584 | 1.005 | 1.424 | 2.366 | 3.665 | 4.642 | 6.251 | 7.815 | 9.837 | 11.341 | 16.268 |
| 4 | .297 | .429 | .711 | 1.064 | 1.649 | 2.195 | 3.357 | 4.878 | 5.989 | 7.779 | 9.488 | 11.668 | 13.277 | 18.465 |
| 5 | .554 | .752 | 1.145 | 1.610 | 2.343 | 3.000 | 4.351 | 6.064 | 7.289 | 9.236 | 11.070 | 13.388 | 15.086 | 20.517 |
| | | | | | | | | | | | | | | |
| 6 | .872 | 1.134 | 1.635 | 2.204 | 3.070 | 3.828 | 5.348 | 7.231 | 8.558 | 10.645 | 12.592 | 15.033 | | |
| 7 | 1.239 | 1.564 | 2.167 | 2.833 | 3.822 | 4.671 | 6.346 | 8.383 | 9.803 | 12.017 | 14.067 | 16.622 | | |
| 8 | 1.646 | 2.032 | 2.733 | 3.490 | 4.594 | 5.527 | 7.344 | 9.524 | 11.030 | 13.362 | 15.507 | | | |
| 9 | 2.088 | 2.532 | 3.325 | 4.168 | 5.380 | 6.393 | 8.343 | 10.656 | 12.242 | 14.684 | 16.919 | 19.679 | 21.666 | 27.877 |
| 10 | 2.558 | 3.059 | 3.940 | 4.865 | 6.179 | 7.267 | 9.342 | 11.781 | 13.442 | 15.987 | 18.307 | 21.161 | 23.209 | 29.588 |
| 11 | 3.053 | 3.609 | 4.575 | 5.578 | 6.989 | 8.148 | 10.341 | 12.899 | 14.631 | 17.275 | 19.675 | 22.618 | 24.725 | 31.264 |
| 12 | 3.571 | 4.178 | 5.226 | 6.304 | 7.807 | 9.034 | 11.340 | | 15.812 | 18.549 | | | | 32.909 |
| 13 | 4.107 | 4.765 | 5.892 | 7.042 | 8.634 | 9.926 | | 15.119 | 16.985 | | 22.362 | | | 34.528 |
| 14 | 4.660 | 5.368 | 6.571 | 7.790 | 9.467 | 10.821 | 13.339 | 16.222 | 18.151 | | 23.685 | | | 36.123 |
| 15 | 5.229 | 5.985 | 7.261 | 8.547 | 10.307 | 11.721 | 14.339 | 17.322 | 19.311 | 22.307 | 24.996 | | 30.578 | 37.697 |
| 10 | 0.225 | 0.800 | 1.201 | 0.011 | 10.001 | 11.721 | 11.000 | 11.022 | 15.011 | 22.001 | -1.000 | =0.200 | 00.010 | |
| 16 | 5.812 | 6.614 | 7.962 | 9.312 | 11.152 | 12.624 | 15.338 | 18.418 | 20.465 | 23.542 | 26.296 | 29.633 | 32.000 | 39.252 |
| 17 | 6.408 | 7.255 | 8.672 | 10.085 | 12.002 | 13.531 | 16.338 | 19.511 | 21.615 | 24.769 | 27.587 | 30.995 | 33.409 | 40.790 |
| 18 | 7.015 | 7.906 | 9.390 | 10.865 | 12.857 | 14.440 | 17.338 | 20.601 | 22.760 | 25.989 | 28.869 | 32.346 | 34.805 | 42.312 |
| 19 | 7.633 | 8.567 | 10.117 | 11.651 | 13.716 | 15.352 | 18.338 | 21.689 | 23.900 | 27.204 | 30.144 | 33.687 | 36.191 | 43.820 |
| 20 | 8.260 | 9.237 | 10.851 | 12.443 | 14.578 | 16.266 | 19.337 | 22.775 | 25.038 | 28.412 | 31.410 | 35.020 | 37.566 | 45.315 |
| | | | | | | | | | | | | | 1 | |
| 21 | 8.897 | | 11.591 | 13.240 | | 17.182 | 20.337 | 23.858 | 26.171 | | 32.671 | 36.343 | | 46.797 |
| 22 | 9.542 | 10.600 | 12.338 | | 16.314 | | 21.337 | 24.939 | 27.301 | 30.813 | l . | 37.659 | 40.289 | 48.268 |
| 23 | 10.196 | 11.293 | | 14.848 | 17.187 | 19.021 | 22.337 | 26.018 | 28.429 | 32.007 | | 38.968 | 41.638 | 49.728 |
| 24 | 10.856 | 11.992 | 13.848 | 15.659 | 18.062 | 19.943 | 23.337 | 27.096 | 29.553 | | | | 42.980 | 51.179 |
| 25 | 11.524 | 12.697 | 14.611 | 16.473 | 18.940 | 20.867 | 24.337 | 28.172 | 30.675 | 34.382 | 37.652 | 41.566 | 44.314 | 52.620 |
| 26 | 12.198 | 13.409 | 15.379 | 17.292 | 19.820 | 21.792 | 25.336 | 29.246 | 31.795 | 35.563 | 38.885 | 42.856 | 45.642 | 54.052 |
| 20 27 | 12.198 | 14.125 | 16.151 | | 20.703 | 22.719 | 26.336 | | | 36.741 | | 44.140 | 46.963 | 55.476 |
| 28 | 13.565 | 14.125 | 16.151 | | 21.588 | | | 31.391 | | 1 | | 45.419 | 48.278 | 56.893 |
| 29 | 14.256 | | 17.708 | 19.768 | | 24.577 | | | 35.139 | | 42.557 | 46.693 | 49.588 | 58.302 |
| 30 | 14.250 | 16.306 | 18.493 | 20.599 | 23.364 | | 29.336 | 33.530 | 36.250 | 40.256 | 43.773 | 47.962 | 50.892 | 59.703 |
| 00 | 17.000 | 10.000 | 10.400 | 20.039 | 20.004 | 20.000 | 25.550 | 35.000 | 30.200 | 20.200 | 10 | 1 | 30.002 | |
| | <u> </u> | <u> </u> | 1 | <u> </u> | 1 | <u>. </u> | <u> </u> | <u> </u> | ٠ | <u>'</u> | <u> </u> | <u>' </u> | <u> </u> | |

For larger values of df, the expression $\sqrt{2\chi^2} - \sqrt{2df-1}$ may be used as a normal deviate with unit variance, remembering that the probability for χ^2 corresponds with that of a single tail of the normal curve.

SOURCE: Table I is reprinted from Table IV of R. A. Fisher and F. Yates, Statistical Tables for Biological, Agricultural and Medical Research (1948 ed.), published by Oliver & Boyd Ltd,, Edinburgh and London, by permission of the authors and publishers.

| publishers. | 10 | 5 | 1 |
|-------------|---------|-------|-------|
| 40 | 51,81 | 55,76 | 63,64 |
| 60 | 74,40 | 14.08 | 88,38 |
| 40 | . 07, 6 | "3", | 124,1 |
| 20 | 140,2 | 146,6 | 154,0 |

Some Handy Rules

Diameter of a circle × 3.1416 = Circumference.

Radius of a circle \times 6.283185 = Circumference.

Square of the radius of a circle $\times 3.1416 = \text{Area}$.

Square of the diameter of a circle \times 0.7854 = Area.

Square of the circumference of a circle \times 0.07958 = Area.

Half the circumference of a circle × by half its diameter = Area.

Circumference of a circle \times 0.159155 = Radius.

Square root of the area of a circle \times 0.56419 = Radius.

Circumference of a circle \times 0.31831 = Diameter.

Square root a the area of a circle $\times 1.12838 = \text{Diameter}$.

Diameter of a circle \times 0.86 = Side of inscribed equilateral triangle.

Diameter of a circle \times 0.7071 = Side of an inscribed square.

Circumference of a circle \times 0.225 = Side of an inscribed square.

Circumference of a circle × 0.282 = Side of an equal square.

Diameter of a circle \times 0.8862 = Side of an equal square.

Base of a triangle \times by $\frac{1}{2}$ the altitude = Area.

Multiplying both diameters and .7854 together = Area of an ellipse.

Surface of a sphere \times by $\frac{1}{6}$ of its diameter = Solidity.

Circumference of a sphere \times by its diameter = Surface.

Square of the diameter of a sphere \times 3.1416 = Surface.

Square of the circumference of a sphere \times 0.3183 = Surface.

Cube of the diameter of a sphere $\times 0.5236 = \text{Solidity}$.

Cube of the radius of a sphere $\times 4.1888 = \text{Solidity}$.

Cube of the circumference of a sphere $\times 0.016887 = \text{Solidity}$.

Square root of the surface of a sphere $\times 0.56419 = \text{Diameter}$.

Square root of the surface of a sphere X 0.50419 = Diameter

Square root of the surface of a sphere $\times 1.772454 = \text{Circumference}$.

Cube root of the solidity of a sphere $\times 1.2407$ = Diameter.

Cube root of the solidity of a sphere \times 3.8978 = Circumference.

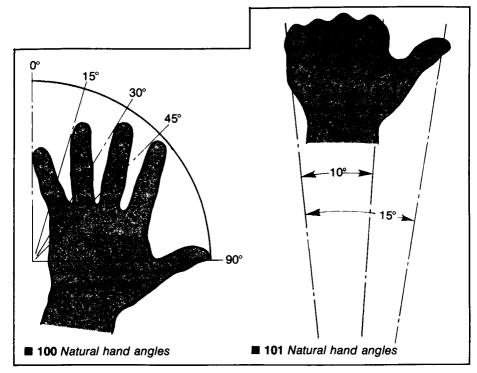
Radius of a sphere \times 1.1547 = Side of inscribed cube.

Square root of $(\frac{1}{3})$ of the square of) the diameter of a sphere = Side of inscribed cube.

Area of its base \times by $\frac{1}{3}$ of its altitude = Solidity of a cone or pyramid, whether round, square or triangular.

Area of one of its sides \times 6 = the surface of a cube.

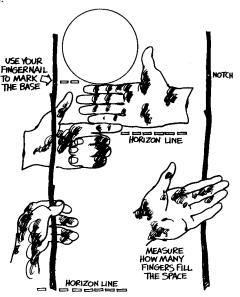
Altitude of trapezoid $\times \frac{1}{2}$ the sum of it parallel sides = Area.



Face the setting sun with arms extended and measure the distance between Ole Sol's base and the horizon in fingers (no thumbs). Each finger counts as fifteen minutes. Four of them, then, equal one hour . . . four on one hand and two on the other add up to an hour and a half . . . and so on.

If the space to be measured is greater than all eight fingers, hold a stick at arm's length with its base on the horizon and mark the position of the sun's bottom edge with your fingernail. The number of fingers it takes to fill the distance is your time.

In deep woods or hilly country where it's difficult to judge the horizon, work from an imaginary line at eye level.



Angles

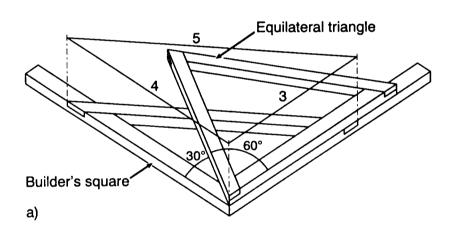
Set out a right-angle using a 3-4-5 triangle. This can be done in several ways:

- In the form of a builder's square make a 'builder's square' from accurately cut and fixed pieces of planed wood (Figure A23.6a) or simply cut from a sheet of plywood.
- Peg out both ends of one side (3m) of the triangle. Attach a string (of 4m length) to one peg and another string (of 5m length) to the other peg. Stretch out the strings to meet each other and a right angle will be formed at the corner (Figure A23.6b).
- An alternative to string is to wrap the measuring tape itself around the pegs and position to the correct lengths.

An equilateral triangle will give an angle of 60° and, when used together with a builder's square, an angle of 30°, and multiples thereof (Figure A23.6a).

Squareness

Check the squareness of a rectangle by measuring the length of the diagonals. They should be equal.



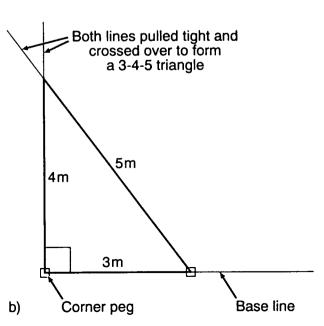
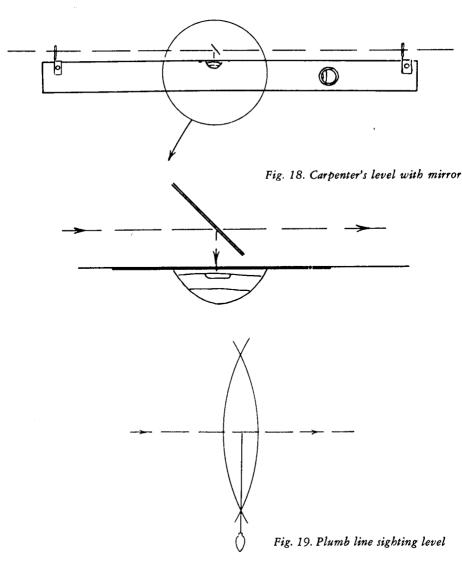


Figure A23.6 Setting out angles

It is not necessary to use a manufactured level when one can be easily made from scrap materials. Variations of the following device have been used for the past 4000 years in the Near Eastern area. It can be made with three sticks, five nails, a stone, a wire, and a piece of string. Even this list can be reduced by substituting lashings and pegs for the nails. The gadget is basically an isosceles triangle. with the base upward. If a plumb bob is hung from the midpoint of the upper side, then this side will be level when the plumb line crosses the bottom point of the triangle. The triangle does not have to be precisely constructed because an approximation will suffice for the frame. Two nails are driven part way into the face of the frame, one at each upper corner. Then, using the wire (a string would be too stretchy) and a nail as a compass, scribe two arcs of equal radius using these corner nails as the centers. These arcs should intersect on the triangular frame near the bottom corner. This point is marked. By a series of trial-and-error arcs of smaller radii, find the midpoint of the upper side. Drive a nail part way into the frame here. From this midpoint you suspend the stone (or other weight) on the string. When using this leveling frame, the surveyor sights across the upper corner nails and his assistant watches the device from the side to see that the plumb line hangs across the lower mark, that the device is being held level. Possibly some gadgeteer can devise a system of mirrors so he can watch the plumb line himself while taking the horizontal sight. (See Fig. 19.)

The same device can be used as a simple level, not as a sighting device, when it is turned with the point up instead of down. Some adjustment will have to be made to the plumb bob so that it doesn't strike the ground. Otherwise the principle and operation remain the same. (See Fig. 20.)



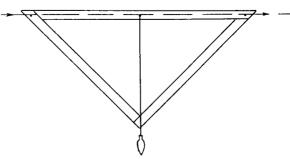
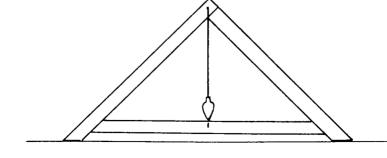
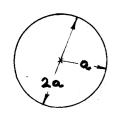


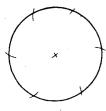
Fig. 20. Plumb line surface level



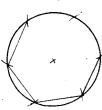
How to braw a Nexagon:



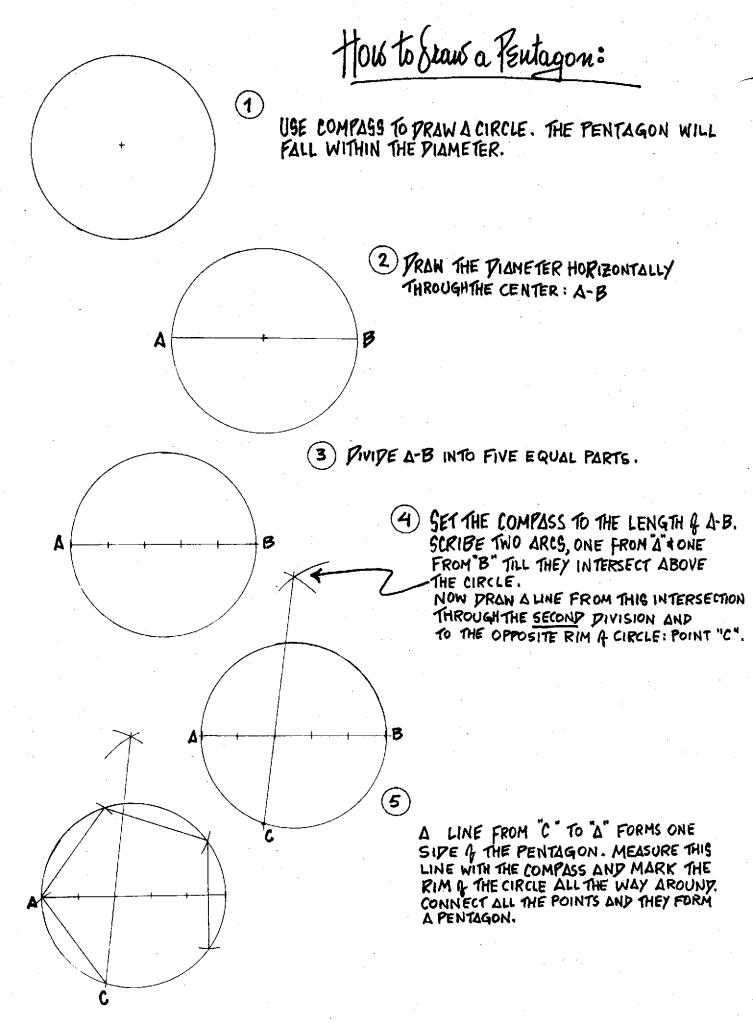
1 PECIPE ON THE GIZE YOU WANT & SET COMPASS
TO THE LENGTH of THE SIPE of HEXAGON (a). THIS
WILL BE THE RAPIUS of THE CIRCLE & ALSO &
THE CIRCLE'S PIAMETER. DRAW CIRCLE.



2 WITH THE COMPAGE STILL SET TO THE RADIUS (a), MARK OFF THIS RADIUS 6 TIMES AROUND THE CIRCLE'S EPGE.



3 CONNECT THE 6 POINTS YOU HAVE MARKED OFF WITH STRAIGHT LINES. YOU NOW HAVE A HEXAGON, ALL & ITS SIPES ARE (a) IN LENGTH.



MENSURATION. That part of mathematics which treats of the measurements of geometrical figures is called *mensuration*; it deals with the lengths of lines, the areas of surfaces, and the volumes of solids.

Lines. — A line is produced by the movement of a point. A straight line is one which has the same direction

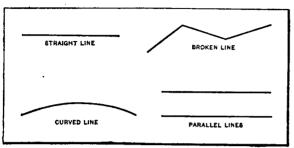
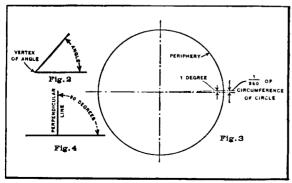


Fig. 1. Lines

throughout its length; it is also defined as the shortest distance between two points. A broken line is one which is made up of several straight lines, joined together, but having different directions. A curved line is one that constantly changes its direction; it is generally known as a curve. If two lines are drawn so that they are at all points at an equal distance from each other, they are said to be parallel. Parallel lines do not meet or intersect, no matter how far they may be extended or "produced" in either direction. (To extend a line in geometry is often called to produce the line.) The length of lines is measured in units of length, as inches, feet, miles, etc.

Surfaces. — A surface may be conceived of as produced by the movement of a line. A surface has two dimensions, length and breadth. The area of a surface is measured in square measure, as square inches, square



Figs. 2 to 4. Angular Measurements

feet, etc. A plane surface is one that is perfectly flat. A curved surface is one that has no plane or flat portion.

Angles. — When two lines meet as shown in Fig. 2, they form an angle with each other. The point where the two lines meet or intersect is called the *vertex* of the angle. The two lines forming the angle are called the sides of the angle. Angles are measured in degrees and subdivisions of a degree. If the circumference (periphery) of a circle is divided into 360 parts, each part is called one degree, and the angle between two lines from the center to the ends of

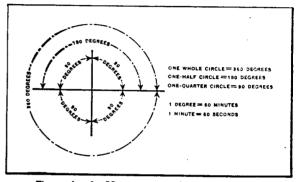


Fig. 5. Angular Measurements relative to the Circle

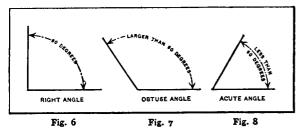
the small part of the circle is a one-degree angle, as shown in Fig. 3. As the whole circle contains 360 degrees, one-half of a circle contains 180 degrees, and one-quarter of a circle, 90 degrees.

A 90-degree angle is called a right angle. An angle larger than 90 degrees is called an obtuse angle, and an angle less than 90 degrees is called an acute angle. (See Figs. 6, 7, and 8.) Any angle which is not a right angle is called an oblique angle. When two lines form a right or 90-degree angle with each other, as shown in Fig. 4, one line is said to be perpendicular to the other.

Angles are said to be equal when they contain the same number of degrees. The angle shown in Fig. 9 and the angle in Fig. 10 are equal, because they are both 60 degrees; that the sides of the angle in Fig. 10 are longer than the sides of the angle in Fig. 9 has no influence on the angle,

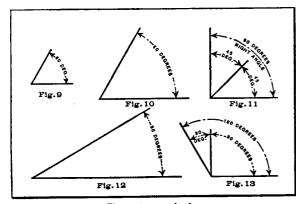
because of the fact that an angle is only the difference in direction of two lines. The angle shown in Fig. 12, which contains only 30 degrees, is only one-half of the angle in Fig. 9. One-half of a right angle is 45 degrees, as shown in Fig. 11. In Fig. 13 is shown an angle which is 120 degrees, and which can be divided into a right or 90-degree angle, and a 30-degree angle.

In order to obtain finer subdivisions for the measurement of angles than the degree, one degree is divided into 60 minutes, and one minute into 60 seconds. Any part of a degree can be expressed in minutes and seconds, for in-



stance, $\frac{1}{2}$ degree = 30 minutes, $\frac{1}{3}$ of a degree = 20 minutes; and since $\frac{1}{4}$ of a degree = 15 minutes, $\frac{3}{4}$ of a degree = 45 minutes. In the same way, $\frac{1}{2}$ minute = 30 seconds, $\frac{1}{3}$ minute = 20 seconds, $\frac{1}{4}$ minute = 15 seconds, and $\frac{3}{4}$ minute = 45 seconds. The word "degree" is often abbreviated "deg.," or the sign (°) is used to indicate degrees; thus 60° = 60 degrees. In the same way, 60' = 60 minutes (min.), 60'' = 60 seconds (sec.).

Measuring Angles in Radians. — While in practical work angles are always measured in degrees and minutes, the system for measuring angles in what is termed *circular measure* is often employed in theoretical investigations and in formulas relating to revolving bodies. In this system,



Figs. 9 to 13. Angles

the unit of measurement is the *radian*, that is, the angle at the center of a circle which embraces an arc equal in length to the length of the radius. The value of the radian in degrees equals $180 \div \pi = 57.2958$ degrees. In this measurement, then, π denotes an angle of 180 degrees, and $\pi \div 2$, an angle of 90 degrees.

It is especially convenient to measure angles in radians when dealing with angular velocity. If ω = angular velocity per second of the revolving body, in radians; v = velocity of a point on the periphery of the body, in feet per second; and r = the radius, in feet, then:

$$\omega = \frac{v}{r}$$

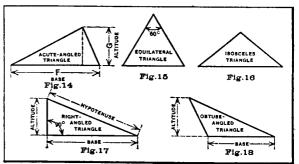
For example, assume that the velocity of a point on the periphery is 20 feet per second and the radius, 2 feet. Then the angular velocity is found as below:

$$\omega = \frac{30}{2} = 10$$
 radians.

The simple manner in which the relation between the angular velocity, the linear velocity, and the radius or diameter of the revolving body can be expressed, is the reason for using the radian as a convenient unit of angular measurement.

Triangles. — Any figure bounded by three straight lines is called a triangle. Any one of the three lines may be called the base, and the line drawn from the angle opposite the base at right angles to it is called the height or altitude of the triangle. In Fig. 14, if the side F is taken as the base of the triangle, then G is the altitude. If all three sides of a triangle are of equal length, as in the one shown in Fig. 15, the triangle is called equilateral. Each of the three angles in an equilateral triangle equals 60 degrees. If two sides are of equal length, as shown in Fig. 16, the triangle is an isosceles triangle.

If one angle is a right or 90-degree angle, the triangle is called a right or right-angled triangle. Such a triangle is



Figs. 14 to 18. Triangles

shown in Fig. 17; the side opposite the right angle is called the hypotenuse. If all the angles are less than 90 degrees, the triangle is called an acute or acute-angled triangle, as shown in Fig. 14. If one of the angles is larger than 90 degrees, as shown in Fig. 18, the triangle is called an obtuse or obtuse-angled triangle. The sum of the three angles in every triangle equals 180 degrees, or two right angles.

Right-angled Triangle. — Let A = area, and a, b, and c be the sides of the triangle, as shown in Fig. 19. Then:



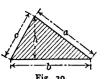
As an example, assume that the sides b and c in a right-angled triangle are 6 and 8 inches. Find side a and the area.

$$a = \sqrt{b^2 + c^2} = \sqrt{6^2 + 8^2} = \sqrt{36 + 64} = \sqrt{100} = 10$$
 in.
 $A = \frac{b \times c}{2} = \frac{6 \times 8}{2} = \frac{48}{2} = 24$ square inches.

If a = 10 and b = 6, had been known, but not c, the latter would have been found as follows:

$$c = \sqrt{a^2 - b^2} = \sqrt{10^2 - 6^2} = \sqrt{100 - 36} = \sqrt{64} = 8 \text{ in.}$$

Acute-angled Triangle. — Let A = area, and a, b, c, and h be the dimensions shown in Fig. 20. Then:



$$A = \frac{bh}{2} = \frac{b}{2} \sqrt{a^2 - \left(\frac{a^2 + b^2 - c^2}{2b}\right)^2}$$

If $S = \frac{1}{2}(a + b + c)$, then

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$
.
If $a = 10$, $b = 9$, and $c = 8$ inches,

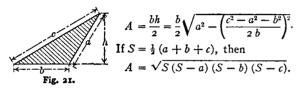
What is the area of the triangle?

$$A = \frac{b}{2} \sqrt{a^2 - \left(\frac{a^2 + b^2 - c^2}{2b}\right)^2} = \frac{9}{2} \sqrt{10^2 - \left(\frac{10^2 + 9^2 - 8^2}{2 \times 9}\right)^2}$$

$$= 4.5 \sqrt{100 - \left(\frac{117}{18}\right)^2} = 4.5 \sqrt{100 - 42.25} = 4.5 \sqrt{57.75}$$

$$= 4.5 \times 7.60 = 34.20 \text{ square inches.}$$

Obluse-angled Triangle. — Let A = area, and a, b, c, and h be the dimensions shown in Fig. 21. Then:



The side a = 5, side b = 4, and side c = 2 inches. Find the area.

$$S = \frac{1}{2} (a + b + c) = \frac{1}{2} (5 + 4 + 2) = \frac{1}{2} \times II = 5.5.$$

$$A = \sqrt{S(S - a)(S - b)(S - c)}$$

$$= \sqrt{5.5 (5.5 - 5)(5.5 - 4)(5.5 - 2)}$$

$$= \sqrt{5.5 \times 0.5 \times I.5 \times 3.5} = \sqrt{I4.437} = 3.8 \text{ sq. in.}$$

Square. — The square has four sides of equal length, and each of the four angles between the sides is a right or 90-degree angle. Let A = area, s = side, and d = diagonal of the square, as shown in Fig. 22. Then:



$$A = s^{2}.$$

$$A = \frac{1}{2}d^{2}.$$

$$s = 0.7071 d = \sqrt{A}.$$

$$d = 1.414 s = 1.414 \sqrt{A}.$$

Assume that the side s of a square is 15 inches. Find the area and the length of the diagonal.

Area =
$$A = s^2 = 15^2 = 225$$
 square inches.
Diagonal = $d = 1.414 s = 1.414 \times 15 = 21.21$ inches.

The area of a square is 625 square inches. Find the length of the side s and the diagonal d.

$$s = \sqrt{A} = \sqrt{625} = 25$$
 inches.
 $d = 1.414 \sqrt{A} = 1.414 \times 25 = 35.35$ inches.

Rectangle. — The rectangle, as shown in Fig. 23, has four sides, of which those opposite each other are of equal length, and the four angles between the sides are right or 90-degree angles. Let A = area, and a, b, and d be the dimensions shown in Fig. 23. Then:



$$A = ab.$$

$$A = a\sqrt{d^{2} - a^{2}} = b\sqrt{d^{2} - b^{2}}.$$

$$A = a\sqrt{a^{2} + b^{2}}.$$

$$A = \sqrt{a^{2} - b^{2}} = A \div b.$$

$$A = ab.$$

$$A$$

Assume that the side a of a rectangle is 12 inches, and the area, 70.5 square inches. Find the length of the side b, and the diagonal d.

$$b = A \div a = 70.5 \div 12 = 5.875$$
 inches.
 $d = \sqrt{a^2 + b^2} = \sqrt{12^2 + 5.875^2} = \sqrt{178.516} = 13.361$ in.

The sides of a rectangle are 30.5 and 11 inches long. Find the area.

Area =
$$a \times b$$
 = 30.5 \times 11 = 335.5 square inches.

Parallelogram. — Any figure made up of four sides, of which those opposite are parallel, is called a parallelogram. The square and rectangle are parallelograms in which all the angles are right angles. In Fig. 24 is shown a parallelogram where two of the angles are less and two more than 90 degrees. A line drawn from one side of a parallelogram at right angles to the opposite side is called the height or altitude of the parallelogram. In Fig. 24, a is the altitude, and b is the length or base. Let A = area. Then:



$$A = ab.$$

$$a = A \div b.$$

$$b = A \div a.$$

Fig. 24.

Note that dimension a is measured at right angles to line b.

As an example, assume that the base b of a parallelogram is 16 feet. The height a is 5.5 feet. Find the area.

Area =
$$A = a \times b = 5.5 \times 16 = 88$$
 square feet.

The area of a parallelogram is 12 square inches. The height is 1.5 inch. Find the length of the base b.

$$b = A \div a = 12 \div 1.5 = 8$$
 inches.



Trapezoid. — A figure bounded by four lines, of which only two are parallel, is called a trapezoid. The height of a trapezoid is the distance h, Fig. 25, between the two parallel lines. Let A = area and a, b, and h be the dimensions

shown in Fig. 25. Then

$$A = \frac{(a+b)\,h}{2}.$$

As an example, assume that side a=23 feet, side b=32 feet, and height h=12 feet. Find the area.

$$A = \frac{(a+b)h}{2} = \frac{(23+32)12}{2} = \frac{55 \times 12}{2} = \frac{660}{2} = 330 \text{ sq. ft.}$$

Trapezium. — A figure bounded by four lines, no two of which are parallel, as shown in Fig. 26, is called a tra-



pezium. Let A = area, and a, b, c, H, and h be the dimensions indicated in Fig. 26. Then:

$$A = \frac{(H+h)a + bh + cH}{2}.$$

Fig. 26.

A trapezium can also be divided into two triangles as indicated by the dotted line. The area of each of these triangles is computed, and the results added to find the area of the trapezium.

As an example, let a = 10, b = 2, c = 3, h = 8, and H = 12 inches. Find the area.

$$A = \frac{(H+h) a + bh + cH}{2} = \frac{(12+8) 10 + 2 \times 8 + 3 \times 12}{2}$$
$$= \frac{20 \times 10 + 16 + 36}{2} = \frac{252}{2} = 126 \text{ square inches.}$$

Regular Polygon. — Any plane figure or surface bounded by straight lines is called a *polygon*. (See Polygons.)



If all the sides are of equal length and the angles between the sides equal, the figure is called a regular polygon, as shown in Fig. 27. Let A = area, n = number of sides, s = length of side, R = radius of circumscribed circle, r = radius of sides, and the sides r = radius of $r = \text{r$

inscribed circle, and α and β , angles as indicated in Fig. 27. Then:

$$\alpha = 360^{\circ} \div n$$
; $\beta = 180^{\circ} - \alpha$.

$$A = \frac{nsr}{2} = \frac{ns}{2} \sqrt{R^2 - \frac{s^2}{4}}.$$

$$R = \sqrt{r^2 + \frac{s^2}{4}}; \ r = \sqrt{R^2 - \frac{s^2}{4}}; \ s = 2\sqrt{R^2 - r^2}.$$

As an example, find the area of a polygon having 12 sides, inscribed in a circle of 8 inches radius. The length of the side s is 4.141 inches.

$$A = \frac{ns}{2} \sqrt{R^2 - \frac{s^2}{4}} = \frac{12 \times 4.141}{2} \sqrt{8^2 - \frac{4.141^2}{4}}$$

= 24.846 \sqrt{59.713} = 24.846 \times 7.727 = 191.98 sq. in.

Regular Hexagon. — Of the regular polygons with more than four sides, the hexagon, having six sides, is the most commonly met with in mechanical work. Let A = area;



R= radius of circumscribed circle; r= radius of inscribed circle; and s= length of side. Then:

$$A = 2.598 \, s^2 = 2.598 \, R^2 = 3.464 \, r^2.$$

$$R = s = 1.155 r.$$

$$r = 0.866 s = 0.866 R$$

$$s = R = 1.155 r.$$

The side s of a regular hexagon is 4 inches. Find the area and the radius r of the inscribed circle.

$$A = 2.598 \, s^2 = 2.598 \times 4^2 = 2.598 \times 16 = 41.568 \, \text{sq. in.}$$

 $r = 0.866 \, s = 0.866 \times 4 = 3.464 \, \text{inches.}$

What is the length of the side of a hexagon that is described about a circle of 5 inches radius? — Here r = 5. Hence,

$$s = 1.155 r = 1.155 \times 5 = 5.775$$
 inches.

Regular Octagon. — A polygon having eight sides is called an octagon. Let A = area; R = radius of circumscribed circle; r = radius of inscribed



circle; and s = length of side. Then: $A = 4.828 \, s^2 = 2.828 \, R^2 = 3.314 \, r^2.$

R = 1.307 s = 1.082 r. r = 1.207 s = 0.924 R.s = 0.765 R = 0.828 r.

s = 0.765 R = 0 Fig. 29.

Find the area and the length of the side of an octagon that is inscribed in a circle of 12 inches diameter.

Diameter of circumscribed circle = 12 inches; hence, R = 6 inches.

$$A = 2.828 R^2 = 2.828 \times 6^2 = 2.828 \times 36 = 101.81 \text{ sq. in.}$$

 $s = 0.765 R = 0.765 \times 6 = 4.590 \text{ inches.}$

Circle. — The circle is a plane surface bounded by a curved line called the periphery or circumference, which is



at all points at an equal distance from a point within the circle called the *center*. The distance from the center of the circle to the periphery is the *radius*, and the distance across the circle through the center is the diameter. It is evident that the

radius is one-half of the diameter. If a line is drawn from one point on the periphery to another point, so that it does not pass through the center, it is called a *chord*.

Let A = area; C = circumference; d = diameter; and r = radius. Then:

$$A = \pi r^2 = 3.1416 \, r^2 = 0.7854 \, d^2.$$

$$C = 2\pi r = 6.2832 \, r = 3.1416 \, d.$$

$$r = C \div 6.2832 = \sqrt{A \div 3.1416} = 0.564 \, \sqrt{A}.$$

 $d = C \div 3.1416 = \sqrt{A \div 0.7854} = 1.128 \sqrt{A}$. Length of arc for center-angle of 1° = 0.008727 d. Length of arc for center-angle of $n^{\circ} = 0.008727$ nd.

Find the area A and circumference C of a circle with a diameter of $2\frac{3}{4}$ inches.

$$A = 0.7854 d^2 = 0.7854 \times 2.75^2 = 0.7854 \times 2.75 \times 2.75$$

= 5.9396 square inches.

$$C = 3.1416 d = 3.1416 \times 2.75 = 8.6394$$
 inches.

The area of a circle is 16.8 square inches. Find its diameter.

$$d = 1.128 \sqrt{A} = 1.128 \sqrt{16.8} = 1.128 \times 4.099 = 4.624 \text{ in.}$$

Circular Sector. — A figure bounded by a part of the circumference of a circle and two radii, as shown in Fig. 31,

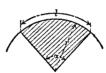


Fig. 31.

 α between the radii is called the angle of the sector, and the length l of the circumference of the circle is called the arc of the sector. Let A = area of sector; r = radius; α = angle of sector in degrees; and

is called a circular sector. The angle

l = length of arc. Then:

$$l = \frac{r \times \alpha \times 3.1416}{180} = 0.01745 \, r\alpha = \frac{2 \, A}{r}.$$

 $A = \frac{1}{2} rl = 0.008727 \alpha r^2$

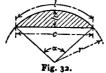
$$\alpha = \frac{57.296 \, l}{r}; \qquad r = \frac{2 \, A}{l} = \frac{57.296 \, l}{\alpha}.$$

The radius of a circle is $1\frac{1}{2}$ inch, and angle α of a sector of the circle is 60 degrees. Find the area of the sector and the length of arc l.

$$A = 0.008727 \,\alpha r^2 = 0.008727 \times 60 \times 1.5^2$$

= 0.5236 × 1.5 × 1.5 = 1.178 square inch.
 $l = 0.01745 \,r\alpha = 0.01745 \times 1.5 \times 60 = 1.5705$ inch.

Circular Segment. — A figure bounded by a part of the circumference of a circle and a chord, as shown in Fig. 32,



is called a circular segment. The distance h from the chord to the highest point of the circular arc is called the height of the segment. Let A = area of segment, and c, h, l, and r be the dimensions indicated

in Fig. 32; α = angle, in degrees. Then the following formulas are applicable:

$$c = 2\sqrt{h(2r - h)}. \qquad A = \frac{1}{2}[rl - c(r - h)].$$

$$r = \frac{c^2 + 4h^2}{8h}. \qquad l = 0.01745 r\alpha.$$

$$h = r - \frac{1}{2}\sqrt{4r^2 - c^2}. \qquad \alpha = \frac{57.296 l}{10.01745 r\alpha}.$$

The radius r of a circular segment is 60 inches and the height h is 8 inches. Find the length of the chord c.

$$c = 2\sqrt{h(2r-h)} = 2\sqrt{8 \times (2 \times 60 - 8)} = 2\sqrt{896}$$

= 2 × 29.93 = 59.86 inches.

If c = 16, and h = 6 inches, what is the radius of the circle of which the segment is a part?

$$r = \frac{c^2 + 4h^2}{8h} = \frac{16^2 + 4 \times 6^2}{8 \times 6} = \frac{256 + 144}{48} = \frac{400}{48} = 8\frac{1}{8}$$
 in.

Circular Ring. — An area bounded by two concentric



circles, that is, by two circles having a common center but radii of different lengths, is generally called a circular ring or an annular surface, as shown in Fig. 33. Let A = area. D = diameter, and R = radius of large circle, d = diameter, and r =

radius of small circle. Then:

 $A = \pi (R^2 - r^2) = 3.1416 (R^2 - r^2)$ = 3.1416 (R + r) (R - r) $= 0.7854 (D^2 - d^2) = 0.7854 (D + d) (D - d).$

Let the outside diameter D = 12 inches and the inside diameter d = 8 inches. Find the area of the ring.

$$A = 0.7854 (D^2 - d^2) = 0.7854 (12^2 - 8^2)$$

= 0.7854 (144 - 64) = 0.7854 × 80
= 62.83 square inches.

By the alternative formula:

$$A = 0.7854 (D + d) (D - d) = 0.7854 (12 + 8) (12 - 8)$$

= 0.7854 × 20 × 4 = 62.83 square inches.



Circular Ring Sector. - In a circular ring sector (or annular sector). as shown in Fig. 34, let A = area, and α = angle of sector in degrees; let D, d, R, and r be the dimensions indicated in the illustration. Then:

 $A = \frac{\alpha\pi}{260} (R^2 - r^2) = 0.00873 \alpha (R^2 - r^2)$ $= \frac{\alpha \pi}{4 \times 360} (D^2 - d^2) = 0.00218 \alpha (D^2 - d^2).$

Find the area, if the outside radius R = 5 inches, the inside radius r = 2 inches, and $\alpha = 72$ degrees.

$$A = 0.00873 \alpha (R^2 - r^2) = 0.00873 \times 72 (5^2 - 2^2)$$

= 0.6286 (25 - 4) = 0.6286 \times 21 = 13.2 sq. in.

Spandrel or Fillet. — The area enclosed between a circular arc equal to one-quarter of the complete circle, and two tangents to the circle at the extreme ends of the arc, as shown in Fig. 35. is called a spandrel or fillet. Let A =area, and c and r be the dimen-

sions indicated in Fig. 35. Then:

$$A = r^2 - \frac{\pi r^2}{4} = 0.215 \, r_a^2 = 0.1075 \, c^2$$

Find the area of a spandrel, the radius of which is 0.7 inch.

$$A = 0.215 r^2 = 0.215 \times 0.7^2$$

= 0.215 × 0.7 × 0.7 = 0.105 square inch.

If chord c were given as 2.2 inches, what would be the area?

$$A = 0.1075 c^2 = 0.1075 \times 2.2^2$$

= 0.1075 × 4.84 = 0.520 square inch.

Ellipse. — The ellipse is a plane surface bounded by a curved line having two diameters or axes of different length; the longer of these is called the major axis, the



shorter, the minor axis. The point where these two axes intersect is called the center of the ellipse. An ellipse is formed by taking a section through a cylinder in a plane at an oblique angle to the axis of the

cylinder. In Fig. 36, a = one-half the major axis, and b = one-half the minor axis. Let A = the area of the ellipse, and P = the perimeter or circumference. Then:

$$A = \pi ab = 3.1416 ab.$$

The circumference of an ellipse cannot be obtained exact by any formula. An approximate formula for the perimeter is:

$$P = 3.1416 \sqrt{2(a^2 + b^2)}$$
.

A closer approximation is:

$$P = 3.1416 \sqrt{2(a^2 + b^2) - \frac{(a - b)^2}{2.2}}.$$

The larger or major axis of an ellipse is 8 inches. The smaller or minor axis is 6 inches. Find the area and the approximate circumference. Here, then, a = 4, and b = 3.

A = 3.1416 ab = 3.1416
$$\times$$
 4 \times 3 = 37.699 sq. in.
P = 3.1416 $\sqrt{2(a^2 + b^2)}$ = 3.1416 \times $\sqrt{2(4^2 + 3^2)}$
= 3.1416 \times $\sqrt{2 \times 25}$ = 3.1416 $\sqrt{50}$ = 3.1416
 \times 7.071 = 22.214 inches.

Hyperbola. — The hyperbola is an open curve having two branches, each extending into the infinite, and is ob-



tained by taking a section through a cone parallel to the axis, or by a section at an angle to the axis, providing the angle is less than the angle between the axis and the side of the cone. The area A, enclosed by the hyperbolic curve BD, its

principal axis BC, and the line CD, perpendicular to BC as shown in Fig. 37, is found by the formula:

$$A = \frac{xy}{2} - \frac{ab}{2}$$
 hyp. $\log \left(\frac{x}{a} + \frac{y}{b}\right)$,

in which a, b, x, and y are dimensions indicated in the

The half-axes a and b are 3 and 2 inches, respectively. Find the area shown shaded in the illustration for x = 8and $\nu = 5$.

Inserting the known values in the formula:

$$A = \frac{8 \times 5}{2} - \frac{3 \times 2}{2} \times \text{hyp. log.} \left(\frac{8}{3} + \frac{5}{2}\right)$$

= 20 - 3 × hyp. log. 5.167 = 20 - 3 × 1.6423
= 20 - 4.927 = 15.073 sq. in.

Parabola. - The parabola is an open curve having two branches, each extending into the infinite, and is ob-



tained by taking a section through a cone parallel to the side of the cone. The length l of a parabolic arc, when p, x, and y are known, as shown in Fig. 38, is found from the formula (distance p is known as the

Fig. 38.

parameter of the parabola):

$$l = \frac{p}{2} \left[\sqrt{\frac{2x}{p}} \left(1 + \frac{2x}{p} \right) + \text{hyp. log.} \left(\sqrt{\frac{2x}{p}} + \sqrt{1 + \frac{2x}{p}} \right) \right].$$

When x is small in proportion to y, the following is a close approximation:

$$l = y \left[1 + \frac{2}{3} \left(\frac{x}{y} \right)^2 - \frac{2}{5} \left(\frac{x}{y} \right)^4 \right], \text{ or } l = \sqrt{y^2 + \frac{4}{3} x^2}.$$

If x = 2 and y = 24 feet, what is the approximate length l of the parabolic curve?

$$l = y \left[1 + \frac{2}{3} \left(\frac{x}{y} \right)^2 - \frac{2}{5} \left(\frac{x}{y} \right)^4 \right] = 24 \left[1 + \frac{2}{3} \left(\frac{2}{24} \right)^2 - \frac{2}{5} \left(\frac{2}{24} \right)^4 \right]$$
$$= 24 \left[1 + \frac{2}{3} \times \frac{1}{144} - \frac{2}{5} \times \frac{1}{20,736} \right] = 24 \times 1.0046 = 24.11 \text{ ft.}$$

The area enclosed between an arc of the parabola, its axis, and a line y (Fig. 39), at right angles to the axis, is



equal to two-thirds of the rectangle which has x for its base and y for its height or altitude; or, if A =area, then:

$$A = \frac{2}{3} xy.$$

Let the dimension x in the illustration be 15 inches, and y, 9 inches. Find the area of the shaded portion of the parabola.

$$A = \frac{2}{3} \times xy = \frac{2}{3} \times 15 \times 9 = 10 \times 9 = 90 \text{ sq. in.}$$

Segment of Parabola. - A segment of a parabola is en-



closed between an arc of the parabola and a chord which intersects the arc at two points. In Fig. 40,

Area $BFC = \frac{3}{4}$ area of parallelogram BCDE.

If FG is the height of the segment, measured at right angles to BC, then:

Area of segment $BFC = \frac{2}{3}BC \times FG$.

The length of the chord BC = 19.5 inches. The distance between lines BC and DE, measured at right angles to BC, is 2.25 inches. This is the height of the segment. Find the area.

Area =
$$\frac{2}{3}BC \times FG = \frac{2}{3} \times 19.5 \times 2.25 = 29.25 \text{ sq. in.}$$

Cycloid. — The cycloid is a curve described by a given point of a circle, if the circle is rolled along a straight line.



The circle which rolls upon the line is called a generating circle. Let A be the area enclosed between the cycloidal curve and the line upon which the generating circle rolls; I

is the length of the cycloid; d is the diameter and r the radius of the generating circle. Then:

$$A = 3 \pi r^2 = 9.4248 r^2 = 2.3562 d^2$$

= 3 × area of generating circle.
 $l = 8 r = 4 d$.

The diameter of the generating circle of a cycloid is 6 inches. Find the length l of the cycloidal curve, and the area enclosed between the curve and the base line.

$$l = 4 d = 4 \times 6 = 24$$
 inches.
 $A = 2.3562 d^2 = 2.3562 \times 6^2 = 2.3562 \times 36$
= 84.82 square inches.

Plane Surfaces of Irregular Outline. - The areas of plane surfaces of irregular outline can best be found by dividing the surfaces into a number of geometrical figures, the areas of which can be found by the general rules and formulas. The most convenient method is, as a rule, to divide the area into a number of narrow strips which may be regarded as rectangles, the base of the rectangle being the width of the strip, and a line through the center of the strip, its mean height. Surfaces of irregular outline, having straight boundary lines, are most conveniently divided into a number of triangles, the areas of which can be readily found and added together.

Cube. — The cube, Fig. 42, is a solid body having six



surfaces or faces, all of which are squares; as all the faces are squares, all the sides are of equal length. Let V = volume of cube, and s =length of side. Then:

$$V = s^3.$$

$$s = \sqrt[4]{V}.$$

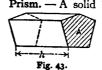
The side of a cube equals 9.5 inches. Find its volume.

Volume =
$$V = s^3 = 9.5^3 = 9.5 \times 9.5 \times 9.5$$

= 857.375 cubic inches.

The volume of a cube is 231 cubic inches. What is the length of the side?

$$s = \sqrt[3]{V} = \sqrt[3]{231} = 6.136$$
 inches.



Prism. — A solid body having the end faces parallel. and the lines along which the other faces intersect or meet parallel, is called a prism. The two parallel end faces are called bases. The length, height, or altitude h, Fig. 43,

of a prism is the distance between the bases, measured at right angles to the base surfaces.

The volume of a prism equals the area of the base multiplied by the length or height h of the prism. The area of the base must, therefore, first be found before the volume can be obtained. If the base is a triangle, parallelogram, trapezoid, trapezium, or a regular polygon, its area is found by the rules given in preceding paragraphs. If it is a polygon which is not regular, it can always be divided into triangles, and the area of each of the triangles can be calculated, and these areas added together, to obtain the area of the whole polygon. Let V = volumeof prism, h = height of prism measured perpendicular to the end surface, and A = area of end surface. Then:

$$V = h \times A$$
.

A prism having for its base a regular hexagon, with a side s of 3 inches, is 10 inches high. Find the volume.

Area of hexagon =
$$A = 2.598 \text{ s}^2 = 2.598 \times 9$$

= 23.382 square inches.
Volume of prism = $h \times A = 10 \times 23.382$
= 233.82 cubic inches.

Square Prism. — A solid body, the sides of which are all rectangles, and the ends of which are either rectangles



or squares, is commonly called a square prism. Opposite surfaces or faces are parallel, and all the angles are right angles. A square prism is shown in Fig. 44, where a is its

length, b, its height, and c, its width. Let V = volume of square prism, then:

$$V = abc.$$

$$a = \frac{V}{bc}, \quad b = \frac{V}{ac}, \quad c = \frac{V}{ab}.$$

In a square prism, a = 6, b = 5, c = 4. Find the volume.

$$V = a \times b \times c = 6 \times 5 \times 4 = 120$$
 cubic inches.

How high should a box be made to contain 25 cubic feet, if it is 4 feet long and $2\frac{1}{2}$ feet wide? Here, a = 4, c = 2.5, and V = 25. Then:

$$b = \text{depth} = \frac{V}{ac} = \frac{25}{4 \times 2.5} = \frac{25}{10} = 2.5 \text{ feet.}$$

Pyramid. — A solid body having a polygon for the base and a number of triangles all having a common vertex for the sides is called a *pyramid*. In Fig. 45 a pyramid is shown where the base has six sides and the side surfaces



are made up of triangles having two equal sides. If a line is drawn from the vertex of the pyramid at *right* angles to the base, the length of this line is the altitude or height h of the pyramid. The volume of a

pyramid equals the base area multiplied by one-third of the height. It is, therefore, necessary to find the base area before the volume can be found. Let V = volume of pyramid, and h = height perpendicular to base. Then:

$$V = \frac{1}{3}h \times \text{area of base.}$$

If the base is a regular polygon with n sides, and s = length of side, r = radius of inscribed circle, and R = radius of circumscribed circle, then:

$$V = \frac{nsrh}{6} = \frac{nsh}{6} \sqrt{R^2 - \frac{s^2}{4}}.$$

A pyramid, having a height of 9 feet, has a base formed by a rectangle, the sides of which are 2 and 3 feet, respectively. Find the volume.

Area of base = $2 \times 3 = 6$ square feet; h = 9 feet. Volume = $V = \frac{1}{3}h \times \text{area}$ of base = $\frac{1}{3} \times 9 \times 6$ = 18 cubic feet.

Frustum of Pyramid. — A frustum of a pyramid is shown in Fig. 46. It is a pyramid from which the top has been cut off, the top surface being parallel to the



base. The height h of a frustum of a pyramid is the length of a line drawn from the top surface at right angles to the base. The volume of a frustum of a pyramid can be found when the height, the top area, and

the base area are known. Let V = volume of frustum; $A_1 =$ area of top surface; $A_2 =$ area of base surface; and h = height perpendicular to base. Then:

$$V=\frac{h}{3}(A_1+A_2+\sqrt{A_1\times A_2}).$$

As an example, assume that a pyramid, having a height of 9 feet, has a base formed by a rectangle, the sides of which are 2 and 3 feet, respectively. This pyramid is cut off 4½ feet from the base, the upper part being removed. The sides of the rectangle forming the top surface of the frustum are, then, I and I½ foot long, respectively. Find the volume of the frustum.

Area of top =
$$A_1 = 1 \times 1\frac{1}{2} = 1\frac{1}{2}$$
 sq. ft.
Area of base = $A_2 = 2 \times 3 = 6$ sq. ft.

$$V = \frac{4.5}{3} (1.5 + 6 + \sqrt{1.5 \times 6}) = 1.5 (7.5 + \sqrt{9})$$

$$= 1.5 \times 10.5 = 15.75$$
 cubic feet.

Prismoidal Formula. — The prismoidal formula is a general formula by which the volume of any prism, pyramid, or frustum of a pyramid may be found.

 A_1 = area at one end of the body;

 A_2 = area at the other end;

 A_m = area of middle section between the two end surfaces;

h = height of body.

Then, volume V of the body is:

$$V = \frac{h}{6}(A_1 + 4A_m + A_2).$$

Wedge. — A solid body enclosed by a rectangular base surface, two trapezoids, and two triangles, is called a



wedge. The two trapezoids forming the side surfaces of the wedge may also be rectangles. Let V = volume of wedge, and a, b, c, and b be the dimensions indicated in Fig. 47. The height b is measured perpendic-

Fig. 47. The height h is measured perpular to the base surface. Then:

$$V=\frac{(2 a+\epsilon) bh}{6}.$$

Let a = 4 inches, b = 3 inches, and c = 5 inches. The height h = 4.5 inches. Find the volume.

$$V = \frac{(2 \ a + c) \ bh}{6} = \frac{(2 \times 4 + 5) \times 3 \times 4.5}{6}$$
$$= \frac{(8 + 5) \times 13.5}{6} = \frac{13 \times 13.5}{6} = \frac{175.5}{6} = 29.25 \text{ cu. in.}$$

Cylinder. — A solid body, as shown in Fig. 48, having circular and parallel end faces of equal size, is called a cylinder. The two parallel faces are called bases. The



height or altitude h of a cylinder is the distance between the bases measured at right angles to the base surfaces. The volume of a cylinder equals the area of the base multi-

plied by the height. The area of the base must, therefore, first be found before the volume can be obtained. Let V = volume of cylinder; S = area of cylinderical surface; d = diameter, and r = radius of cylinder; and h = height measured perpendicular to base. Then:

$$V = 3.1416 \, r^2 h = 0.7854 \, d^2 h.$$

 $S = 6.2832 \, rh = 3.1416 \, dh.$

Total area A of cylindrical surface and end surfaces:

$$A = 6.2832 r (r + h) = 3.1416 d (\frac{1}{2} d + h).$$

The diameter of a cylinder is 2½ inches. The length or

height is 20 inches. Find the volume and the area of the cylindrical surface S.

$$V = 0.7854 d^2h = 0.7854 \times 2\frac{1}{2} \times 20$$

= 0.7854 \times 6.25 \times 20 = 98.17 cubic inches.
 $S = 3.1416 dh = 3.1416 \times 2\frac{1}{2} \times 20 = 157.08 \text{ sq. in.}$

Portion of a Cylinder. - The volume of a portion of



a cylinder, cut off by an inclined plane as shown in Fig. 49, may be found by the following formulas. Let V = volume of portion of cylinder, S = area of cylindrical surface, and d, r, h₁, and h₂ be the dimensions

shown in Fig. 49. Then:

$$V = 1.5708 \, r^2 \, (h_1 + h_2) = 0.3927 \, d^2 \, (h_1 + h_2).$$

$$S = 3.1416 \, r \, (h_1 + h_2) = 1.5708 \, d \, (h_1 + h_2).$$

A cylinder 5 inches in diameter is cut off at an angle, as shown in the illustration. Dimension $h_1 = 6$, and $h_2 = 4$ inches. Find the volume and the area S of the cylindrical surface.

$$V = 0.3927 d^2 (h_1 + h_2) = 0.3927 \times 5^2 \times (6 + 4)$$

= 0.3927 × 25 × 10 = 98.175 cubic inches.
 $S = 1.5708 d (h_1 + h_2) = 1.5708 \times 5 \times 10$
= 78.54 square inches.

The volume of a portion of a cylinder so cut by an inclined plane that part of the circ



inclined plane that part of the circular base surface is removed also, as shown in Fig. 50, may be found as follows. Let V = volume of portion of cylinder, S = area of cylindrical surface, and the other

dimensions be as shown in Fig. 50. Then:

$$V = \left(\frac{2}{3}a^3 \pm b \times \text{area } ABC\right) \frac{h}{r \pm b}.$$

$$S = (ad \pm b \times \text{length of arc } ABC) \frac{h}{r + b}.$$

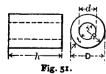
Use + when base area is larger, and - when base area is less than one-half the base circle.

Find the volume of a cylinder so cut off that line AC passes through the center of the base circle — that is, the base area is a half-circle. The diameter of the cylinder = 5 inches, and height h = 2 inches.

In this case, a = 2.5; b = 0; area $ABC = \frac{1}{2} \times 0.7854 \times 5^2 = 9.82$; r = 2.5.

$$V = \left(\frac{2}{3} \times 2.5^3 + 0 \times 9.82\right) \frac{2}{2.5 + 0} = \frac{2}{3} \times 15.625 \times 0.8$$

= 8.33 cubic inches.



Hollow Cylinder. — In a hollow cylinder, as shown in Fig. 51, let V = volume, and the other dimensions be as shown in the illustration. Then:

$$V = 3.1416 h (R^2 - r^2) = 0.7854 h (D^2 - d^2)$$

$$= 3.1416 ht (2 R - t) = 3.1416 ht (D - t)$$

$$= 3.1416 ht (2 r + t) = 3.1416 ht (d + t)$$

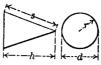
$$= 3.1416 ht (R + r) = 1.5708 ht (D + d).$$

A cylindrical shell, 28 inches high, is 36 inches in outside diameter, and 4 inches thick. Find its volume.

$$V = 3.1416 ht (D - t) = 3.1416 \times 28 \times 4 (36 - 4)$$

= 3.1416 × 28 × 4 × 32 = 11,259.5 cubic inches.

Cone. — A solid body having a circular base and the sides inclined so that they meet at a common vertex, the same as in a pyramid, is called a *cone*. (See Fig. 52.) If a



line is drawn from the vertex of the cone at *right angles* to the base, the length of this line is the altitude or height h of the cone. The volume of the cone equals the base area multiplied by one-third of the

height. It is, therefore, necessary to find the area of the base circle before the volume can be found.

Let V = volume of cone, A = area of conical surface, and the other dimensions be as shown in Fig. 52. Then:

$$V = \frac{3.1416 \, r^2 h}{3} = 1.0472 \, r^2 h = 0.2618 \, d^2 h.$$

$$A = 3.1416 \, r \sqrt{r^2 + h^2} = 3.1416 \, rs = 1.5708 \, ds.$$

$$s = \sqrt{r^2 + h^2} = \sqrt{\frac{d^2}{4} + h^2}.$$

Find the volume and area of the conical surface of a cone, the base of which is a circle of 6 inches diameter, and the height of which is 4 inches.

$$V = 0.2618 \, d^2h = 0.2618 \times 6^2 \times 4 = 0.2618 \times 36 \times 4$$
= 37.7 cubic inches.
$$A = 3.1416 \, r \sqrt{r^2 + h^2} = 3.1416 \times 3 \times \sqrt{3^2 + 4^2}$$
= 9.4248 \times \sqrt{25} = 47.124 square inches.

Frustum of Cone. — A frustum of a cone is shown in Fig. 53. It is a cone from which the top has been cut off,

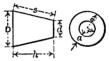


Fig. 53.

the top surface being a circle parallel to the base. The height h of a frustum of a cone is the length of a line drawn from the top surface at right angles to the base. The volume of a frustum of a cone can

be found when the diameters of the top and base circles and the height are known. Let V = volume of frustum of cone, $A = \text{area of conical surface, and the other dimensions be as indicated in Fig. 53. Then:$

$$V = 1.0472 h (R^2 + Rr + r^2) = 0.2618 h (D^2 + Dd + d^2).$$

$$A = 3.1416 s (R + r) = 1.5708 s (D + d).$$

$$a = R - r; s = \sqrt{a^2 + h^2} = \sqrt{(R - r)^2 + h^2}.$$

Find the volume of a frustum of a cone of the following dimensions: D = 8 inches; d = 4 inches; h = 5 inches.

$$V = 0.2618 \times 5 (8^2 + 8 \times 4 + 4^2)$$

= 0.2618 × 5 (64 + 32 + 16) = 0.2618 × 5 × 112
= 146.61 cubic inches.

Sphere. — The name sphere is applied to a solid body shaped like a ball or globe, that is, bounded by a surface



which at all points is at the same distance from a point inside of the sphere called its *center*. The diameter of a sphere is the length of a line drawn from a point on the surface through the center to the

opposite side. Let V = volume of sphere; A = area of spherical surface; d = diameter, and r = radius of sphere. Then:

$$V = \frac{4 \pi r^3}{3} = \frac{\pi d^3}{6} = 4.1888 \, r^3 = 0.5236 \, d^3.$$

$$A = 4 \pi r^2 = \pi d^2 = 12.5664 \, r^2 = 3.1416 \, d^2.$$

$$r = \sqrt[3]{\frac{3}{4} \frac{V}{\pi}} = 0.6204 \, \sqrt[4]{V}.$$

Find the volume and surface of a sphere 6.5 inches in diameter.

$$V = 0.5236 d^3 = 0.5236 \times 6.5^3$$

= 0.5236 × 6.5 × 6.5 × 6.5 = 143.79 cubic inches.
 $A = 3.1416 d^3 = 3.1416 \times 6.5^2 = 3.1416 \times 6.5 \times 6.5$
= 132.73 square inches.

The volume of a sphere is 64 cubic inches. Find its radius.

$$r = 0.6204 \sqrt[3]{64} = 0.6204 \times 4 = 2.4816$$
 inches.



Spherical Sector. - A spherical sector is a part of a sphere bounded by a section of the spherical surface and a cone, having its vertex at the center of the sphere, as shown in Fig. 55. Let V = volume of sector,

A = total area of conical and spherical surface, and c, h, and r be the dimensions indicated in the illustration. Then:

$$V = \frac{2 \pi r^2 h}{3} = 2.0944 r^2 h.$$

$$A = 3.1416 r (2 h + \frac{1}{2} c).$$

$$c = 2 \sqrt{h (2 r - h)}.$$

Find the volume of a sector of a sphere 6 inches in diameter, the height h of the sector being 1.5 inch. find length of chord c. — Here r = 3, and h = 1.5.

$$V = 2.0944 \, r^2 h = 2.0944 \times 3^2 \times 1.5$$

$$= 2.0944 \times 9 \times 1.5 = 28.27 \text{ cubic inches.}$$

$$c = 2\sqrt{h(2r - h)} = 2\sqrt{1.5(2 \times 3 - 1.5)}$$

$$= 2\sqrt{6.75} = 2 \times 2.598 = 5.196 \text{ square inches.}$$



Spherical Segment. - A spherical segment is a part of a sphere bounded by a portion of the spherical surface and a plane circular base, as shown in Fig. 56. Let V = volume of segment, A =area of spheri-

cal surface of segment, and c, h, and r be the dimensions shown in Fig. 56. Then:

$$V = 3.1416 h^{2} \left(r - \frac{h}{3} \right) = 3.1416 h \left(\frac{c^{2}}{8} + \frac{h^{2}}{6} \right)$$

$$A = 2 \pi r h = 6.2832 r h = 3.1416 \left(\frac{c^{2}}{4} + h^{2} \right)$$

$$c = 2 \sqrt{h (2r - h)}; \quad r = \frac{c^{2} + 4 h^{2}}{8 h}.$$

A segment of a sphere has the following dimensions: h = 2 inches; c = 5 inches. Find the volume V and the radius of the sphere of which the segment is a part.

$$V = 3.1416 \times 2 \times \left(\frac{5^2}{8} + \frac{2^2}{6}\right) = 6.2832 \times \left(\frac{25}{8} + \frac{4}{6}\right)$$
$$= 6.2832 \times 3.792 = 23.825 \text{ cubic inches.}$$
$$r = \frac{5^2 + 4 \times 2^2}{8 \times 2} = \frac{25 + 16}{16} = \frac{41}{16} = 2\frac{9}{16} \text{ inches.}$$

Spherical Zone. — A spherical zone is bounded by a part



of a spherical surface, and by two parallel circular bases, as shown in Fig. 57, where c_1 and c_2 are the diameters of the circular bases of the zone, and h its height.

Let V = volume of zone, A =area of spherical surface, and c_1 , c_2 , h, and r be the dimensions shown in Fig. 57. Then:

$$V = 0.5236 h \left(\frac{3 c_1^2}{4} + \frac{3 c_2^2}{4} + h^2 \right).$$

$$A = 2 \pi r h = 6.2832 r h.$$

$$r = \sqrt{\frac{c_2^2}{4} + \left(\frac{c_2^2 - c_1^2 - 4 h^2}{8 h} \right)^2}.$$

In a spherical zone, let $c_1 = 3$; $c_2 = 4$; and h = 1.5inch. Find the volume.

$$V = 0.5236 \times 1.5 \times \left(\frac{3 \times 3^2}{4} + \frac{3 \times 4^2}{4} + 1.5^2\right)$$

$$= 0.5236 \times 1.5 \times \left(\frac{27}{4} + \frac{48}{4} + 2.25\right)$$

$$= 0.5236 \times 1.5 \times 21 = 16.493 \text{ cubic inches.}$$

If a plane parallel with the end faces and passing through the center of the sphere intersects the zone, consider the zone as two zones, one zone being on each side of the center. Calculate the volume of each, and add these to find the total volume.

Spherical Wedge. — A spherical wedge is bounded by



part of a spherical surface and two plane surfaces intersecting each other at the center of the sphere. as shown in Fig. 58. Let V = volume of wedge, A = area of spherical surface, α = center angle in

degrees, and r = radius of sphere. Then:

$$V = \frac{\alpha}{360} \times \frac{4 \pi r^3}{3} = 0.0116 \, \alpha r^3.$$

$$A = \frac{\alpha}{360} \times 4 \pi r^2 = 0.0349 \, \alpha r^2.$$

Find the area of the spherical surface and the volume of a wedge of a sphere. The diameter of the sphere is 4 inches, and the center angle α is 45 degrees.

$$V = 0.0116 \times 45 \times 2^3 = 0.0116 \times 45 \times 8 = 4.176$$
 cu. in. $A = 0.0349 \times 45 \times 2^2 = 0.0349 \times 45 \times 4 = 6.282$ sq. in.



Hollow Sphere. - A hollow sphere is the shell formed between the surfaces of two spheres with the same center but different radii, as shown in Fig. 59. Let V = volume of shellof hollow sphere, and D, d, R, and r

be the dimensions shown in the illustration. Then:

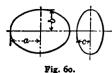
$$V = \frac{4\pi}{3} (R^3 - r^3) = 4.1888 (R^3 - r^3)$$
$$= \frac{\pi}{6} (D^3 - d^3) = 0.5236 (D^3 - d^3).$$

Find the volume of a hollow sphere, 8 inches in outside diameter, with a thickness of material of 1.5 inch.

Here
$$R = 4$$
; $r = 4 - 1.5 = 2.5$.
 $V = 4.1888 (4^3 - 2.5^3) = 4.1888 (64 - 15.625)$
 $= 4.1888 \times 48.375 = 202.63$ cubic inches.

Ellipsoid. — A solid body of such shape that all sections through its center are ellipses is called an ellipsoid, as shown in Fig. 60. Let V = volume; a, b, and c are half the axes in three planes at right angles to each other. Then:

$$V = \frac{4\pi}{3} abc = 4.1888 abc.$$



Spheroid. - If the ellipsoid is formed by an ellipse rotating about one of its axes, say, a, then b and c will be equal, and the body is called an ellipsoid of revolution or a spheroid. In this case:

$$V = 4.1888 \, ab^2$$
, and $A = \frac{4\pi}{\sqrt{2}} \, b \, \sqrt{a^2 + b^2}$,

in which A =area of surface of spheroid.

Find the volume and area of surface of a spheroid in which a = 5, and b = c = 1.5 inch.

$$V = 4.1888 \times 5 \times 1.5^2 = 4.1888 \times 5 \times 2.25$$

= 47.124 cubic inches.

$$A = \frac{4 \times 3.1416}{\sqrt{2}} \times 1.5 \times \sqrt{5^2 + 1.5^2}$$
$$= \frac{4 \times 3.1416}{1.414} \times 1.5 \times 5.22 = 69.57 \text{ square inches.}$$

Paraboloid. - A paraboloid is formed by the rotation

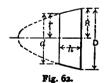
of a parabola about its own axis, as shown in Fig. 61. Let V = volume enclosed by paraboloidal surface and a plane surface at right angles to the axis of the paraboloid; r, h, and d are dimensions shown in the illustration. Then:

$$V = \frac{\pi}{2} r^2 h = 1.5708 r^2 h = \frac{\pi}{8} d^2 h = 0.3927 d^2 h.$$

Find the volume of a paraboloid in which h = 12 and d = 5 inches.

$$V = 0.3927 d^2h = 0.3927 \times 5^2 \times 12 = 0.3927 \times 25 \times 12$$

= 0.3927 × 300 = 117.81 cubic inches.



Paraboloidal Segment. - A paraboloidal segment is formed by a part of a paraboloidal surface and two plane surfaces at right angles to the axis of the paraboloid. Let V =volume of segment, the other dimen-

sions being as shown in Fig. 62. Then:

$$V = \frac{\pi}{2} h (R^2 + r^2) = 1.5708 h (R^2 + r^2)$$
$$= \frac{\pi}{8} h (D^2 + d^2) = 0.3927 h (D^2 + d^2).$$

Find the volume of a segment of a paraboloid in which D = 5 inches, d = 3 inches, and h = 6 inches.

$$V = 0.3927 h (D^2 + d^2) = 0.3927 \times 6 \times (5^2 + 3^2)$$

= 0.3927 \times 6 \times (25 + 9) = 0.3927 \times 6 \times 34

= 80.11 cubic inches.

Relation between Volume of Certain Solids. -- An interesting relation exists between the volumes of a cone,



a paraboloid, a sphere, and a cylinder. If d =base diameter and height of a cone, a paraboloid, and a cylinder, and the diameter of a sphere, as shown in Fig. 63, then the volumes of these bodies are to each other as below.

Cone: paraboloid: sphere: cylinder = $\frac{1}{3}$: $\frac{1}{2}$: $\frac{2}{3}$: 1.

Assume, as an example, that the diameter of the base of a cone, paraboloid, and cylinder is 2 inches, that the height is 2 inches, and that the diameter of a sphere is 2 inches. Then the volumes, written in formula form, are as below:

Cone Paraboloid Sphere
$$\frac{3.1416 \times 2^2 \times 2}{12} : \frac{3.1416 \times 2^2 \times 2}{8} : \frac{3.1416 \times 2^3}{6} : \frac{2.1416 \times 2^3}{6} : \frac{3.1416 \times 2^3}{4} = \frac{1}{3} : \frac{1}{2} : \frac{2}{3} : 1.$$



Torus. - The torus or ring is a circular or ring-shaped body having a circular cross-section, as shown in Fig. 64. Let V = volume of torus; A = area of its surface; D = itsmean diameter and R = its mean

radius; and d = diameter, and r = radius of cross-section.

$$V = 2 \pi^2 R r^2 = 19.739 R r^2 = \frac{\pi^2}{4} D d^2 = 2.4674 D d^2.$$

$$A = 4 \pi^2 R r = 39.478 R r = \pi^2 D d = 9.8696 D d.$$

Find the volume and area of surface of a torus in which d = 1.5 and D = 5 inches.

$$V = 2.4674 \times 5 \times 1.5^2 = 2.4674 \times 5 \times 2.25 = 27.76$$
 cu. in. $A = 9.8696 \times 5 \times 1.5 = 74.022$ square inches.



Barrel. - The exact volume of a barrel-shaped body cannot be obtained directly by a formula. The approximate volume V can be obtained, however, as below:

If the sides are bent to the arc of a circle:

$$V = \frac{1}{12} \pi h (2 D^2 + d^2) = 0.262 h (2 D^2 + d^2).$$

If the sides are bent to the arc of a parabola:

$$V = 0.209 h (2 D^2 + Dd + \frac{3}{4} d^2).$$

Find the approximate contents of a barrel, the inside dimensions of which are D = 24 inches; d = 20 inches; h = 48 inches.

$$V = 0.262 \,h\,(2\,D^2 + d^2) = 0.262 \times 48 \times (2 \times 24^2 + 20^2)$$

= 0.262 × 48 × (1152 + 400) = 0.262 × 48 × 1552
= 19,518 cubic inches.

Pappus or Guldinus Rules. - By means of these rules, the area of any surface of revolution and the volume of any solid of revolution may be found.

Rule for Surfaces. — The area of the surface swept out by the revolution of a line ABC (see Fig. 66) about the axis DE equals the length of the line multiplied by the length of the path of its center of gravity, P.

Approximate Method. — If the line is of such a shape that it is difficult to determine its center of gravity, then the line may be divided into a number of short sections, each of which may be considered as a straight line, and the approximate areas swept out by these different sections, as computed by the rule given, may be added to find the total area. The line must lie wholly on one side of the axis of revolution and must be in the same plane.

Rule for Solids. — The volume of a solid body formed by the revolution of a surface FGHJ about axis KL equals the area of the surface multiplied by the length of the path of its center of gravity. The surface must lie wholly on one side of the axis of revolution and in the same plane.

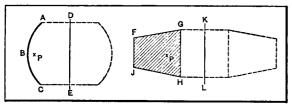


Fig. 66. Principle of Pappus Rule

By means of these rules the area and volume of a cylindrical ring or torus may be found, as an example. The torus is formed by a circle AB, Fig. 67, being rotated about axis CD. The center of gravity of the circle is at its center. Hence, with the dimensions given in the illustration, the length of the path of the center of gravity of the circle is $3.1416 \times 10 = 31.416$ inches. This multiplied by the length of the circumference of the circle, which is $3.1416 \times 3 = 9.4248$ inches, equals:

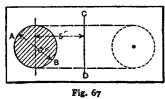
 $31.416 \times 9.4248 = 296.089$ square inches,

which is the area of the torus.

The volume equals the area of the circle, which is 0.7854 \times 9 = 7.0686 square inches, multiplied by the path of the center of gravity, which is 31.416, as before; hence,

volume = $7.0686 \times 31.416 = 222.067$ cubic inches.

Application to Surface of Irregular Body.—Fig. 68 is shown in order to give an example of the approximate method based on Guldinus' rule, that can be used for finding the area of a symmetrical body. In the illustration, the dimensions in common fractions are the known



dimensions; those in decimals are found by actual measurements on a figure drawn to scale. The method for finding the area is as follows: First separate such areas as are cylindrical, coni-

cal, or spherical, as these can be found by exact formulas. In the illustration, ABCD is a cylinder, the area of the surface of which can be easily found. The top area EF is simply a circular area, and can thus be computed separately. The remainder of the surface generated by rotating line AF about the axis GH is found by the approximate method explained in a previous section. From point A, set off equal distances on line AF. In the present case, each division indicated is $\frac{1}{2}$ inch long. From the central or middle point of each of these parts, draw a line at right angles to the axis of rotation GH, measure the length of these lines or diameters (the length of each is given in decimals), add all these lengths together

and multiply the sum by the length of one division set off on line AF (in this case, $\frac{1}{2}$ inch), and multiply this product by π . This gives the approximate area of the surface of revolution.

In setting off divisions $\frac{1}{6}$ inch long along line AF, the last division does not reach exactly to point F, but only to a point 0.03 inch below it. The part 0.03 inch high at the top of the cup can be considered as a cylinder of $\frac{1}{2}$ inch diameter and 0.03 inch height, the area of the cylindrical surface of which is easily computed. By adding the various surfaces together, the total surface of the cup is found as below:

Accuracy Obtainable. — In testing the accuracy of this method, the surface of a half-sphere 6 inches in diameter was found by dividing a great circle into parts $\frac{1}{4}$ inch long and finding the area by this graphical method. The exact area of this half-sphere is 56.55 square inches. The

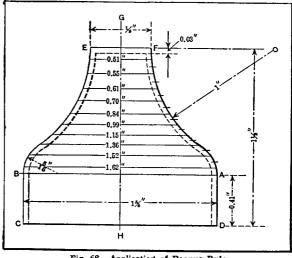


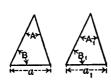
Fig. 68. Application of Pappus Rule

graphical method, using only an ordinary draftsman's scale, compass, and triangle, gave an area of 55.28 square inches, which may be considered fairly accurate for an approximate method. The half-sphere was selected for the test case because it presents one of the difficult shapes for the application of this method, as the curved outline merges from a vertical into a horizontal direction; the surface being convex throughout, the errors are also likely to be all in one direction. A more accurate result may be expected when part of the surface is convex and part concave.



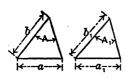
1. The sum of the three angles in a triangle always equals 180 degrees. Hence, if two angles are known, the third angle can always be found.

$$A + B + C = 180^{\circ}$$
.
 $A = 180^{\circ} - (B + C)$.
 $B = 180^{\circ} - (A + C)$.
 $C = 180^{\circ} - (A + B)$.



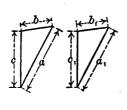
2. If one side and two angles in one triangle are equal to one side and similarly located angles in another triangle, then the remaining two sides and angle are also equal.

If $a = a_1$, $A = A_1$, and $B = B_1$, then the two other sides and the remaining angle are also equal.



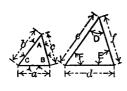
3. If two sides and one angle in one triangle are equal to two sides and a similarly located angle in another triangle, then the remaining side and angles are also equal; provided, however, that the triangles must either be both acute-angled triangles, both obtuse-angled triangles, or both right-angled triangles.

If $a = a_1$, $b = b_1$, and $A = A_1$, then the remaining side and angles are also equal, the triangles in this case being both acute-angled.



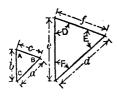
4. If the three sides in one triangle are equal to the three sides of another triangle, then the angles in the two triangles are also equal.

If $a = a_1$, $b = b_1$, and $c = c_1$, then the angles between the respective sides are also equal.



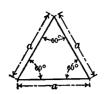
5. If the three sides of one triangle are proportional to corresponding sides in another triangle, then the triangles are called *similar*, and the angles in the one are equal to the angles in the other.

If a : b : c = d : e : f, then A = D, B = E, and C = F.



 If the angles in one triangle are equal to the angles of another triangle, then the triangles are similar and their corresponding sides are proportional.

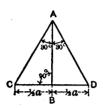
If A = D, B = E, and C = F, then a : b : c = d : e : f.



7. If the three sides in a triangle are equal—that is, if the triangle is equilateral—then the three angles are also equal.

Each of the three equal angles in an equilateral triangle is 60 degrees.

If the three angles in a triangle are equal, then the three sides are also equal.



8. A line which in an equilateral triangle bisects or divides any of the angles into two equal parts, bisects also the side opposite the angle and is at right angles to it.

If line AB divides angle CAD into two equal parts, it also divides line CD into two equal parts and is at right angles to it.



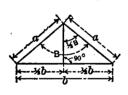
9. If two sides in a triangle are equal — that is, if the triangle is an *isosceles* triangle — then the angles opposite these sides are also equal.

If side a equals side b, then angle A equals angle B.

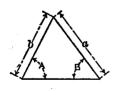


10. If two angles in a triangle are equal, then the sides opposite these angles are also equal.

If angles A and B are equal, then side a equals side b.

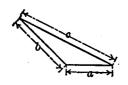


11. In an isosceles triangle, if a straight line is drawn from the point where the two equal sides meet, so that it bisects the third side or base of the triangle, then it also bisects the angle between the equal sides and is perpendicular to the base.



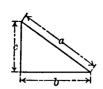
12. In every triangle, that angle is greater which is opposite a longer side. — In every triangle, that side is greater which is opposite a greater angle.

If a is longer than b, then angle A is greater than B. If angle A is greater than B, then side a is longer than b.



13. In every triangle, the sum of the lengths of two sides is always greater than the length of the third.

Side a + side b is always greater than side c.



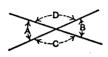
14. In a right-angled triangle, the square of the hypotenuse or the side opposite the right angle is equal to the sum of the squares on the two sides which form the right angle.

$$a^2 = b^2 + c^2$$
.



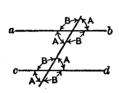
15. If one side of a triangle is produced, then the exterior angle is equal to the sum of the two interior opposite angles.

Angle D = angle A + angle B.



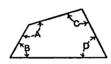
16. If two lines intersect, then the opposite angles formed by the intersecting lines are equal.

Angle
$$A = \text{angle } B$$
.
Angle $C = \text{angle } D$.



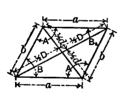
17. If a line intersects two parallel lines, then the corresponding angles formed by the intersecting line and the parallel lines are equal.

Lines ab and cd are parallel. Then all the angles designated A are equal, and all those designated B are equal.

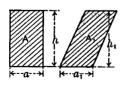


18. In any figure having four sides, the sum of the interior angles equals 360 degrees.

$$A + B + C + D = 360$$
 degrees.

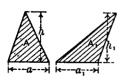


19. The sides which are opposite each other in a parallelogram are equal; the angles which are opposite each other are equal; the diagonal divides it into two equal parts. If two diagonals are drawn, they bisect each other.



20. The areas of two parallelograms which have equal base and equal height are equal.

If
$$a = a_1$$
 and $h = h_1$, then area $A = \text{area } A_1$.



21. The areas of triangles having equal base and equal height are equal.

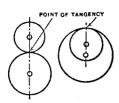
If
$$a = a_1$$
 and $h = h_1$, then area $A = \text{area } A_1$.



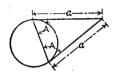
22. If a diameter of a circle is at right angles to a chord, then it bisects or divides the chord into-two equal parts.



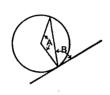
23. If a line is tangent to a circle, then it is also at right angles to a line drawn from the center of the circle to the point of tangency—that is, to a radial line through the point of tangency.



24. If two circles are tangent to each other, then the straight line which passes through the centers of the two circles must also pass through the point of tangency.

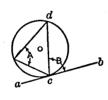


25. If from a point without a circle tangents are drawn to a circle, the two tangents are equal and make equal angles with the chord joining the points of tangency.



26. The angle between a tangent and a chord drawn from the point of tangency equals one-half the angle at the center subtended by the chord.

Angle $B = \frac{1}{2}$ angle A.



27. The angle between a tangent and a chord drawn from the point of tangency equals the angle at the periphery subtended by the chord.

Angle B, between tangent ab and chord cd, equals angle A subtended at the periphery by chord cd.



28. All angles having their vertex at the periphery of a circle and subtended by the same chord are equal.

Angles A, B, and C, all subtended by chord cd, are equal.



29. If an angle at the circumference of a circle, between two chords, is subtended by the same arc as the angle at the center, between two radii, then the angle at the circumference is equal to one-half of the angle at the center.

Angle $A = \frac{1}{2}$ angle B.

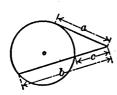


30. An angle subtended by a chord in a circular segment larger than one-half the circle is an acute angle — an angle less than 90 degrees. An angle subtended by a chord in a circular segment less than one-half the circle is an obtuse angle — an angle greater than 90 degrees.



31. If two chords intersect each other in a circle, then the rectangle of the segments of the one equals the rectangle of the segments of the other.

$$a \times b = c \times d$$
.



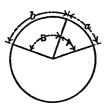
32. If from a point outside of a circle two lines are drawn, one of which intersects the circle while the other is tangent to it, then the rectangle contained by the total length of the intersecting line, and that part of it which is between the outside point and the periphery, equals the square of the tangent.

$$a^2 = b \times c$$
.



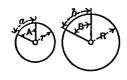
33. If a triangle is inscribed in a semi-circle, the angle opposite the diameter is a right (90-degree) angle.

All angles at the periphery of a circle, subtended by the diameter, are right (90-degree) angles.



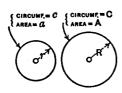
34. The length of circular arcs of the same circle are proportional to the corresponding angles at the center.

$$A:B=a:b.$$



35. The length of circular arcs having the same center angle are proportional to the length of the radii.

If
$$A = B$$
, then $a : b = r : R$.

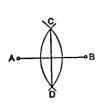


36. The circumferences of two circles are proportional to their radii.

The areas of two circles are proportional to the squares of their radii.

$$c: C = r: R.$$

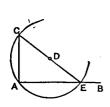
$$a:A=r^2:R^2.$$



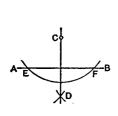
1. To divide a line AB into two equal parts: With the ends A and B as centers and a radius greater than one-half the line, draw circular arcs. Through the intersections C and D, draw line CD. This line divides AB into two equal parts and is also perpendicular to AB.



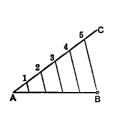
2. To draw a perpendicular to a straight line from a point A on that line: With A as a center and with any radius, draw circular arcs intersecting the given line at B and C. Then, with B and C as centers and a radius longer than AB, draw circular arcs intersecting at D. Line DA is perpendicular to BC at A.



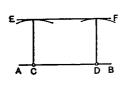
3. To draw a perpendicular line from a point A at the end of a line AB: With any point D, outside of the line AB, as a center, and with AD as a radius, draw a circular arc intersecting AB at E. Draw a line through E and D intersecting the arc at C; then join AC. This line is the required perpendicular.



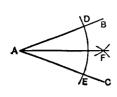
4. To draw a perpendicular to a line AB from a point C at a distance from it: With C as a center, draw a circular arc intersecting the given line at E and F. With E and F as centers, draw circular arcs with a radius longer than one-half the distance between E and F. These arcs intersect at D. Line CD is the required perpendicular.



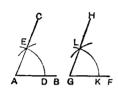
5. To divide a straight line AB into a number of equal parts: Let it be required to divide AB into five equal parts. Draw line AC at an angle with AB. Set off on AC five equal parts of any convenient length. Draw B 5 and then draw lines parallel with B 5 through the other division points on AC. The points where these lines intersect AB are the required division points.



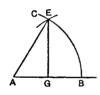
6. To draw a straight line parallel to a given line AB, at a given distance from it: With any points C and D on AB as centers, draw circular arcs with the given distance as radius. Line EF, drawn to touch the circular arcs, is the required parallel line.



7. To bisect or divide an angle BAC into two equal parts: With A as a center and any radius, draw arc DE. With D and E as centers, and a radius greater than one-half DE, draw circular arcs intersecting at F. Line AF divides the angle into two equal parts.

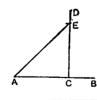


8. To draw an angle upon a line AB, equal to a given angle FGH: With point G as a center and with any radius, draw arc KL. With A as a center and with the same radius, draw arc DE. Make arc DE equal to KL and draw AC through E. Angle BAC then equals FGH.



9. To lay out a 60-degree angle: With A as a center and any radius, draw an arc BC. With point B as a center and AB as a radius, draw an arc intersecting at E the arc just drawn. EAB is a 60-degree angle.

A 30-degree angle may be obtained either by dividing a 60-degree angle into two equal parts, or by drawing a line EG perpendicular to AB. Angle AEG is then 30 degrees.



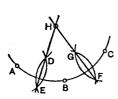
10. To draw a 45-degree angle: From point A on line AB, set off a distance AC. Draw the perpendicular DC and set off a distance CE equal to AC. Draw AE. Angle EAC is a 45-degree angle.



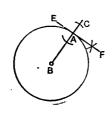
11. To draw an equilateral triangle, the length of the sides of which equals AB: With A and B as centers and AB as radius, draw circular arcs intersecting at C. Draw AC and BC. Then ABC is an equilateral triangle.



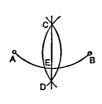
12. To draw a circular arc with a given radius through two given points A and B: With A and B as centers, and the given radius as radius, draw circular arcs intersecting at C. With C as a center, and the same radius, draw a circular arc through A and B.



or of an arc of a circle: Select three points on the periphery of the circle, as A, B, and C. With each of these points as a center and the same radius, describe arcs intersecting each other. Through the points of intersection, draw lines DE and FG. Point H where lines intersect is the center of the circle.



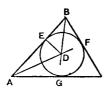
14. To draw a tangent to a circle from a given point on the circumference: Through the point of tangency A, draw a radial line BC. At point A, draw a line EF at right angles to BC. This line is the required tangent.



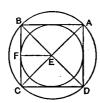
15. To divide a circular arc AB into two equal parts: With A and B as centers, and a radius larger than half the distance between A and B, draw circular arcs intersecting at C and D. Line CD divides arc AB into two equal parts at E.



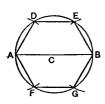
16. To describe a circle about a triangle: Divide the sides AB and AC into two equal parts, and from the division points E and F draw lines at right angles to the sides. These lines intersect at G. With G as a center and GA as a radius, draw circle ABC.



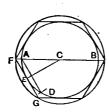
17. To inscribe a circle in a triangle: Bisect two of the angles, A and B, by lines intersecting at D. From D draw a line DE perpendicular to one of the sides, and, with DE as a radius, draw circle EFG.



18. To describe a circle about a square and to inscribe a circle in a square: The center of both the circumscribed and inscribed circle is located at the point E, where the two diagonals of the square intersect. The radius of the circumscribed circle is AE, and of the inscribed circle, EF.

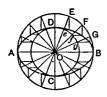


19. To inscribe a hexagon in a circle: Draw a diameter AB. With A and B as centers and with the radius of the circle as radius, describe circular arcs intersecting the given circle at D, E, F, and G. Draw lines AD, DE, etc., forming the required hexagon.

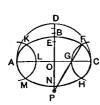


20. To describe a hexagon about a circle: Draw a diameter AB, and with A as a center and the radius of the circle as radius, cut the circumference of the given circle at D. Join AD and bisect it with radius CE. Through E, draw FG parallel to AD and intersecting line AB at F. With C as a center and CF as radius, draw a circle. Within this circle inscribe the hexagon, as in the preceding problem.

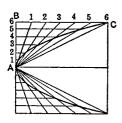
21. To describe an ellipse with the given axes AB and CD: Describe circles with O as a center and AB



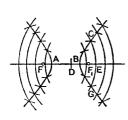
and CD as diameters. From a number of points, E, F, G, etc., on the outer circle, draw radii intersecting the inner circle at e, f, g. From E, F, and G, draw lines perpendicular to AB, and from e, f, and g draw lines parallel to AB. The intersections of these perpendicular and parallel lines are points on the curve of the ellipse.



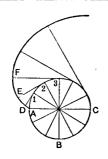
22. To construct an approximate ellipse by circular arcs: Let AC be the major axis and BN the minor. Draw half circle ADC with O as a center. Divide BD into three equal parts and set off BE equal to one of these parts. With A and C as centers and OE as radius, describe circular arcs KLM and FGH; with G and L as centers, and the same radius, describe arcs FCH and KAM. Through F and G, draw line FP, and with P as a center draw the arc FBK. Arc HNM is drawn in the same manner.



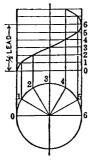
23. To construct a parabola: Divide line AB into a number of equal parts and divide BC into the same number of parts. From the division points on AB, draw horizontal lines. From the division points on BC, draw lines to point A. The points of intersection between lines drawn from points numbered alike are points on the parabola.



24. To construct a hyperbola: From focus F lay off a distance FDequal to the transverse axis, or the distance AB between the two branches of the curve. With F as a center and any distance FE greater than FB as a radius, describe a circular arc. Then with F_1 as a center and DE as a radius, describe arcs intersecting at C and G the arc just described. C and G are points on the hyperbola. Any number of points can be found in a similar manner.



25. To construct an involute: Divide the circumference of the base circle ABC into a number of equal parts. Through the division points 1, 2, 3, etc., draw tangents to the circle and make the lengths D1, E2, F3, etc., of these tangents equal to the actual length of the arcs A1, A2, A3, etc.



26. To construct a helix: Divide half the circumference of the cylinder on the surface of which the helix is to be described into a number of equal parts. Divide half the lead of the helix into the same number of equal parts. From the division points on the circle representing the cylinder, draw vertical lines, and from the division points on the lead, draw horizontal lines as shown. The intersections between lines numbered alike are points on the helix.

§ 35. The Parabola. Derivation of the Canonical Equation of the Parabola

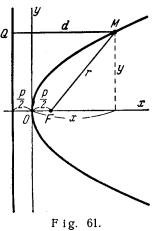
101. A parabola is the locus of points whose distance from a fixed point (called the focus) in the plane is equal to their distance from a fixed straight line (called the directrix and assumed not to pass through the focus).

It is customary to denote the focus of a parabola by the letter F, and the distance from the focus to the directrix by the

letter p. The quantity p is called the parameter of a parabola. The curve is shown in Fig. 61 (the details of the drawing are fully explained in the next few articles).

Note. In accordance with Art. 100, a parabola is said to have eccentricity $\varepsilon = 1$.

102. Let there be given a parabola (we assume that the parameter p is also given). Let us attach to the plane rectangular cartesian coordinate system, whose axes are specially chosen with respect to the given parabola; namely, let the x-axis be drawn through the focus perpendicular to the directrix,



the direction from the directrix to the focus adopted as positive on the x-axis, and the origin placed midway between the focus and the directrix (Fig. 61). We now proceed to derive the equation of the given parabola in this coordinate system.

Take an arbitrary point M in the plane and designate its coordinates as x and y. Let r denote the distance of the point M from the focus (r = FM), and d the distance of the point M from the directrix. The point M will lie on the given parabola if, and only if,

$$r = d. (1)$$

In order to obtain the desired equation, it is necessary to express the variables r and d in terms of the current coordinates x, y and to substitute these expressions in (1). Note that the coordinates of the focus F are $(\frac{p}{2}, 0)$; bearing this in mind and using formula (2) of Art. 18, we find

$$r = \sqrt{\left(x - \frac{p}{2}\right)^2 + y^2} \,. \tag{2}$$

Denote by Q the foot of the perpendicular dropped from M upon the directrix. The coordinates of the point Q will clearly be $\left(-\frac{p}{2}, y\right)$; hence, by formula (2) of Art. 18, we obtain

$$d = MQ = \sqrt{\left(x + \frac{p}{2}\right)^2 + (y - y)^2} = x + \frac{p}{2}$$
 (3)

(on extracting the root, we take $x+\frac{p}{2}$ with its original sign since $x+\frac{p}{2}$ is a positive number; this follows from the fact that the point M(x, y) must lie on that side of the directrix where the focus is situated, that is, we must have $x>-\frac{p}{2}$, whence $x+\frac{p}{2}>0$). Substituting expressions (2) and (3) for r and d in (1), we find

$$\sqrt{\left(x - \frac{p}{2}\right)^2 + y^2} = x + \frac{p}{2}.$$
 (4)

The coordinates of a point M(x, y) satisfy equation (4) if, and only if, the point M lies on the given parabola; accordingly, (4) is the equation of this parabola referred to the chosen coordinate system.

To reduce the equation of the parabola to a simpler form, we

square both members of (4), which gives

$$x^{2} - px + \frac{p^{2}}{4} + y^{2} = x^{2} + px + \frac{p^{2}}{4}.$$
 (5)

or

$$y^2 = 2px. (6)$$

We have derived equation (6) as a consequence of equation (4). It is easy to show that equation (4) may, in its turn, be derived as a consequence of (6). In fact, equation (5) is readily obtained from (6) by "retracing steps"; next, from (5) we get

$$\sqrt{\left(x-\frac{p}{2}\right)^2+y^2}=\pm\left(x+\frac{p}{2}\right).$$

It remains to show that, if x, y satisfy equation (6), then the plus sign is here the only sign to choose. But this is clear since, from (6), $x = \frac{y^2}{2p}$ and, consequently, $x \ge 0$, so that $x + \frac{p}{2}$ is a positive number. Thus, we have come back to equation (4). Since each of equations (4) and (6) is a consequence of the other, they are equivalent. We hence conclude that equation (6) is the equa-

tion of the parabola. This equation is called the canonical equation of the parabola.

103. The equation $y^2 = 2px$, which represents the parabola in a certain system of rectangular cartesian coordinates is an equation of the second degree; accordingly, the parabola is a curve of the second order.

§ 36. Discussion of the Shape of the Parabola

104. Let us analyse the equation

$$y^2 = 2px \tag{1}$$

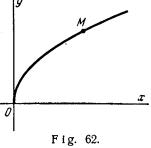
in order to form a clear idea of the shape of the parabola and thereby to show the correctness of its representation in Fig. 61.

Since equation (1) contains y only in an even power, the parabola represented by it is symmetrical with respect to the

axis Ox. It will therefore be sufficient to investigate only the portion of the parabola which lies in the upper halfplane. This portion is represented by the equation

$$y = +\sqrt{2px}. (2)$$

For negative values of x, equation (2) gives imaginary values of y. Consequently, no point of the parabola appears to the left of the axis Oy. For x = 0, we have y = 0. Hence the origin lies on the parabola and is its extreme "left" point. Equation (2)



shows that, as x increases from zero, y continually increases. The

equation also shows that, as $x \to +\infty$, $y \to +\infty$.

Thus, the variable point M(x, y), which traces the portion of the parabola under consideration, moves to the "right" and "upwards", starting from the origin and receding indefinitely from both the axis Oy (to the "right") and the axis Ox ("upwards"; see Fig. 62).

Note. The following two properties of the parabola are also of importance: (1) the direction of the parabola is perpendicular to the axis Ox in the point O(0, 0); (2) the portion of the parabola in the upper half-plane is convex "upwards". The graph in Fig. 62 has been drawn in accordance with these properties. Their proof will not, however, be given here, since the most natural methods for curve analysis of such kind are those furnished by the calculus.

105. Now that we have established the shape of the portion of the parabola lying in the upper half-plane, the determination of the shape of the entire parabola will present no difficulties; we have merely to reflect this portion of the curve in the axis Ox. The above-discussed Fig. 61 gives a general idea of the entire parabola represented by the equation

$$y^2 = 2px$$
.

Usually the axis of symmetry of a parabola is referred to simply as its axis (in the case under consideration, the axis of the parabola coincides with the axis Ox). The point where a parabola cuts its axis is called the vertex of the parabola (in our case, the vertex is coincident with the origin). The number p, that is, the parameter of a parabola, represents the distance between the focus and the directrix. The geometric meaning of the parameter p may also be described as follows. Take some definite value of the abscissa, say x = 1, and find from equation (1) the corresponding values of the ordinate: $y = \pm \sqrt{2p}$. We obtain two points of the parabola, $M_1(1, +\sqrt{2p})$ and $M_2(1, -\sqrt{2p})$ symmetric with respect to the axis; the distance between these points is equal to $2\sqrt{2p}$. Thus, $2\sqrt{2p}$ is the

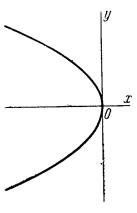


Fig. 63.

length of the chord perpendicular to the axis and one unit of length distant from the vertex. We see that the length $(=2\sqrt{2p})$ of this chord of the parabola increases with p. Consequently, the parameter p characterises the "spread" of a parabola, provided that this "spread" is measured perpendicular to the axis at a definite distance from the vertex.

106. The equation

$$y^2 = -2px \tag{3}$$

(where p is positive) may be reduced to the equation $y^2 = 2px$ by substituting -xfor x, that is, by a transformation of coordinates corresponding to a reversal

of the direction of the axis Ox. Hence, the equation $y^2 = -2px$ also represents a parabola whose axis is coincident with the axis Ox and whose vertex coincides with the origin; but this parabola is situated in the left half-plane, as shown in Fig. 63.

107. By analogy with the foregoing, we may assert that each of the equations

$$x^2 = 2py, \quad x^2 = -2py$$

(where p > 0) represents a parabola symmetric with respect to the axis Oy, with vertex at the origin (these equations, as well as equations (1) and (3), are referred to as the canonical equations of the parabola). A parabola represented by the equation $x^2 = 2py$ is said to open upwards; a parabola represented by

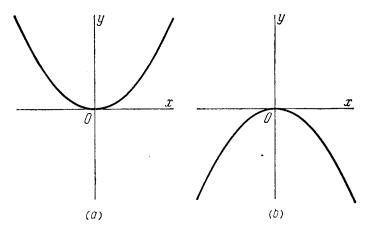


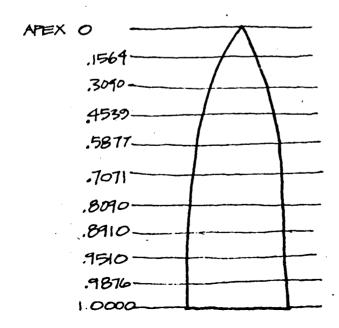
Fig. 64.

the equation $x^2 = -2py$ is said to open downwards (see Fig. 64 a and b, respectively); the use of these terms is natural and requires no further explanation.

Panel (gore) design for a hemispherical airhouse of any size:

- 1. Select your diameter and find the resulting circumference (3.1416 x diameter).
 - 2. Determine a maximum gore width that will go evenly into the circumference. This will also show the number of gores needed. Consider the available fabric widths when determining the maximum gore width.
 - 3. Determine the length of each gore (circumference ÷ 4
 - 4. To determine the detailed shape of the gore: First, divide the gore into 10 equal sections along its length. The tenth line will be the base.

Next, determine the width at each of these division lines by multiplying each of the following numbers times the maximum gore width found in step 2. Take the trouble to carry your figures out to 4 places and lay out your template carefully. Any error will be exagerated by the number of gores used.



Note: let a little extend below base

TRIANGULATION.

Triangulation is an application of the principles of trigonometry to the calculation of inaccessible lines and angles.

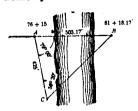


Fig. 1.

A common occasion for its use is illustrated in Fig. 1, where the line of survey crosses a stream too wide and deep for actual measurement. Set two points A and B on line, one on each side of the stream. Estimate roughly the distance AB. Suppose the estimate is 425 ft. Set another point C, making the distance AC equal to the estimated

distance AB = 425 ft. Set the transit at A and measure the angle BAC =say, 79°00′. Next set up at the point C and measure the angle ACB =say, 56°20′. The angle ABC is then determined by subtracting the sum of the angles A and C from 180°; thus, 79°00′ + 56°20′ = 135°20′; 180°00′ - 135°20′ = 44°40′ = the angle ABC. We now have a side and three angles of a triangle given, to find the other two sides AB and CB. In trigonometry, it is demonstrated that, in any triangle the sines of the angles are proportional to the lengths of the sides opposite to them. In other words, $\sin A : \sin B = BC : AC$; or, $\sin A : \sin C = BC : AB$, and $\sin B : \sin C = AC : AB$.

```
Hence, we have \sin 44^{\circ} 40' : \sin 56^{\circ} 20' = 425 : \text{side } A B;

\sin 56^{\circ} 20' = .83228;

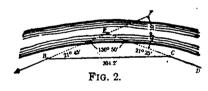
.83228 \times 425 = 353.719;

\sin^{\circ} 44^{\circ} 40' = .70298;

353.719 + .70298 = 503.17 \text{ ft. } = \text{side } A B.
```

Adding this distance to 76 + 15, the station of the point A, we have 81 + 18.17, the station at B.

Another case is the following: Two tangents, A B and CD (see Fig. 2), which are to be united by a curve, meet at some inaccessible point E. Tangents are the straight portions of a



line of railroad. The angle CEF, which the tangents make with each other, and the distances BE and CE are required. Two points A and B of the tangent

AB, and two points C and D of the tangent CD, being carefully located, set the transit at B, and backsighting to A, measure the angle $EBC=21^{\circ}45'$; set up at C, and, backsighting to D, measure the angle $ECB=21^{\circ}25'$. Measure the side BC=304.2 ft.

Angle CEF being an exterior angle of triangle EBC equials sum of EBC and $ECB = 21^{\circ}45' + 21^{\circ}25' = 43^{\circ}10'$; angle $BEC = 180^{\circ} - CEF = 136^{\circ}50'$. From trigonometry, we have:

```
\sin 136^{\circ} 50' : \sin 21^{\circ} 45' = 304.2 \text{ ft.} : CE;

\sin 21^{\circ} 45' = .37056;

.37056 \times 304.2 = 112.724352;

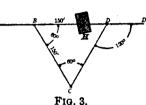
\sin 136^{\circ} 50' = .68412;

\operatorname{side} CE = 112.724352 + .68412 = 164.77 \text{ ft.}
```

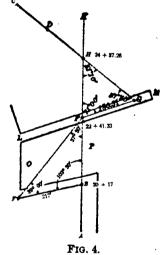
Again, we find BE by the following proportion: $\sin 136^{\circ} 50' : \sin 21^{\circ} 25' = 304.2 : \text{side } BE;$ $\sin 21^{\circ} 25' = .36515;$ $.36515 \times 304.2 = 111.07863;$ $\sin 136^{\circ} 50' = .68412;$ $\sin BE = 111.07863 + .68412 = 162.36 \text{ ft.}$

A building H, Fig. 3, lies directly in the path of the line AB, which must be produced beyond H. Set a plug at B,

and then turn an angle DBC = 60°. Set a plug at C in the line BC, at a suitable distance from B, say, 150 ft. Set up at C, and turn an angle $BCD = 60^\circ$, and set a plug at D, 150 ft. from C. The point D will be in the prolongation of AB. Then, set up at D, and backsighting to



C, turn the angle $CDD' = 120^{\circ}$. DD' will be the line



required, and the distance BD will be 150 ft., since BCD is an equilateral triangle.

A B and CD, Fig. 4, are tangents intersecting at some inaccessible point H. The line AB crosses a dock OP, too wide for direct measurement, and the wharf LM. F is a point on the line AB at the wharf crossing. It is required to find the distance BH and the angle FHG. At B, an angle of 103° 30' is turned to the left and the point E set 217' from B = to the estimated distance BF. Setting up at E. the angle BEF is found to be 39° 00'.

Whence, we find the angle $BFE = 180^{\circ} - (103^{\circ} 30' + 39^{\circ}) = 37^{\circ} 30'$.

From trigonometry, we have

sin 37° 30': sin 39° 00' = 217 ft.: side BF; sin 39° 00' = .62932; .62932 × 217 = 136.56244; sin 37° 30' = .60876; side BF = 136.56244 ÷ .60876 = 224.33 ft.

Whence, we find station F to be 20 + 17 + 224.33 = 22 + 41.33. Set up at F and turn an angle $HFG = 71^{\circ}00'$ and set up at a point G where the line CD prolonged intersects FG. Measure the angle $FGH = 57^{\circ}50'$, and the side FG = 180.3. The angle $FHG = 180^{\circ} - (71^{\circ} + 57^{\circ}50') = 51^{\circ}10'$. From trigonometry we have

 $\sin 51^{\circ}10' : \sin 57^{\circ}50' = 180.3 : \text{side } FH.$

Sin 57° 50' = .84650; .84650 × 180.3 = 152.62395; sin 51° 10' = .77897; side FH = 152.62395 + .77897 = 195.93 ft.; whence we find station H to be 24 + 37.26.

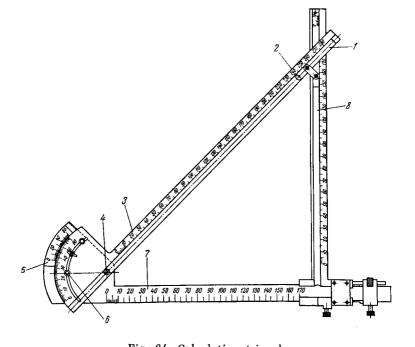


Fig. 64. Calculating triangle:

1-slide; 2-screw; 3-scale of hypotenuse rule; 4 and 6-set screws
5-vernier; 7 and 8-cathetuses

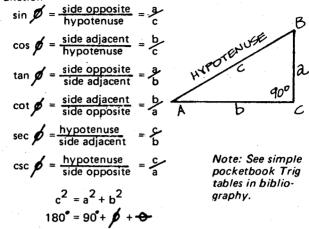


RIGHT-ANGLED TRIGONOMETRIC FUNCTIONS

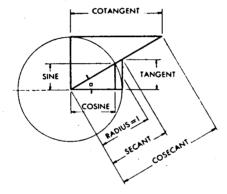
Right-angled trigonometric functions:

The trig functions are the ratios of sides of right triangles.

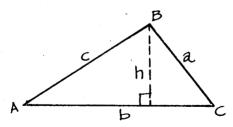




The trigonometric functions may be found graphically with the aid of the following diagram:



OBLIQUE TRIANGLE TRIGONOMETRIC FUNCTIONS



Law of sines:

Lengths of the sides of a triangle are proportional to the sines of the angles opposite them:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Law of cosines:

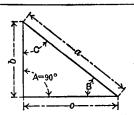
The square of the length of a side of a triangle equals the sum of the squares of the lengths of the other two sides minus twice the product of these two sides times the cosines of the angle between them.

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$

 $b^{2} = a^{2} + c^{2} - 2ac \cos B$
 $c^{2'} = a^{2} + b^{2} - 2ab \cos C$

Solving Right-angled Triangles

Formulas

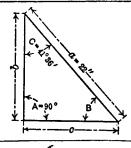


As shown in the illustration, the sides of the right-angled triangle are designated a, b, and c. The angles opposite each of these sides are designated A, B, and C, respectively.

Angle A, opposite the hypotenuse a, is the right angle, and is, therefore, always one of the known quantities.

| Sides and Angles Known | Formulas i | for Sides and Angles to | be Found |
|------------------------|------------------------|-------------------------|----------------------|
| Sides a and b | $c = \sqrt{a^2 - b^2}$ | $\sin B = \frac{b}{a}$ | $C = 90^{\circ} - B$ |
| Sides a and c | $b = \sqrt{a^2 - c^2}$ | $\sin C = \frac{c}{a}$ | B = 90° - C |
| Sides b and c | $a=\sqrt{b^2+c^2}$ | $\tan B = \frac{b}{c}$ | C = 90° - B |
| Side a; angle B | $b = a \times \sin B$ | $c = a \times \cos B$ | $C = 90^{\circ} - B$ |
| Side a; angle C | $b = a \times \cos C$ | $c = a \times \sin C$ | B = 90° - C |
| Side b; angle B | $a = \frac{b}{\sin B}$ | $c = b \times \cot B$ | $C = 90^{\circ} - B$ |
| Side b; angle C | $a = \frac{b}{\cos C}$ | $c = b \times \tan C$ | B = 90° - C |
| Side c; angle B | $a = \frac{c}{\cos B}$ | $b = c \times \tan B$ | C = 90° - B |
| Side c; angle C | $a = \frac{c}{\sin C}$ | $b = c \times \cot C$ | $B = 90^{\circ} - C$ |





Sides and angles known:

a = 22 inches; C = 41 degrees 36 minutes. Then, by the formulas given herewith:

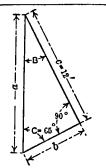
$$b = a \times \cos C = 22 \times \cos 41^{\circ} 36' = 22 \times 0.74780$$

= 16.4516 inches.

$$c = a \times \sin C = 22 \times \sin 41^{\circ} 36' = 22 \times 0.66393$$

= 14.6065 inches.

$$B = 90^{\circ} - 41^{\circ} 36' = 48^{\circ} 24'.$$



Sides and angles known:

$$c = 12$$
 feet; $C = 65$ degrees.

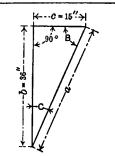
Then, by the formulas:

$$a = \frac{c}{\sin C} = \frac{12}{\sin 65^{\circ}} = \frac{12}{0.90631} = 13.2405$$
 feet.

$$b = c \times \cot C = 12 \times \cot 65^{\circ} = 12 \times 0.46631$$

= 5.5957 feet.

$$B = 90^{\circ} - 65^{\circ} = 25^{\circ}.$$



Sides known:

$$b = 36$$
 inches; $c = 15$ inches.

Then, by the formulas:

$$a = \sqrt{b^2 + c^2} = \sqrt{36^2 + 15^2} = \sqrt{1296 + 225}$$

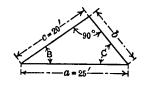
$$= \sqrt{1521} = 39 \text{ inches.}$$

$$\tan B = \frac{b}{c} = \frac{36}{15} = 2.4.$$

$$\tan B = \frac{1}{c} = \frac{30}{15} = 2.4.$$

$$B = 67^{\circ} 23'.$$

 $C = 90^{\circ} - 67^{\circ} 23' = 22^{\circ} 37'.$



Sides known:

Hence,

$$a = 25$$
 feet; $c = 20$ feet.

From the formulas:

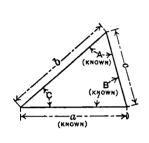
$$b = \sqrt{a^2 - c^2} = \sqrt{25^2 - 20^2} = \sqrt{625 - 400}$$
$$= \sqrt{225} = 15 \text{ feet.}$$

$$\sin C = \frac{c}{a} = \frac{20}{25} = 0.8.$$

Hence,

$$C = 53^{\circ} 8'$$
.
 $B = 90^{\circ} - 53^{\circ} 8' = 36^{\circ} 52'$.

Formulas



One side and two angles known.

Call the known side a, the angle opposite it A, and the other known angle B. Then:

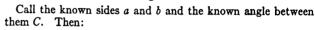
$$C = 180^{\circ} - (A+B).$$

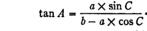
$$b = \frac{a \times \sin B}{\sin A} \cdot \qquad c = \frac{a \times \sin C}{\sin A} \cdot$$

Area =
$$\frac{a \times b \times \sin C}{2}$$
.

If angles B and C are given, but not A, then $A = 180^{\circ} - (B+C)$, the other formulas being the same.





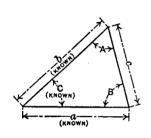


$$B = 180^{\circ} - (A + C). \quad c = \frac{a \times \sin C}{\sin A}.$$

Side c may also be found directly as below:

$$c = \sqrt{a^2 + b^2 - 2 ab \times \cos C}.$$

Area =
$$\frac{a \times b \times \sin C}{2}$$
.



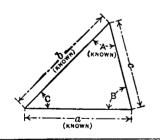
Two sides and the angle opposite one of the sides known.

Call the known angle A, the side opposite it a, and the other known side b. Then:

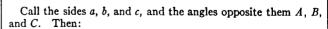
$$\sin B = \frac{b \times \sin A}{a} \cdot C = 180^{\circ} - (A + B).$$

$$c = \frac{a \times \sin C}{\sin A}$$
.

Area =
$$\frac{a \times b \times \sin C}{c}$$
.



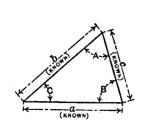
All three sides known.



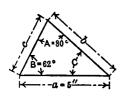
$$\cos A = \frac{b^2 + c^2 - a^2}{2 bc}.$$

$$\sin B = \frac{b \times \sin A}{a} \cdot C = 180^{\circ} - (A + B).$$

Area =
$$\frac{a \times b \times \sin C}{a}$$
.



Examples



Sides and angles known:

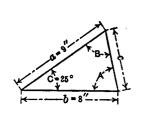
Then, by the formulas opposite:

$$C = 180^{\circ} - (80^{\circ} + 62^{\circ}) = 180^{\circ} - 142^{\circ} = 38^{\circ}.$$

$$b = \frac{a \times \sin B}{\sin A} = \frac{5 \times \sin 62^{\circ}}{\sin 80^{\circ}} = \frac{5 \times 0.88295}{0.98481} = 4.483 \text{ inches.}$$

a = 5 inches; A = 80 degrees; B = 62 degrees.

$$c = \frac{a \times \sin C}{\sin A} = \frac{5 \times \sin 38^{\circ}}{\sin 80^{\circ}} = \frac{5 \times 0.61566}{0.98481} = 3.126 \text{ inches.}$$

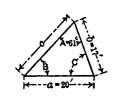


Sides and angles known:

$$a = 9$$
 inches; $b = 8$ inches; $C = 35$ degrees.

$$\tan A = \frac{a \times \sin C}{b - a \times \cos C} = \frac{9 \times \sin 35^{\circ}}{8 - 9 \times \cos 35^{\circ}}$$
$$= \frac{9 \times 0.57358}{8 - 9 \times 0.81915} = \frac{5.16222}{0.62765} = 8.22468.$$

Hence,
$$A = 83^{\circ} 4'$$
.
 $B = 180^{\circ} - (A + C) = 180^{\circ} - 118^{\circ} 4' = 61^{\circ} 56'$.
 $c = \frac{a \times \sin C}{\sin A} = \frac{9 \times 0.57358}{0.99269} = 5.2$ inches.



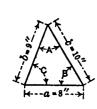
Sides and angles known:

$$a = 20$$
 feet; $b = 17$ feet; $A = 61$ degrees.
 $\sin B = \frac{b \times \sin A}{a} = \frac{17 \times \sin 61^{\circ}}{20}$

$$= \frac{17 \times 0.87462}{20} = 0.74343.$$

Hence,
$$B = 48^{\circ} \text{ I'}$$
.
 $C = 180^{\circ} - (A + B) = 180^{\circ} - 109^{\circ} \text{ I'} = 70^{\circ} 59'$.

$$c = \frac{a \times \sin C}{\sin A} = \frac{20 \times \sin 70^{\circ} 59'}{\sin 61^{\circ}} = \frac{20 \times 0.94542}{0.87462} = 21.62 \text{ feet.}$$



Sides known: a = 8 inches; b = 9 inches; c = 10 inches.

$$b^2 + c^2 - a^2$$
 $9^2 + 10^2 - 8^2$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc} = \frac{9^2 + 10^2 - 8^2}{2 \times 9 \times 10}$$
$$= \frac{81 + 100 - 64}{180} = \frac{117}{180} = 0.65000.$$

Hence,
$$A = 49^{\circ} 27'$$
.

$$\sin B = \frac{b \times \sin A}{a} = \frac{9 \times 0.75984}{8} = 0.85482.$$

Hence,
$$B = 58^{\circ} 44'$$
.
 $C = 180^{\circ} - (A + B) = 180^{\circ} - 108^{\circ} 11' = 71^{\circ} 49'$.

| | o' | 6' | 12' | 18' | 24' | 30' | 36′ | 42' | 48' | 54' | | Т | | AD | | |
|----------|-----------------|--------------|--------------|--------------|--------------|--------------|---------------|--------------|--------------|--------------|------|--|--------|----|----------|----------|
| х | | | | | | | | | | | ₫ | <u> </u> | | AD | | |
| | 0°.0 | 00.1 | 00.2 | 00.3 | 00.4 | 00.5 | 00.6 | 00.7 | 00.8 | 00.9 | | 1' | 2' | 3' | 4' | 5′ |
| oo | 0.0000 | 0017 | 0035 | 0052 | | 0087 | 0105 | 0122 | 0140 | 0157 | 18 | 3 | 6 | 9 | 12 | 15 |
| 1 1 | ·0175 | 0192 | 0209 | 0227 | 0244 | | 0279 | 0297 | 0314 | 0332 | | 3 | 6 | 9 | 12 | 15 |
| 2 3 | ·0349 ·0523 | 0366 0541 | 0384 0558 | 0401 0576 | 0419 0593 | 0436 0610 | 0454 0628 | 0471 0645 | 0488 0663 | 0506 0680 | | 3 | 6 | 9 | 12 | 15 |
| 4 | 0698 | 0715 | 0732 | 0750 | 0767 | 07B5 | 0802 | 0819 | 0837 | 0854 | | 3 | 6 | 9 | 12 12 | 15 14 |
| 5 | 0.0872 | 0889 | 0906 | 0924 | 0941 | 0958 | 0976 | 0993 | 1011 | 1028 | | 3 | 6 | 9 | 12 | 14 |
| 6 | -1045 | 1063 | 10B0 | 1097 | 1115 | 1132 | 1149 | 1167 | 1184 | 1201 | 1 | 3 | 6 | 9 | 12 | 14 |
| 7 | 1219 | 1236 | 1253 | 1271 | 1288 | 1305 | 1323 | 1340 | 1357 | 1374 | 1 | 3 | 6 | 9 | 12 | 14 |
| 8 | ·1392 ·1564 | 1409 | 1426 1599 | 1444 1616 | 1461 1633 | 1478 1650 | 1495 1668 | 1513 1685 | 1530 1702 | 1547 1719 | 1 | 3 | 6 | 9 | 11 | 14 |
| - | | | | | | | | | | 1713 | | ³ | 0 | 9 | 11 | 14 |
| 10 | 0.1736 | | 1771 | 1788 1959 | 1805 | 1822 1994 | 1840 | 1857 | 1874 | 1891 | | 3 | 6 | 9 | 11 | 14 |
| 11 | ·1908 ·2079 | 1925 2096 | 1942 2113 | 2130 | 1977 2147 | 2164 | 2011 2181 | 2028 2198 | 2045 2215 | 2062 2233 | 17 | 3 | 6 | 9 | 11 | 14 |
| 13 | 2250 | 2267 | 2284 | 2300 | 2317 | 2334 | 2351 | 2368 | 2385 | 2402 | 1'' | 3 | 6 | 9 | 11 | 14 |
| 14 | ·2419 | 2436 | 2453 | 2470 | 2487 | 2504 | 2521 | 2538 | 2554 | 2571 | | š | 6 | B | 11 | 14 |
| 15 | 0.2588 | 2605 | 2622 | 2639 | 2656 | 2672 | 2689 | 2706 | 2723 | 2740 | | 3 | 6 | 8 | 11 | 14 |
| 16 | . •2756 | 2773 | 2790 | 2807 | 2823 | 2840 | 2857 | 2874 | 2890 | 2907 | | 3 | 6 | 8 | 11 | 14 |
| 17 | -2924 | 2940 | 2957 | 2974 | 2990 | 3007 | 3024 | 3040 | 3057 | 3074 | 1 | 3 | 6 | 8 | 11 | 14 |
| 18 19 | -3090 -3256 | 3107 3272 | 3123 3289 | 3140 3305 | 3156 3322 | 3173 3338 | 3190 3355 | 3206 | 3223 3387 | 3239 | | 3 | 6 | 8 | 11 | 14 |
| | | - | | | | | | | | 3404 | | 3 | 5 | 8 | 11 | 14 |
| 20 | 0.3420 | 3437 | 3453 | 3469 | 3486 | 3502 | 3518 | 3535 | 3551 | 3567 | | 3 | 5 | 8 | 11 | 14 |
| 21 | ·3584 ·3746 | 3600 | 3616 3778 | 3633 3795 | 3649 3811 | 3665 3827 | 3681 3843 | 3697 3859 | 3714 | 3730 | 1 | 3 | 5 | 8 | 11 | 14 |
| 23 | 3907 | 3923 | 3939 | 3955 | 3971 | 3987 | 4003 | 4019 | 3875 4035 | 3891 4051 | 16 | 3 | 5 5 | 8 | 11 11 | 13 |
| 24 | -4067 | 4083 | 4099 | 4115 | 4131 | 4147 | 4163 | 4179 | 4195 | 4210 | `` | 3 | 5 | 8 | 11 | 13 |
| 25 | 0-4226 | 4242 | 4258 | 4274 | 4289 | 4305 | 4321 | 4337 | 4352 | 4368 | | 3 | 5 | 8 | 11 | 13 |
| 26 | 4384 | 4399 | 4415 | 4431 | 4446 | 4462 | 4478 | 4493 | 4509 | 4524 | 1 | 3 | 5 | 8 | 10 | 13 |
| 27 | ·4540 ·4695 | 4555 4710 | 4571 4726 | 4586 4741 | 4602 4756 | 4617 4772 | 4633 4787 | 4648 | 4664 | 4679 | | 3 | 5 | 8 | 10 | 13 |
| 29 | 4848 | 4863 | 4879 | 4894 | 4909 | 4924 | 4939 | 4802 4955 | 4818 4970 | 4833 4985 | | 3 | 5 5 | 8 | 10 10 | 13 |
| 30 | 0.5000 | 5015 | 5030 | 5045 | 5060 | 5075 | 5090 | 5105 | 5120 | 5135 | 15 | 3 | 5 | 8 | 10 | 13 |
| 31 | ·5150 | | 5180 | 5195 | 5210 | 5225 | 5240 | 5255 | 5270 | 5284 | 1 " | 2 | 5 | 7 | 10 | 12 |
| 32 | -5299 | 5314 | | 5344 | 5358 | 5373 | 5388 | 5402 | 5417 | 5432 | | 2 | 5 | 7 | 10 | 12 |
| 33 | -5446 | 5461 | 5476 | 5490 | 5505 | 5519 | 5534 | 5548 | 55 63 | 5577 | Į į | 2 | 5 | 7 | 10 | 12 |
| 34 | -5592 | 5606 | 5621 | 5635 | 5650 | 5664 | 5678 | 5693 | 5707 | 5721 | | 2 | 5 | 7 | 10 | 12 |
| 35 | 0.5736 | 5750 | 5764 | 5779 | 5793 | 5807 | 5821 | 5835 | 5850 | 5864 | | 2 | 5 | 7 | 9 | 12 |
| 3B 37 | ·5878 ·6018 | 5892 6032 | 5906 6046 | 5920 6060 | 5934 6074 | 5948 6088 | 5962 | 5976 | 5990 | 6004 | 14 | 2 | 5 | 7 | 9 | 12 |
| 37 | ·6018 | 6170 | 6184 | 6198 | 6211 | 6225 | 6101 6239 | 6115 6252 | 6129 6266 | 6143 6280 | | 2 2 | 5 5 | 7 | 9 | 12 |
| 39 | -6293 | 6307 | | 6334 | 6347 | 6361 | 6374 | 6388 | 6401 | 6414 | | 2 | 4 | 7 | 9 | 11 11 |
| 40 | 0-6428 | 6441 | 6455 | 6468 | 6481 | 6494 | 6508 | 6521 | 6534 | 6547 | | 2 | 4 | 7 | 9 | 11 |
| 41 | ·6561 | 6574 | 6587 | 6600 | 6613 | 6626 | 6639 | 6652 | 6665 | 6678 | 13 | 2 | 4 | ź | 9 | 11 |
| 42 | ·6691 | 6704 | 6717 | 6730 | 6743 | 6756 | 6769 | 6782 | 6794 | 6807 | | 2 | 4 | 6 | 9 | 11 |
| 43 | ·6820 ·6947 | 6833 6959 | 6845 6972 | 6858 6984 | 6871 6997 | 6884 7009 | 6896 7022 | 6909 7034 | 6921 7046 | 6934 7059 | | 2 | 4 | ô | 8 | 11 |
| ' | 1 | | | | | | | | | | | | 4 | 6 | 8 | 10 |
| 45 | 0·7071 ·7193 | 7083 7206 | 7096 7218 | 7108 7230 | 7120 | 7133 7254 | 7145 | 7157 | 7169 | 7181 | ا ۱۰ | 2 | 4 | 6 | 8 | 10 |
| 46 | ·7193 | 7325 | 7337 | 7230 7349 | 7361 | 7373 | 7266 7385 | 7278 7396 | 7290 7408 | 7302 7420 | 12 | 2 | 4 | 6 | 8 | 10 |
| 48 | ·7431 | 7443 | 7455 | 7466 | 747B | 7490 | 75 0 1 | 7513 | 7524 | 7536 | | 2 | 4 | 6 | 8 | 10 10 |
| 49 | 0.7547 | 7559 | 7570 | 7581 | 7593 | 7604 | 7615 | 7627 | 7638 | 7649 | | 2 | 4 | 6 | 8 | 9 |
| | <u> </u> | L | | | I | | | <u></u> | | | | ــــــــــــــــــــــــــــــــــــــ | _ | | | لــــــا |

| | | | | | | | | | | | , | | | | | _ |
|----------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----|-----|----|-----|----------|---|
| x | 0' | 6′ | 12' | 18′ | 24′ | 30′ | 36′ | 42' | 48' | 54′ | ⊿ | | _/ | ADI | <u> </u> | |
| ^ | 00.0 | 00.1 | 00-2 | 00-3 | 00.4 | 00.5 | 00.6 | 00.7 | 00.8 | 00.9 | 4 | 1 | 2 | 3′ | 4 | 5 |
| 500 | 0.7660 | 7672 | 7683 | 7694 | 7705 | 7716 | 7727 | 7738 | 7749 | 7760 | | 2 | 4 | 6 | 7 | 9 |
| 51 | -7771 | 7782 | 7793 | 7804 | 7815 | 7826 | 7837 | 7848 | 7859 | 7869 | 11 | 2 | 4 | 5 | 7 | 9 |
| 52 | -7880 | 7891 | 7902 | 7912 | 7923 | 7934 | 7944 | 7955 | 7965 | 7976 | | 2 | 4 | 5 | 7 | 9 |
| 53 | ·7986 | 7997 | 8007 | 8018 | 8028 | 8039 | 8049 | 8059 | 8070 | 8080 | | 2 | 3 | 5 | 7 | 9 |
| 54 | -8090 | 8100 | 8111 | 8121 | 8131 | 8141 | 8151 | 8161 | 8171 | 8181 | 10 | 2 | 3 | 5 | 7 | 8 |
| 55 | 0-8192 | 8202 | 8211 | 8221 | 8231 | 8241 | 8251 | 8261 | 8271 | 8281 | | 2 | 3 | 5 | 7 | 8 |
| 56 | -8290 | 8300 | 8310 | 8320 | 8329 | 8339 | 8348 | 8358 | 8368 | 8377 | 1 | 2 | 3 | 5 | 6 | 8 |
| 57 | -8387 | 8396 | 8406 | 8415 | 8425 | 8434 | 8443 | 8453 | 8462 | 8471 | ١. | 2 | 3 | 5 | 6 | 8 |
| 58 | ·8480 | 8490 | 8499 | 8508 | 8517 | 8526 | 8536 | 8545 | 8554 | 8563 | 9 | 2 | 3 | 5 | 6 | 8 |
| 59 | -8572 | 8581 | 8590 | 8599 | 8607 | 8616 | 8625 | 8634 | 8643 | 8652 | | 1 | 3 | 4 | 6 | 7 |
| 60 | 0-8660 | 8669 | 8678 | 8686 8771 | 8695 | 8704 8788 | 8712 8796 | 8721 8805 | 8729 8813 | 8738 8821 | | 1 | 3 | 4 | 6 | 7 |
| 61 | ·8746 | 8755 | 8763 | 8854 | 8780 8862 | 8870 | 8878 | 8886 | 8894 | 8902 | ۱. | 1 | 3 | 4 | 6 | 7 |
| 62 | -8829 -8910 | 8838 8918 | 8846 8926 | 8934 | 8942 | 8949 | 8957 | 8965 | 8973 | 8980 | 8 | | 3 | 4 | 5 | 6 |
| 63 64 | -8988 | 8996 | 9003 | 9011 | 9018 | 9026 | 9033 | 9041 | 9048 | 9056 | | i | 3 | 4 | 5 | 6 |
| | 0.9063 | 9070 | 9078 | 9085 | 9092 | 9100 | 9107 | 9114 | 9121 | 9128 | ł | 1 | 2 | 4 | 5 | 6 |
| 65 | 19135 | 9143 | 9150 | | 9164 | 9171 | 9178 | 9184 | 9121 | 9198 | 7 | 1 | 2 | 4 | 6 | 6 |
| 66 67 | -9205 | 9212 | 9219 | 9225 | 9232 | 9239 | 9245 | 9252 | 9259 | 9265 | ' | li | 2 | 3 | 4 | 6 |
| 68 | 9272 | 9278 | 9285 | 9291 | 9298 | 9304 | 9311 | 9317 | 9323 | 9330 | | 1 | 2 | | 4 | 5 |
| 69 | ·9336 | 9342 | 9348 | 9354 | 9361 | 9367 | 9373 | 9379 | 9385 | 9391 | 6 | 1 | 2 | 3 | 4 | 5 |
| 70 | 0.9397 | 9403 | 9409 | 9415 | 9421 | 9426 | 9432 | 9438 | 9444 | 9449 | l | 1 | 2 | 3 | 4 | 5 |
| 71 | 9455 | 9461 | 9466 | 9472 | 9478 | 9483 | 9489 | 9494 | 9500 | 9505 | 1 | Ιi | 2 | | 4 | 5 |
| 72 | ·9511 | 9516 | 9521 | 9527 | 9532 | 9537 | 9542 | 9548 | 9553 | 9558 | 1 | Ιi | 2 | 3 | 3 | 4 |
| 73 | -9563 | 9568 | 9573 | 9578 | 9583 | 9588 | 9593 | 9598 | 9603 | 9608 | l 5 | Ιi | | | 3 | 4 |
| 74 | ·9613 | 9617 | 9622 | 9627 | 9632 | 9636 | 9641 | 9646 | 9650 | 9655 | | 1 | 2 | 2 | 3 | 4 |
| 75 | 0.9659 | 9664 | 9668 | 9673 | 9677 | 9681 | 9686 | 9690 | 9694 | 9699 | l | 1 | 1 | 2 | 3 | 4 |
| 76 | -9703 | 9707 | 9711 | 9715 | 9720 | 9724 | 9728 | 9732 | 9736 | 9740 | 4 | 1 | 1 | 2 | 3 | 3 |
| 77 | -9744 | 9748 | 9751 | 9755 | 9759 | 9763 | 9767 | 9770 | 9774 | 9778 | 1 |] 1 | 1 | 2 | 2 | 3 |
| 78 | -9781 | 9785 | 9789 | 9792 | 9796 | 9799 | 9803 | 9806 | 9810 | 9813 | | 1 | 1 | 2 | 2 | 3 |
| 79 | -9816 | 9820 | 9823 | 9826 | 9829 | 9833 | 9836 | 9839 | 9842 | 9845 | l | 1 | 1 | 2 | 2 | 3 |
| 80 | 0-9848 | 9851 | 9854 | 9857 | 9860 | 9863 | 9866 | 9869 | 9871 | 9874 | 3 | 0 | 1 | 1 | 2 | 2 |
| 81 | ·9877 | 9880 | 9882 | 9885 | 9888 | 9890 | 9893 | 9895 | 9898 | 9900 | l | ļ | 1 | 1 | 2 | 2 |
| 82 | ·9903 | 9905 9928 | 9907 9930 | 9910 9932 | 9912 9934 | 9914 9936 | 9917 9938 | 9919 9940 | 9921 9942 | 9923 9943 | ۾ ا | ļ | 1 | 1 | 1 | 2 |
| 83 | -9925 -9945 | 9928 | 9930 | 9932 9951 | 9954 | 9956 | 9956 | 9940 | 9942 | 9943 9960 | 2 | 0 | 1 | 1 | 1 | 2 |
| 84 | C+68. | 994/ | 3343 | 3301 | | | | | 3303 | | | ľ | ١ | 1 | 1 | 1 |
| 85 | 0.9962 | 9963 | 9965 | 9966 | 9968 | 9969 | 9971 | 9972 | 9973 | 9974 | | 0 | 0 | 1 | 1 | 1 |
| 86 | ·9976 | 9977 | 9978 | 9979 | 9980 | 9981 | 9982 | 9983 | 9984 | 9985 | 1 | 0 | Q | 1 | 1 | 1 |
| 87 | -9986 | 9987 | 9988 | 9989 | 9990 | 9990 | 9991 | 9992 | 9993 | 9993 | | | _ | _ | | |
| 86 | -9994 | 9995 | 9995 | 9996 | 9996 | 9997 | 9997 | 9997 | 9998 | 9998 | l | | | e T | | • |
| 89 | 0-9998 | 9999 | 9999 | 9999 | 9999 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | l | | Ь | elo | w. | |
| 90 | 1-0000 | | | | l | | | L | | | | | | | | |
| | · | | | | 1 | | | <u> </u> | | | | - | | | | - |

Sines of Angles near 90%

| | | 211163 | • | \sim | 18103 | 1115 | a, | J Q / | |
|------|----|--------|----|--------|-------|------|----|--------------|------|
| | | sine | | | _ | | | sine | |
| 0 | • | J. | 0 | | | 0 | • | ↲ | ٥ |
| 86 - | 48 | • | 86 | -80 | | 87 | 46 | 0.9993 | 87-7 |
| 86 | | 0.9985 | 86 | 91 | | 87 | 56 | | 87.9 |
| 87 | | 0.9986 | 87 | 02 | | 88 | 05 | 0.9994 | 88.0 |
| 87 | | 0.9987 | 87 | 13 | | 88 | 16 | 0.9995 | 88.2 |
| 87 | | 0.9988 | 87 | -25 | | 88 | 29 | 0-9996 | 88.4 |
| 87 | | 0.9989 | 87 | 37 | | 88 | 43 | 0.9997 | 88.7 |
| 87 | | 0.9990 | 87 | 50 | | 89 | 00 | 0.9998 | 89-0 |
| 87 | | 0.9991 | 87 | 63 | | 89 | 25 | 0.9999 | 89-4 |
| 87 | | 0.9992 | 87 | | | 90 | | 1.0000 | 90.0 |

The values in the centre columns represent the sines for all angles lying between the successive ranges shown in the outer columns. Thus 87° 20' is 0-9889. For inverse use, the best angle for a given sine is the one lying midway between the adjacent ranges; if the difference is odd, choose the angle near 90°. Thus if 81° x = 87° 12'.

For tabulated angles read the sine value in the half-line above; e.g., sin 87° 38' - 0.9991,

| <u> </u> | ľ | | | | | | | | | | Ī | 1 | | | | |
|----------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------------|--------------|-----|----|----|-----|----|----|
| x | 0′ | 6′ | 12' | 18' | 24' | 30′ | 36' | 42' | 48′ | 54' | 4 | S | UB | TR | AC | Τ. |
| , , | 00.0 | 00.1 | 00.2 | 00.3 | 0°∙4 | 0°·5 | 00.6 | 0°-7 | $\alpha_{\rm O}.8$ | 00.9 | | 1' | 2' | 3′ | 4′ | 5′ |
| 0° | 1.000 | 1.000 | 1-000 | 1-000 | 1.000 | 1.000 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 1. | Se | e | tab | le | at |
| i | 0.9998 | 9998 | 9998 | 9997 | 9997 | 9997 | 9996 | 9996 | 9995 | 9995 | | | | of | | |
| 2 | -9994 | 9993 | 9993 | 9992 | 9991 | 9990 | 9990 | 9989 | 9988 | 9987 | 1 | ! | | | | |
| 3 | -9986 -9976 | 9985 9974 | 9984 9973 | 9983 9972 | 9982 9971 | 9981 9969 | 9980 9968 | 9979 | 9978 | 9977 | 1 | 0 | 0 | 1 | 1 | 1 |
| 4 | .9970 | 33/4 | 3314 | 3312 | 9971 | 9909 | 3300 | 9966 | 9965 | 9963 | | 0 | 0 | 1 | 1 | 1 |
| 5 | 0.9962 | 9960 | 9959 | 9957 | 9956 | 9954 | 9952 | 9951 | 9949 | 9947 | | 0 | 1 | 1 | 1 | 1 |
| 6 | 9945 | 9943 | 9942 | 9940 | 9938 | 9936 | 9934 | 9932 | 9930 | 9928 | 2 | 0 | 1 | 1 | 1 | 2 |
| 7 | ·9925 | 9923 9900 | 9921 9898 | 9919 9895 | 9917 | 9914 | 9912 | 9910 | 9907 | 9905 | 1 | 0 | 1 | 1 | 1 | 2 |
| 8 | 9903 | 9874 | | 9869 | 9893 9866 | 9890 9863 | 9888 9860 | 9885 9857 | 9882 9854 | 9880 9851 | 3 | 0 | 1 | 1 | 2 | 2 |
| - | 9077 | 3014 | 30,1 | 3003 | 3000 | 3003 | 3000 | 3607 | 3 004 | 3031 | 3 | 0 | 1 | 1 | 2 | 2 |
| 10 | 0.9848 | 9845 | 9842 | 9839 | 9836 | 9833 | 9829 | 9826 | 9823 | 9820 | | 1 | 1 | 2 | 2 | 3 |
| 11 | 9816 | 9813 | 9810 | 9806 | 9803 | 9799 | 9796 | 9792 | 9789 | 9785 | l | 1 | 1 | 2 | 2 | 3 |
| 12 | 9781 | 9778 9740 | 9774 | 9770 9732 | 9767 | 9763 | 9759 | 9755 | 9751 | 9748 | ١. | 1 | 1 | 2 | 2 | 3 |
| 13 | ·9744 ·9703 | 9699 | | 9690 | | 9724 9681 | 9720 9677 | 9715 9673 | 9711 9668 | 9707 9664 | 4 | 1 | 1 | 2 | 3 | 3 |
| 14 | .9703 | 3033 | 3034 | 3030 | 9000 | 3001 | 9077 | 90/3 | 3000 | 9004 | | 1 | 1 | 2 | 3 | 4 |
| 15 | 0.9659 | 9655 | 9650 | 9646 | 9641 | 9636 | 9632 | 9627 | 9622 | . 9617 | | 1 | 2 | 2 | 3 | 4 |
| 16 | -9613 | 9608 | | 9598 | 9593 | 9588 | 9583 | 9578 | 9573 | 9568 | 5 | 1 | 2 | 2 | 3 | 4 |
| 17 | 9563 | 9558 | 9553 | 9548 | | 9537 | 9532 | 9527 | 9521 | 9516 | 1 | 1 | 2 | 3 | 3 | 4 |
| 18 | ·9511 | 9505 | 9500 | 9494 9438 | 9489 | 9483 | 9478 | 9472 | 9466 | 9461 | | 1 | 2 | 3 | 4 | 5 |
| 19 | 19455 | 9449 | 9444 | 9436 | 9432 | 9426 | 9421 | 9415 | 9409 | 9403 | | 1 | 2 | 3 | 4 | 5 |
| 20 | 0.9397 | 9391 | 9385 | 9379 | 9373 | 9367 | 9361 | 9354 | 9348 | 9342 | 6 | 1 | 2 | 3 | 4 | 5 |
| 21 | ·9336 | | 9323 | 9317 | 9311 | 9304 | 9298 | 9291 | 9285 | 9278 | i | 1 | 2 | 3 | 4 | 5 |
| 22 | -9272 | 9265 9198 | 9259 9191 | 9252 | | 9239 | 9232 | 9225 | 9219 | 9212 | i _ | 1 | 2 | 3 | 4 | 6 |
| 23 24 | ·9205 ·9135 | 9198 | 9191 | 9184 9114 | 9178 9107 | 9171 | 9164 9092 | 9157 9085 | 9150 9078 | 9143 | 7 | 1 | 2 | 4 | 5 | 6 |
| | 3133 | 3120 | 3121 | 3114 | 3103 | 3100 | 3032 | 3000 | 3076 | 9070 | l | 1 | 2 | 4 | 5 | 6 |
| 25 | 0.9063 | 9056 | 9048 | 9041 | 9033 | 9026 | 9018 | 9011 | 9003 | 8996 | | 1 | 3 | 4 | 5 | 6 |
| 26 | -8988 | | 8973 | 8965 | | 8949 | 8942 | 8934 | 8926 | 8918 | | 1 | 3 | 4 | 5 | 6 |
| 27 | -8910 -8829 | 8902 8821 | 8894 8813 | 8805 | | 8870 | 8862 | 8854 | 8846 | 8838 | 8 | 1 | 3 | 4 | 5 | 7 |
| 28 29 | ·8746 | 8738 | B729 | B721 | | 8788 8704 | 8780 8695 | 8771 8686 | 8763 8678 | 8755 | | 1 | 3 | 4 | 6 | 7 |
| 45 | 0,40 | 0130 | 4143 | 3121 | Of 12 | 9704 | 0095 | 0000 | 8078 | 8669 | | 1 | 3 | 4 | 6 | 7 |
| 30 | 0.8660 | 8652 | 8643 | 8634 | 8625 | 8616 | 8607 | 8599 | 8590 | 8581 | | 1 | 3 | 4 | 6 | 7 |
| 31 | -8572 | 8563 | 8554 | 8545 | 8536 | 8526 | 8517 | 8508 | 8499 | 8490 | 9 | 2 | 3 | 5 | 6 | 8 |
| 32 | -8480 -8387 | 8471 8377 | 8462 8368 | 8453 8358 | 8443 | 8434 | 8425 | 8415 | 8406 | 8396 | | 2 | 3 | 5 | 6 | 8 |
| 33 34 | ·838/ ·8290 | 8281 | 8271 | 8261 | 8348 8251 | 8339 8241 | 8329 8231 | 8320 8221 | 8310 8211 | 8300 | | 2 | 3 | 5 | 6 | 8 |
| 34 | 0230 | 9201 | 341 | 7201 | 0231 | VE41 | 0231 | 0221 | 0211 | 8202 | | 2 | 3 | 5 | 7 | 8 |
| 35 | 0.8192 | 8181 | 8171 | 8161 | 8151 | 8141 | 8131 | 8121 | 8111 | 8100 | 10 | 2 | 3 | 5 | 7 | В |
| 36 | -8090 | 8080 | 8070 | 8059 | 8049 | 8039 | 8028 | 8018 | 8007 | 7997 | [| 2 | š | 5 | 7 | ğ |
| 37 | -7986 | 7976 | 7965 | 7955 | 7944 | 7934 | 7923 | 7912 | 7902 | 7891 | | 2 | 4 | 5 | 7 | ğ |
| 38 | •7880 | 7869 | 7859 | 7848 | 7837 | 7826 | 7815 | 7804 | 7793 | 7782 | 11 | 2 | 4 | 5 | 7 | 9 |
| 39 | 0.7771 | 7760 | 7749 | 7738 | 7727 | 7716 | 7705 | 7694 | 7683 | 7672 | | 2 | 4 | 6 | 7 | 9 |
| | | | | | | | i | | | | | | | _ | | |

Cosines of Small Angles

| cosine | | | cosine |
|--------------|-----|------|-------------|
| ° ' J | 0 | o, | ა |
| A 04 | 0.0 | 2 13 | 2.21 |
| V 34 1-0000 | 0.5 | 2 21 | 0.9992 2.36 |
| A ED 0-9999 | 0.9 | 2 29 | U-9991 2.40 |
| 1 16 0.3338 | 1.2 | 2 37 | 0.9990 2.60 |
| 1 30 0.9997 | 1.5 | 2 44 | 0.9989 2.74 |
| | 1.7 | | |
| 1 43 0.9995 | | 2 51 | 0-9987 2-86 |
| 1 54 0.9994 | 1.9 | 2 58 | 0.9986 2.97 |
| 2 03 0.9993 | 2.0 | 3 05 | 0-9985 3-08 |
| 2 13 0 3330 | 2.2 | 3 11 | 3.19 |

This table is similar to that given for sines on page 15; thus $\cos 2^{\circ} 40' = 0.9989$ $0.9986 = \cos 3^{\circ} 2'$



| Γ | 0' | 6' | 12' | 18' | 24' | 30' | 36' | 42' | 48' | 54' | | | SUI | вті | RAC | T |
|----------------------------------|---|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|----|------------------|-----------------------|-----------------------|----------------------------|----------------------------|
| × | 00.0 | 00-1 | 0°-2 | 00.3 | 00.4 | 0°-5 | 00.8 | 00.7 | 00.8 | 00.9 | Δ | 1' | 2' | 3' | 4' | 5′ |
| 40° 41 42 43 | 0-7660 -7547 -7431 -7314 | 7649 7536 7420 7302 | 7638 7524 7408 7290 | 7627 7513 7396 7278 | 7615 7501 7385 7266 | 7604 7490 7373 7254 | 7593 7478 7361 7242 | 7581 7466 7349 7230 | 7570 7455 7337 7218 | 7559 7443 7325 7206 | 12 | 2 2 2 2 | 4 4 4 | 6 6 6 | 8 8 8 | 9 10 10 |
| 44 | ·7193 0·7071 | 7181 | 7169 7046 | 7157 7034 | 7145 | 7133 7009 | 7120 6997 | 7108 6984 | 7096 6972 | 7083 6959 | | 2 | 4 | 6 | 8 | 10 |
| 46 47 48 49 | -6947 -6820 -6691 -6561 | 6934 6807 | 6921 6794 6665 6534 | 6909 6782 6652 6521 | 6896 6769 6639 6508 | 6884 6756 6626 6494 | 6871 6743 6613 | 6858 6730 6600 6468 | 6845 6717 6587 6455 | 6833 6704 6574 6441 | 13 | 2 2 2 2 | 4 4 4 | 6 6 7 7 | 9 9 | 11 11 11 11 |
| 50 51 52 53 54 | 0.6428 .6293 .6157 .6018 .5878 | 6414 6280 6143 6004 5864 | 6401 6266 6129 5990 5850 | 6388 6252 6115 5976 5835 | 6374 6239 6101 5962 5821 | 6361 6225 6088 5948 5807 | 6347 6211 6074 5934 5793 | 6334 6198 6060 5920 5779 | 6320 6184 6046 5906 5764 | 6307 6170 6032 5892 5750 | 14 | 2 2 2 2 2 | 4 5 5 5 5 | 7 7 7 7 7 | 9 9 9 | 11 11 12 12 |
| 55 56 57 58 | 0·5736 -5592 •5446 •5299 | 5721 5577 5432 5284 | 5707 5563 5417 5270 | 5693 5548 5402 5255 | 5678 5534 5388 5240 | 5664 5519 5373 5225 | 5650 5505 5358 5210 | 5635 5490 5344 5195 | 5621 5476 5329 5180 | 5606 5461 5314 5165 | | 2 2 2 2 | 5 5 5 5 | 7 7 7 7 | 10 10 10 10 | 12 12 12 12 12 |
| 59 60 61 62 | 0-5000 -4848 -4695 | 4985 4833 4679 | 4970 4818 4664 | 4955 4802 4648 | 4939 4787 4633 | 4924 4772 4617 | 5060 4909 4756 4602 | 4894 4741 4586 | 5030 4879 4726 4571 | 4863 4710 4555 | 15 | 3 3 3 3 | 5 5 5 | 8 8 8 B | 10 10 10 10 | 13 13 13 13 |
| 63 64 65 | ·4540 ·4384 0·4226 | 4524 4368 4210 | 4509 4352 4195 | 4493 4337 4179 | 4478 4321 4163 | 4462 4305 4147 | 4446 4289 4131 | 4431 4274 4115 | 4415 4258 4099 | 4399 4242 4083 | | 3 | 5 | 8 | 10 | 13 |
| 66 67 68 69 | ·4067 ·3907 ·3746 ·3584 | 4051 3891 3730 3567 | 4035 3875 3714 3551 | 4019 3859 3697 3535 | 4003 3843 3681 3518 | 3987 3827 3665 3502 | 3971 3811 3649 3486 | 3955 3795 3633 3469 | 3939 3778 3616 3453 | 3923 3762 3600 3437 | 16 | 3 3 3 3 3 | 5 5 5 5 | 8 8 8 8 8 | 11 11 11 11 | 13 13 13 14 14 |
| 70 71 72 73 74 | 0-3420 -3256 -3090 -2924 -2756 | 3404 3239 3074 2907 2740 | 3387 3223 3057 2890 2723 | 3371 3206 3040 2874 2706 | 3355 3190 3024 £857 2689 | 3338 3173 3007 2840 2672 | 3322 3156 2990 2823 2656 | 3305 3140 2974 2807 2639 | 2790 | 3272 3107 2940 2773 2605 | | 33333 | 5 6 6 6 | 8 8 8 8 | 11 11 11 11 | 14 14 14 14 14 |
| 75 76 77 78 79 | 0·2588 ·2419 ·2250 ·2079 ·1908 | 2571 2402 2233 2062 1891 | 2554 2385 2215 2045 1874 | 2538 2368 2198 2028 1857 | 2521 2351 2181 2011 1840 | 2504 2334 2164 1994 1822 | 2487 2317 2147 1977 1805 | 2470 2300 2130 1959 1788 | | 2436 2267 2096 1925 1754 | 17 | 3 3 3 | 6 6 6 6 | 8 9 9 | 11 11 11 11 11 | 14 14 14 14 14 |
| 80 81 82 83 84 | 0-1736 -1564 -1392 -1219 -1045 | 1719 1547 1374 1201 1028 | 1702 1530 1357 1184 1011 | 1685 1513 1340 1167 0993 | 1668 1495 1323 1149 0976 | 1650 1478 1305 1132 0958 | 1633 1461 1288 1115 0941 | 1616 1444 1271 1097 0924 | 1599 1426 1253 1080 0906 | 1582 1409 1236 1063 0889 | | 3 3 3 | 6 6 6 6 | 9 9 9 9 | 11 11 12 12 12 | 14 14 14 14 |
| 85 86 87 88 89 90 | 0-0872 -0698 -0523 -0349 0-0175 0-0000 | 0854 0680 0505 0332 0157 | 0837 0663 0488 0314 0140 | 0819 0645 0471 0297 0122 | 0802 0628 0454 0279 0105 | 0785 0610 0436 0262 0087 | 0767 0593 0419 0244 0070 | 0750 0576 0401 0227 0052 | 0732 0558 0384 0209 0035 | 0715 0541 0366 0192 0017 | 18 | 3 3 3 3 | 6 6 6 6 | 9 9 | 12 12 12 12 12 | 14 15 15 15 15 |

| | 0' | 6′ | 12' | 18' | 24' | 30, | 36' | 42' | 48' | 54' | | Γ | | ADI | > | |
|----------------------------|---|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|----------------------------------|-----------------------|----------------------------------|----------------------------|--|----------------------------------|
| X | 00.0 | 00-1 | 00.2 | 00.3 | 00.4 | 00.5 | 00.6 | 00.7 | 00.8 | 00.9 | 4 | 1' | 2' | 3′ | 4' | 5′ |
| 0° 1 2 | 0.0000 -0175 -0349 -0524 | 0017 0192 0367 0542 | 0035 0209 0384 0559 | 0227 | | 0087 0262 0437 0612 | 0105 0279 0454 0629 | 0122 0297 0472 0647 | 0140 0314 0489 0664 | 0157 0332 0507 0682 | 18 | 3 3 3 3 | 6 6 6 | 9 9 9 | 12 12 12 12 | 15 15 15 |
| 4 | -0699 | 0717 | 0734 | | 0769 | 0787 | 0805 | 0822 | | 0857 | | 3 | 6 | 9 | 12 | 15 |
| 5 6 7 8 9 | 0.0875 -1051 -1228 -1405 -1584 | 0892 1069 1246 1423 1602 | 0910 1086 1263 1441 1620 | 0928 1104 1281 1459 1638 | 0945 1122 1299 1477 1655 | 0963 1139 1317 1495 1673 | 0981 1157 1334 1512 1691 | 0998 1175 1352 1530 1709 | 1016 1192 1370 1548 1727 | 1033 1210 1388 1566 1745 | | 3 3 3 3 | 6 6 6 6 | 9 9 9 | 12 12 12 12 12 | 15 15 15 15 |
| 10 11 12 13 14 | 0·1763 -1944 •2126 -2309 •2493 | 1781 1962 2144 2327 2512 | 1799 1980 2162 2345 2530 | 1817 1998 2180 2364 2549 | 1835 2016 2199 2382 2568 | 1853 2035 2217 2401 2586 | 1871 2053 2235 2419 2605 | | 1908 2089 2272 2456 2642 | 1926 2107 2290 2475 2661 | : : | 3 3 3 3 | 6 6 6 6 | 9 9 9 9 | 12 12 12 12 12 | 15 15 15 15 |
| 15 16 17 18 19 | 0·2679 ·2867 ·3057 ·3249 ·3443 | 2698 2886 3076 3269 3463 | 2717 2905 3096 3288 3482 | 2736 2924 3115 3307 3502 | 2754 2943 3134 3327 3522 | 2773 2962 3153 3346 3541 | 2792 2981 3172 3365 3561 | 2811 3000 3191 3385 3581 | 2830 3019 3211 3404 3600 | 2849 3038 3230 3424 3620 | 19 | 3 3 3 3 | 6 6 6 7 | 9 10 10 10 | 13 13 13 13 | 16 16 16 16 |
| 20 21 22 23 24 | 0.3640 .3839 .4040 .4245 .4452 | 3659 3859 4061 4265 4473 | 3679 3879 4081 4286 4494 | 3699 3899 4101 4307 4515 | 3719 3919 4122 4327 4536 | 3739 3939 4142 4348 4557 | 3759 3959 4163 4369 4578 | 3779 3979 4183 4390 4599 | 3799 4000 4204 4411 4621 | | 20 21 | 3 3 3 4 | 7 7 7 7 7 | 10 10 10 10 10 | 13 13 14 14 14 | 17 17 17 17 17 |
| 25 26 27 28 29 | 0-4663 -4877 -5095 -5317 -5543 | 4684 4899 5117 5340 5566 | 4706 4921 5139 5362 5589 | 4727 4942 5161 5384 5612 | 4748 4964 5184 5407 5635 | 4770 4986 5206 5430 5658 | 4791 5008 5228 5452 5681 | 40.0 | 4834 5051 5272 5498 5727 | 4856 5073 5295 5520 5750 | 22 | 4 4 4 4 4 | 7 7 7 8 8 | 11 11 11 11 | 14 15 15 15 15 | 18 18 18 19 |
| 30 31 32 33 34 | 0·5774 ·6009 ·6249 ·6494 ·6745 | 5797 6032 6273 6519 6771 | 5820 6056 6297 6544 6796 | 5844 6080 6322 6569 6822 | 5867 6104 6346 6594 6847 | 5890 6128 6371 6619 6873 | 5914 6152 6395 6644 6899 | 5938 6176 6420 6669 6924 | 5961 6200 6445 6694 6950 | 5985 6224 6469 6720 6976 | 24 25 | 4 4 4 4 | 8 8 8 9 | 12 12 12 13 13 | 16 16 16 17 17 | 20 20 20 21 21 |
| 35 38 37 38 39 | 0-7002 -7265 -7536 -7813 -8098 | 7028 7292 7563 7841 8127 | 7054 7319 7590 7869 8156 | 7080 7346 7618 7898 8185 | 7107 7373 7646 7926 8214 | 7133 7400 7673 7954 8243 | 7159 7427 7701 7983 8273 | 7186 7454 7729 8012 8302 | 7212 7481 7757 8040 8332 | 7239 7508 7785 8069 8361 | 26 27 28 29 | 45555 | 9 9 10 10 | 13 14 14 14 15 | 17 18 19 19 | 22 23 23 24 24 |
| 40 41 42 43 44 | 0.8391 -8693 -9004 -9325 -9657 | 8421 8724 9036 9358 9691 | 8451 8754 9067 9391 9725 | 8481 8785 9099 9424 9759 | 8511 8816 9131 9457 9793 | 8541 8847 9163 9490 9827 | 8571 8878 9195 9523 9861 | 8601 8910 9228 9556 9896 | 8632 8941 9260 9590 9930 | 8662 8972 9293 9623 9965 | 30 31 32 33 34 | 55566 | 10 10 11 11 11 | 15 16 16 17 | 20 21 21 22 22 | 25 26 27 28 28 |
| 45 46 47 48 49 | 1.0000 .0355 .0724 .1106 1.1504 | 0035 0392 0761 1145 1544 | 0070 0428 0799 1184 1585 | 0105 0464 0837 1224 1626 | 0141 0501 0875 1263 1667 | 0176 0538 0913 1303 1708 1708 | 0951 1343 | 0990 1383 | 0283 0649 1028 1423 1833 | 0319 0686 1067 1463 | 36 37 38 40 41 42 | 6 6 7 7 | 12 12 13 13 14 14 | 18 19 20 20 21 | 24 25 25 27 27 27 28 | 30 31 32 33 34 35 |



| | 0′ | 6' | 12' | 18' | 24' | 30′ | 36′ | 42' | 48' | 54' | | | , | ADD |) | |
|----------------------------------|---|---|---|---|---|--|---|---|---|---|----------------------------------|-----------------------|---------------------------------|-----------------------|----------------------------------|----------------------------------|
| × | 00.0 | 00-1 | 0°·2 | 0°-3 | 00.4 | 00.5 | 0°-6 | 0°·7 | 00.B | 00·8 | Δ | 1' | 2' | 3′ | 4" | 5′ |
| 50° 51 52 53 54 | 1·192 -235 -280 -327 -376 | 196 239 285 332 381 | 200 244 289 337 387 | 205 248 294 342 392 | 209 253 299 347 397 | 213 257 303 351 402 | 217 262 308 356 407 | 222 266 313 361 412 | 226 271 317 366 418 | 230 275 322 371 423 | 5 | 1 1 1 1 | 1 2 2 2 2 | 2 2 2 2 3 | 3 3 3 3 | 4 4 4 4 |
| 55 56 57 58 59 | 1-428 -483 -540 -600 -664 | 433 488 546 607 671 | 439 494 552 613 678 | 444 499 558 619 684 | 450 505 564 625 691 | 455 511 570 632 698 | 460 517 576 638 704 | 466 522 582 645 711 | 471 528 588 651 718 | 477 534 594 658 725 | 6 | 1 1 1 1 | 2 2 2 2 | 3 3 3 3 | 4 4 4 5 | 5 5 5 6 |
| 60 61 62 63 64 | 1.732 .804 .881 1.963 2.050 | 739 811 889 971 059 | 746 819 897 980 069 | 753 827 905 988 078 | 760 834 913 1-997 087 | 767 842 921 2-006 097 | 775 849 929 2·014 106 | 782 857 937 2·023 116 | 789 865 946 2·032 125 | 797 873 954 2·041 135 | 7 8 9 | 1 1 1 1 2 | 2 3 3 3 | 4 4 4 4 5 | 5 5 6 6 | 6 7 7 8 |
| 65 66 67 68 69 | 2·145 ·246 ·356 ·475 ·605 | 154 257 367 488 619 | 164 267 379 500 633 | 174 278 391 513 646 | 184 289 402 526 660 | 194 300 414 539 675 | 204 311 426 552 689 | 215 322 438 565 703 | 225 333 450 578 718 | 236 344 463 592 733 | 10 11 12 13 14 | 2 2 2 2 2 | 3 4 4 4 5 | 5 6 6 7 | 7 7 8 9 | 8 9 10 11 12 |
| 70 71 72 73 | 2·747 2·904 3·078 | 762 921 096 2 9 1 | 778 937 115 312 | 793 954 133 333 | 808 971 152 354 | 824 2·989 3·172 172 376 376 | 840 3.006 191 398 | 856 3·024 211 420 | 872 3·042 230 442 | 888 3-060 251 465 | 16 17 19 20 21 22 | 3 3 3 4 4 | 5 6 7 7 | 8 9 10 10 | 11 11 13 13 14 15 | 13 14 16 17 18 18 |
| 74 | ·487 | 511 | 534 | 558 | 582 | 606 606 | 630 | 655 | 681 | 706 | 24 25 | 4 | 8 8 | 12 13 | 16 17 | 20 21 |
| 75 76 | 3-732 4-011 | 75B 041 | 785 071 | 812 102 | 839 134 | 867 867 4·165 | 895 | 923 | 952 | 981 | 27 29 31 | 4 5 5 | 9 10 10 | 14 14 15 | 18 19 21 | 22 24 26 |
| 77 | 4-331 | 366 | 402 | 437 | 474 | 165 511 511 | 198 548 | 230 586 | 264 625 | 297 665 | 33 36 39 | 6 6 | 11 12 13 | 17 18 19 | 22 24 26 | 28 30 32 |
| 78 | 4-705 | 745 | 787 | 829 | 872 | 4-915 4-915 | 4.959 | 5.005 | 5.050 | 5.097 | 42 46 50 | 7 8 8 | 14 15 17 | 21 23 25 | 28 31 33 | 35 38 42 |
| 79 | 5.145 | 193 | 242 | 292 | | 5-396 396 | 449 | 503 | 558 | 614 | 55 | 9 | 18 | 28 | 37 | 46 |
| 80 | 5·671 6·314 | 5·730 6·386 | 5·789 6·460 | 5-850 6-535 | 5·912 6·612 | 5.976 5.976 6.691 | 6-041 | 6-107 | 6-174 | 6.243 | | 10 11 13 | 20 23 25 | 30 34 38 | 41 45 50 | 51 56 63 |
| 82 83 84 | 7·115 8·144 9·514 | 7 207 8 264 9 677 | 7·300 8·386 9·845 | 7·396 8·513 10·02 | 7·495 8·643 10·20 | 6.691 7.596 8.777 10.39 | 6·772 7·700 8·915 10·58 | 6·855 7·806 9·058 10·78 | 6·940 7·916 9·205 10·99 | 7·026 8·028 9·357 11·20 | | | 28 iffer | | | |
| 85 86 87 88 89 90 | 11,43 14,30 19,08 28,64 57,29 | 11.66 14.67 19.74 30.14 63.66 | 11·91 15·06 20·45 31·82 71·62 | 12·16 15·46 21·20 33·69 81·85 | 12·43 15·89 22·02 35·80 95·49 | 12·71 16·35 22·90 38·19 114·6 | 13-00 16-83 23-86 40-92 143-2 | 13·30 17·34 24·90 44·07 191·0 | 13·62 17·89 26·03 47·74 286·5 | 13-95 18-46 27-27 52-08 573-0 | | in P | oo r iterp .P.s. n pa; | olat Se | ión e tal | bу |

P.P.s for differences exceeding 14, if not shown on this page, should be taken from the inside end cover of the book. For angles between 72° and 82° P.P.s based on actual differences should be used.

Lay-Out Work

40. Plane Laying-Out

The fabrication of plugs, flanges, and other parts involves inscribing the boundaries of these parts and marking the bolt hole centres on plate steel, transferring them from the working drawings to the blank surface, i.e., laying-out.

In mass production of parts at pipe-fitting shops, lay-out work is performed with the aid of previously made templates. On small jobs and in field conditions lay-out work is done manually in conformity with geometric rules, using rulers, squares, protractors, compasses, scribers, and other tools.

The accurate dimensions of flanges or plugs, as well as the number and position of bolt holes are indicated in the working drawings. When laying-out, allowances must be provided to work the part; the margin allowed should be minimal to save metal, time, and labour required for removing excess metal. The steel to be laid out must be cleaned from dirt and rust, and then coated with chalk paint. Such paint is prepared as follows: take 8 lit of water, add 1 kg of ground chalk, and heat the mixture obtained to the boiling point. Then add 50 g of joiner's glue previously dissolved in water.

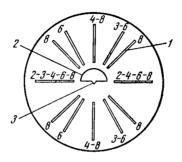


Fig. 77. Template for laying out bolt hole centres in flanges and plugs

1-slits; 2-semicircular hole; 3-template centre]

After adding the glue, reheat the mixture to the boiling point. In the summer, linseed oil and siccative are added to the mixture.

The chalk paint is applied to the steel surface with a painter's brush. It is good practice to use spray guns to apply the paint evenly.

When the paint dries, use a template for laying-out. To make the template (Fig. 77) cut a round disc out of sheet steel 0.3 to 1.0 mm thick. Then cut out semicircular hole 2 and template centre 3. Mark out lines dividing the disc into 2, 4, 6, 8, etc. equal parts. 0.3-mm wide slits 1 made along these lines are designated by figures inscribed at the tips of the slits. The figures indicate the number of circumference parts the slit corresponds to.

For laying-out the bolt hole centres on a flange or plug, draw a circle of the required radius on the blank, all the centres lying on the circumference of this circle. Then place the template on the blank surface so that its centre coincides with the centre of the inscribed circle. After that, using a sharply pointed scriber, incise lines along the appropriate

slits. For example, for laying-out six holes scribe lines in the slits designated by figure 6. The points of intersection of the scribed lines and the previously drawn circle will be the bolt hole centres. The hole centres at these points are marked with a punch.

If templates are not available, flanges and plugs, as well

as bolt holes are laid out in the following way.

Draw line AB on the steel surface with the aid of a rule (Fig. 78). Then using the compasses, draw a circle with

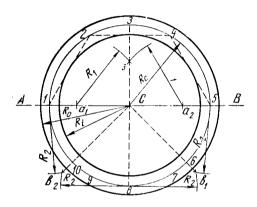


Fig. 78. Laying out holes in flanges in conformity with geometric rules

radius R_0 corresponding to the outside radius of the flange or plug, a second circle with radius R_1 corresponding to the inside radius of the flange, and finally a third circle with radius R_c corresponding to the position of the bolt hole centres. The radii are given in the working drawings.

For marking four bolt centres, lay-out work is carried out as follows. Mark two holes as the points of intersection of line AB and the circle with radius R_c , i. e., at points I and S, and the other two holes at the point of intersection of the same circle with the perpendicular to line AB erected from centre C of the circles. For this purpose, mark points a_1 and a_2 on line AB and draw arcs with radius R_1 from these points. The straight line passing through the point of intersection (a_3) of these arcs and centre C gives the position of

the hole centres for the third and fourth bolts at the points of intersection of this line and the circle with radius R_c , i.e., at points 3 and 8.

The bolt hole centres of six-bolt connections can be marked out very simply, since the chords, i.e., the straight lines between the centres of the bolt holes, are equal to radius R_c . For marking-out the hole centres, inscribe the circle with radius R_c , then starting at point 1 (point of intersection of this circle with line AB), using radius R_c , plot distances 1-2, 2-4, 4-5, 5-7, 7-9, and 9-1. Points 1, 2, 4, 5, 7, and 9 located on the circle with radius R_c will be the hole centres.

In flanges and plugs containing eight bolt holes, first mark four hole centres and then the other four between the previously marked ones. To mark-out these centres, draw arcs with radius R_2 from adjacent centres 5 and 8 (8 and 1); then connect intersection points b_1 and b_2 with centre C. The centres of the additional bolt holes will be located at points 6 and 10 where these lines intersect the circle with radius R_c . On accomplishing lay-out work, each bolt hole centre should be fixed on the metal with a steel prick-punch and hammer.

41. Three-Dimensional Laying-Out

Three-dimensional laying-out is employed when cutting large-diameter steel pipes to obtain accurate cutting lines either at right angles to the pipe axis or at a preset angle; it is also used in producing welded steel fittings (tees, crosses, branches, etc.).

To produce cutting lines at right angles to the pipe axis, use is made of sheet steel strips from 10 to 12 cm wide, their length somewhat exceeding the circumference of the pipe being cut.

The strip must be tightly wrapped around the pipe and its ends should meet so that the cutting line formed is straight. On making sure that the strip is in firm contact with the pipe surface and its ends are properly aligned, scribe the cutting line along the strip edge. To make the eine clearer, use sharpened chalk or crayons.

In case the pipe is not cut immediately after scribing, the cutting line must be prick-punched at points spaced 15-25 cm apart.

For producing steel tees, crosses, and other fittings, use

is made of sheet steel or cardboard templates.

Blanks for producing tees (Fig. 79) or crosses (in the Figure the second branch is shown as a dash line) with

main pipe outer diameter D, and branch diameter d should be laid in the following manner.

The branch is connected to the main pipe along curved line ll_1 which should be scribed on the main pipe and on the branch.

For making the template, it is necessary to develop the branch (show the three-dimensional body on a plane); at first it will represent rectangle $n-6^1-6^1-n$. Then curved line n-m-f-e-c-b-a...n is laid-out on the rectangle. This line is used to contact the branch with the main pipe along line ll_1 .

To make the template, proceed as follows. Draw the cross section of the tee in full size on a sheet of paper. On the

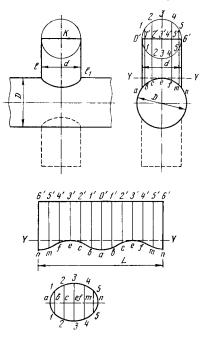


Fig. 79. Laying out blanks for fabricating tees

butt-end of the drawn branch inscribe a circle of the same diameter as that of the actual branch. Then divide the circumference of this circle into 8 or 12 equal parts in accordance with the above-mentioned rules. From points 0', 1, 2, 3, 4, 5, and 6' draw lines parallel to the branch generating line, that intersect the main pipe circumference at points a, b, c, e, f, m, n. Lines 0'-a, 1-b, 2-c, 3-e, 4-f, 5-m, and 6'-n

intersect the branch butt-end line at points 1', 2', 3', etc.

After that, it is possible to make the template. For this purpose draw straight line 6'-6' equal to the branch circumference, i.e., $L = \pi \cdot d = 3 \cdot 14d$, on a sheet of cardboard or roofing steel. Divide the line into as many equal parts as the circumference was divided into (here 12). At each division draw a line at right angles to line 6'-6' and

Table 3
Chord Lengths in Circle (with Radius R=1)
Divided into Equal Parts

| Number | Chord | Number | Chord | Number | Chord |
|---|--|--|--|--|--|
| of | length | of | length | of | length |
| divisions | S | divisions | S | divisions | S |
| 3 4 5 6 7 8 9 10 11 12 13 14 15 16 | 1.7321 1.4142 1.1756 1.0000 0.8678 0.7654 0.6840 0.5635 0.5176 0.4786 0.4450 0.4458 0.3902 | 17 18 19 20 21 22 23 24 25 26 27 28 29 30 | 0.3676 0.3473 0.3292 0.3129 0.2980 0.2845 0.2723 0.2611 0.2507 0.2411 0.2321 0.2321 0.2162 0.2162 | 31 32 33 34 35 36 37 38 39 40 41 42 43 44 | 0.2023 0.1961 0.1901 0.1846 0.1793 0.1743 0.1697 0.1652 0.1609 0.1569 0.1531 0.1494 0.1459 0.1426 |

Example. Determine the chord length X between two centres of adjacent holes around the circumference of a circle with diameter D=960 mm, the number of holes being 24.

The chord length X is determined from the formula

$$X = S \cdot \frac{D}{2} \text{ mm}$$

The chord length S for a circle with a radius equal to 1 is also divided into 24 parts. The number of holes being 24, table 3 gives S=0.2611.

$$X = 0.2611 \cdot \frac{960}{2} = 125.3 \text{ mm}$$

on each of them plot distances corresponding to lines 6'-n, 5'-m, 4'-f, etc. taken from the drawing. For obtaining the bottom contour of the branch development, connect points m, n, f, e, etc. with a smooth curve.

To obtain the required template, carefully cut the steel sheet or cardboard along the developed curve. Place the template on the steel pipe blank and scribe the curved cutting line on the branch and cut it along this line.

The holes for joining the branch to the main pipe can also be marked out with the aid of templates made in conformity with geometric rules. However when ready-made branches are available, it is good practice to place an accurately fabricated branch on the main pipe and to scribe the lines for cutting out the holes.

In lay-out work, division of the circumference into a preset number of equal parts in conformity with geometric rules (particularly if it is divided into a great number of equal parts) takes a lot of time. This work can be done quicker and more simply by using chord lengths S previously calculated for a circle with a radius equal to one (see Table 3).

3. DETERMINING DIMENSIONS AND LAYING OUT STOCK DEVELOPMENTS

Many parts from sheet, strip and round stock (angles, cramps, boxes, jackets, hinges, etc.) are made by bending at various angles and radii or into curvatures and other shapes.

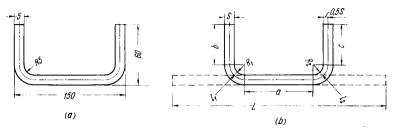


Fig. 68. Example of bending a part

In each case, in order to obtain the required size after bending, it is necessary first to determine (calculate) the size of the stock.

To determine the stock size in bending to internal curvature radii it is sufficient to sum up the straight sections and the neutral lines within the curvature.

The length of the neutral line within the curved section in bending to 90° is determined by the formula:

$$l = \left(R + \frac{S}{2}\right) \frac{\pi}{2}$$

in bending to any other angle l = 0.0175 $\left(R + \frac{S}{2}\right)\alpha$, where l = length of the neutral lines, mm

R = internal curvature radius, mm

S = stock thickness, mm

 α = bending angle, deg.

The lengths of the straight sections of the stock up to the point of bending are calculated from the drawing. The dimensions are usually given on the external contour of the part, as shown in Fig. 68a.

The size of the stock made of sheet material 0.3 to 10 mm thick and bent to a curvature with radius 1 to 30 mm at any bending angle can be found using Table 13 by the formula

$$L = a + b + c + l$$
 (see Fig. 68b)
 $l = l_1 + l_2$

where a, b, c stand for the length of the straight sections before the curvature.

l = length of the neutral lines within the curvature.The length of the neutral line is computed by the formula $l = K\alpha$.

The value of K is given in Table 13. For computing, it is necessary to know stock thickness S, bending radius R and bending angle α , which data are commonly listed in the drawings. The value of K taken from the Table is multiplied by the bending angle α and the product is added to the lengths of the straight sections before the curvature.

How to use Table 13. To calculate the dimensions of the stock for bending to the following sizes: a=48 mm; b=65 mm; $\alpha=137^\circ$; R=2l mm and S=8 mm. L=a+b+l. Find the given thickness figure in the horizontal row for S (S=8 mm) and the bending radius in the vertical column (R=2l mm) in Table 13.

The intersection of the row and column gives K = 0.436.

The length of the neutral line $l = K\alpha = 0.436 \times 137 = 59.7$ mm; by summing up the numerical values of a, b and l determine the stock length

$$L = a + b + l = 48 + 65 + 59.7 = 172.7$$
 mm

Calculating the Length of Neutral

Lines & at Any Bending Angles

| Bend- ing | | | | | | | Fa | actor K | with | Various | Thickne | ss of M | | S, in | mm | | | | | | |
|---|--|---|--|--|---|---|---|---|--|--|--|--|--|--|--|---|---|--|--|--|---|
| us, R, mm | 0.3 | 0 · 5 | 0.8 | 1 | 1.2 | 1.5 | 1 · 6 | 1.8 | 2 | 2.5 | 2.8 | 3 | 3.5 | 4 | 4.5 | 5 | 6 | 7 | 8 | 9 | |
| ing radius, R, mm 1 2 3 4 5 6 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 | 0.020 0.038 0.055 0.072 0.090 0.107 0.125 0.142 0.160 0.177 0.195 0.212 0.230 0.247 0.264 0.282 0.299 0.317 0.330 0.352 0.369 0.387 0.404 0.421 | 0.022 0.039 0.057 0.074 0.092 0.109 0.127 0.144 0.161 0.214 0.231 0.249 0.266 0.284 0.301 0.319 0.353 0.371 0.388 0.406 0.423 | 0.024 0.042 0.059 0.077 0.094 0.112 0.147 0.164 0.182 0.216 0.234 0.251 0.269 0.286 0.304 0.321 0.339 0.356 0.373 0.391 0.408 0.426 | 0.026 0.044 0.061 0.079 0.096 0.113 0.131 0.148 0.166 0.221 0.236 0.271 0.288 0.305 0.323 0.340 0.358 0.375 0.393 0.410 | 0.028 0.045 0.063 0.080 0.115 0.133 0.150 0.168 0.185 0.202 0.237 0.255 0.272 0.290 0.307 0.325 0.342 0.360 0.377 0.394 0.412 | 0.048 0.065 0.083 0.100 0.118 0.153 0.170 0.188 0.206 0.223 0.240 0.257 0.275 0.292 0.310 0.327 0.345 0.362 0.380 0.397 0.415 | | 0.051 0.068 0.086 0.103 0.120 0.138 0.155 0.173 0.208 0.225 0.243 0.260 0.278 0.312 0.330 0.347 0.365 0.382 0.400 0.417 0.435 | 0.052 0.070 0.087 0.105 0.122 0.140 0.157 0.175 0.297 0.227 0.244 0.262 0.279 0.297 0.314 0.332 0.349 0.367 0.384 0.367 | 2.5 0.057 0.074 0.092 0.109 0.127 0.144 0.161 0.179 0.214 0.249 0.266 0.284 0.301 0.319 0.336 0.353 0.371 0.388 0.406 0.423 0.441 | 2.8 0.059 0.077 0.094 0.112 0.128 0.147 0.164 0.182 0.199 0.216 0.234 0.251 0.269 0.286 0.309 0.321 0.339 0.356 0.375 0.391 0.408 0.426 0.443 | 3 | 0.082 0.100 0.118 0.153 0.170 0.188 0.205 0.223 0.240 0.257 0.275 0.310 0.327 0.345 0.362 0.380 0.397 0.415 0.432 0.449 | 0.105 0.122 0.140 0.157 0.175 0.192 0.209 0.227 0.244 0.262 0.279 0.314 0.332 0.349 0.367 0.384 0.401 0.418 0.436 0.454 | 4.5 0.109 0.127 0.144 0.161 0.179 0.196 0.214 0.231 0.249 0.366 0.384 0.301 0.319 0.336 0.353 0.371 0.388 0.406 0.423 0.441 0.458 | 0.131 0.148 0.168 0.183 0.201 0.218 0.236 0.253 0.271 0.288 0.305 0.323 0.340 0.358 0.375 0.393 0.410 0.428 0.445 | 0.157 0.175 0.192 0.209 0.227 0.244 0.262 0.279 0.314 0.332 0.349 0.367 0.384 0.401 0.419 0.436 0.454 | 0.183 0.201 0.218 0.236 0.253 0.271 0.288 0.305 0.323 0.340 0.358 0.375 0.393 0.410 0.428 0.445 0.463 0.480 | 0.209 0.227 0.244 0.262 0.279 0.314 0.332 0.349 0.367 0.384 0.401 0.419 0.436 0.454 | | 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0 |
| 24 25 26 27 28 29 30 | 0.439 0.456 0.474 0.491 0.509 | 0.441 0.458 0.478 0.493 0.511 | 0.443 0.461 0.478 0.496 0.513 | 0.445 0.463 0.480 0.497 0.515 | 0.447 0.464 0.482 0.499 0.517 | 0.449 0.467 0.484 0.502 0.519 | 0.450 0.468 0.485 0.503 0.520 | 0.452 0.469 0.487 0.504 0.522 | 0.454 0.471 0.488 0.506 0.524 | 0.441 0.458 0.476 0.498 0.511 0.528 0.545 | 0.443 0.461 0.478 0.496 0.513 0.531 | 0.445 0.463 0.480 0.497 0.515 0.532 | 0.449 0.467 0.484 0.502 0.519 0.537 | 0.454 0.471 0.489 0.506 0.524 0.540 | | 0.463 0.480 0.497 0.515 0.532 0.550 | 0.471 0.489 0.505 0.524 0.541 0.559 | 0.480 0.497 0.515 0.532 0.550 0.567 | 0.489 0.506 0.524 0.541 0.559 0.576 | 0.497 0.515 0.532 0.550 0.567 0.585 | 0 0 0 0 0 |

4. THE DEVELOPMENT OF A RECTANGULAR BOX

Fig. 69 represents a rectangular box to be made from sheet stock. It is required to calculate the stock dimensions, mark the stock and cut out the development. It is normal to indicate in the drawings the overall (external) dimensions, the thickness of the material and the inside radius of curvature which is all that is necessary for computing the stock dimensions. Fig. 69a represents the box in three projections, the following sizes being given:

- 1. Thickness of the material = 1.5 mm
- 2. Box width = 180 mm
- 3. Length = 250 mm
- 4. Height of sides = 40 mm.

By using the above methods, formulae and tables the stock dimensions (width and length) can be calculated. First determine the width and length of the straight sections: width = 35.5 + 171 + 35.5 = 242

length = 35.5 + 241 + 35.5 = 312

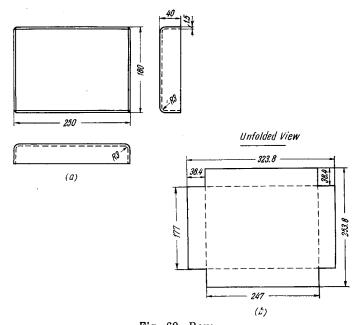


Fig. 69. Box:
(a) drawing of the box in three projections; (b) box development

Add the length of the neutral lines. The neutral line radius is 3.75 mm, hence the length of the neutral lines for two radii will be $3.75 \times 3.14 = 11.8$ mm; therefore

stock width = 242 + 11.8 = 253.8stock length = 312 + 11.8 = 323.8

On calculating the stock dimensions, start laying them out in imagination. The development configuration can be visualized by mentally unbending the sides, turning the part into a flat figure and drawing it according to the dimensions. The development of a rectangular box is given in Fig. 69b.

How to Find the Size of a Pulley.— In order to run any farm machine at its proper speed, that is the speed which the manufacturer recommends as the best, you must be able to calculate the size of the pulley needed on the machine.

The pulley on your tractor is, of course, of a fixed size and if you want to run, say, an ensilage cutter at a given speed, a *ratio* between the sizes of the tractor pulley and the ensilage cutter pulley must be had. You can easily find the size needed by using the following formula:

Now let us take an example. An ensilage cutter, or other machine, is to be run at a speed of 800 r. p. m., by a tractor whose pulley is 16 inches in diameter and which is driven at a speed of 400 r. p. m. What must be the size of the pulley on the ensilage cutter or other machine?

Substituting now the known figures for the formula above we have

$$\begin{array}{c}
\text{Diameter of} \\
\text{Machine Pulley} = \frac{16 \times 400}{800}
\end{array}$$

or worked out

Diameter of Machine Pulley =
$$\frac{6400}{800}$$
 = 8 inches

and 8 inches is the diameter of the pulley you want on your ensilage cutter or other machine.

How to Find the Belt Speed.—The belt speed of your tractor is the rate of travel of any one point on the belt and it is measured in feet per minute. You can find it by the following formula:

where the diameter of the tractor pulley \times 3.1416 = the circumference of the tractor pulley in inches.

As an example, suppose the diameter of the tractor pulley is 18 inches and its speed is 550 r. p. m. Substituting these figures in the formula we have,

Belt Speed =
$$\frac{18 \times 3.1416 \times 550}{12}$$

or,

Belt Speed =
$$\frac{31,200}{12}$$
 = 2,600 feet,

and 2,600 feet is the speed of the belt in feet per minute.

PULLEY SPEEDS. The principle applied to gearing in regard to the ratio between the speeds of two shafts may be directly applied to pulleys, with the only difference that the number of inches to the diameter of the pulley should be substituted for the number of teeth in the gear. (See GEAR TRAINS.)

Assume that a shaft is required to make 300 revolutions per minute, and that it is driven from a lineshaft making 180 revolutions per minute, as indicated in Fig. 1. The pulley on the lineshaft is 15 inches in diameter. should the diameter of the pulley on the shaft making 300 revolutions per minute be made? As the belt on the two pulleys runs at the same speed as the periphery (circumference) of either of the pulleys, it is clear that the peripheries of both pulleys run at the same speed, providing there is no slip between the belt and the pulleys. The pulley running a smaller number of revolutions must be larger in order that its periphery may run at the same speed as the periphery of the pulley making a greater number of revolutions. The circumference of a circle (and, therefore, also the circumference of a pulley) equals the diameter × 3.1416. Therefore, the circumference of the pulley making 180 revolutions and having a diameter of 15 inches, passes, in one minute, through a distance equal to 180 times its circumference, or 180 \times 15 \times 3.1416.

The circumference of the pulley making 300 revolutions must pass through the same distance in one minute; therefore, for each revolution, this pulley must pass through the distance $180 \times 15 \times 3.1416$ divided by 300. This, then, would equal the circumference of the smaller pulley; but the circumference also equals the diameter \times 3.1416. Therefore:

$$\frac{180 \times 15 \times 3.1416}{300} = \text{diameter of smaller pulley} \times 3.1416.$$

As 3.1416 enters as a factor on both sides of the equals sign, it can be canceled. Then:

$$\frac{180 \times 15}{300} = \text{diameter of smaller pulley}.$$

From this, the following rule for the relation between the sizes of pulleys and the number of revolutions of two shafts can be formulated:

The number of revolutions of one shaft multiplied by the diameter of the pulley on the same shaft, divided by the number of revolutions of the second shaft, gives the diameter of the pulley on the second shaft.

This rule can be expressed as a formula:

Diameter of pulley on second shaft = revolutions of first shaft × diam. of pulley on first shaft revolutions of second shaft

If one pulley makes 200 revolutions while another pulley makes 100 revolutions, the *speed ratio* between the two pulleys is 2 to 1. If one pulley makes 200 revolutions while another makes 50 revolutions, the speed ratio is 4 to 1, because one shaft makes four times as many revolutions as the other. If one shaft runs at 200 revolutions and another at 140 revolutions, the speed ratio would be 200 to 140. By canceling equal factors in 200 and 140,

reduce the ratio so as to express it with smaller numbers. In this case the ratio would be 10 to 7, because $\frac{240}{100} = \frac{24}{100}

If very accurate results are required, one thickness of the belt should be added to the diameter of the pulley itself, and the dimension thus obtained should be used in the preceding formulas instead of the diameter of the pulley rim. If the pulley is 5 inches in diameter and the belt $\frac{1}{2}$ inch thick, the diameter to be used in the formulas should be $5\frac{1}{2}$ inches. The results obtained in this manner will be very accurate provided there is no slipping of the belt on either of the pulleys. For ordinary practical purposes, however, it is customary to figure with the diameter of the pulley rim, taking no account of the thickness of the belt.

The following rules apply to the practical questions relating to pulley speeds and diameters that are most frequently met with in shop installations.

Speed of Driven Pulley Required. — Diameter and speed of driving pulley, and diameter of driven pulley are known. *Rule:* Multiply the diameter of the driving pulley by its speed in revolutions per minute, and divide the product by the diameter of the driven pulley.

Example: — If the diameter of the driving pulley is 15 inches and its speed, 180 revolutions per minute, and the

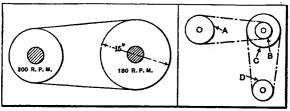


Fig. 1

Fig. 2

diameter of the driven pulley, 9 inches, then the speed of the driven pulley = $\frac{15 \times 180}{9}$ = 300 revolutions per minute.

Diameter of Driven Pulley Required. — Diameter and speed of driving pulley, and revolutions per minute of driven pulley are known. *Rule:* Multiply the diameter of the driving pulley by its speed in revolutions per minute, and divide the product by the required speed of the driven pulley.

Example: — If the diameter of the driving pulley is 24 inches and its speed, 100 revolutions per minute, and the driven pulley is to rotate 600 revolutions per minute, then the diameter of the driven pulley = $\frac{24 \times 100}{600}$ = 4 inches.

Diameter of Driving Pulley Required. — Diameter and speed of driven pulley, and speed of driving pulley are known. *Rule:* Multiply the diameter of the driven pulley by its speed in revolutions per minute, and divide the product by the speed of the driving pulley.

Example: — If the diameter of the driven pulley is 36 inches and its required speed, 150 revolutions per minute, and the speed of the driving pulley is 600 revolutions per minute, then the diameter of the driving pulley

$$= \frac{36 \times 150}{600} = 9 \text{ inches.}$$

Speed of Driving Pulley Required. — Diameters of driving and driven pulleys, and speed of driven pulley are known. *Rule:* Multiply the diameter of the driven pulley by its speed, and divide the product by the diameter of the driving pulley.

Example:—If the diameter of the driven pulley is 4 inches, its required speed, 800 revolutions per minute, and the diameter of the driver, 26 inches, then the required speed of the driver = $\frac{4 \times 800}{26}$ = 123 revolutions per minute, approximately.

Speed of Driven Pulley in Compound Drive Required. — Diameters of pulleys A, B, C, and D (see Fig. 2), and speed of pulley A are known; find speed of pulley D. Rule: Divide product of diameters of driving pulleys by product of diameters of driven pulleys, and multiply quotient by speed of first driving pulley.

Example:—If the diameters of the driving pulleys A and C are 18 and 24 inches; the diameters of the driven pulleys B and D, 12 and 13 inches; and the speed of the driver A, 260 revolutions per minute; then the speed of the driven pulley D equals:

$$\frac{18 \times 24}{12 \times 13} \times 260 = 720$$
 revolutions per minute.

Pulley Diameters in Compound Drive Required. — Speeds of driving and driven pulleys are known; find diameters of the four pulleys A, B, C, and D. Rule: Place the speed of the driving pulley as the numerator of a fraction, and the speed of driven pulley as the denominator, and reduce this fraction to its lowest terms; then resolve both the numerator and denominator into two factors, and multiply each "pair" of factors (a pair being one factor in the numerator and one in the denominator) by a trial number which will give pulleys of suitable diameters.

Example: — If the speed of pulley A is 260 revolutions per minute, and the required speed of pulley D is 720 revolutions per minute, find the diameters of the four pulleys. The fraction $\frac{360}{25}$ reduced to its lowest terms is $\frac{1}{15}$, which represents the required speed ratio. Resolve $\frac{13}{15}$ into two factors; $\frac{13}{36} = \frac{1 \times 13}{2 \times 18}$. Multiply by trial numbers 12 and 1:

$$\frac{(1 \times 12) \times (13 \times 1)}{(2 \times 12) \times (18 \times 1)} = \frac{12 \times 13}{24 \times 18}$$

The values 12 and 13 in the numerator represent the diameters of the *driven* pulleys B and D, and values 24 and 18 in the denominator, the diameters of the *driving* pulleys.

Length of Belt on Pulleys. — A simple rule, which can be used with fair accuracy when the pulley diameters are nearly equal, is as follows: Add the diameters of the two pulleys, divide the sum by 2, and multiply the quotient by $3\frac{1}{2}$; then add to the product twice the distance between the centers of the shafts. Expressing this rule as a formula, in which D = diameter of large pulley; d = diameter of small pulley; C = center distance between shafts; L = belt length:

$$L = \frac{D+d}{2} \times 3^{\frac{1}{2}} + 2 C.$$

Example: — Diameter of large pulley equals 15 inches; diameter of small pulley equals 13 inches. The center distance is 92 inches. Find length of belt.

$$L = \frac{15+13}{2} \times 3\frac{1}{7} + 2 \times 92 = 228$$
 inches.

SIMPLE INTEREST TABLE

| Amount | and Time | 4% | 5% | 6% | 7% | 8% |
|--|--|--|--|--|---|--|
| \$1.00 \$1.00 \$1.00 \$1.00 \$1.00 \$100.00 \$100.00 \$100.00 \$100.00 \$100.00 \$100.00 \$100.00 \$100.00 | 1 month 2 months 3 months 6 months 12 months 12 months 1 day 2 days 3 days 4 days 5 days 6 days 1 month 2 months 3 months 6 months | \$.003 .007 .011 .020 .040 .011 .022 .034 .045 .056 .067 .334 .667 1.000 | \$.004 .008 .013 .025 .050 .013 .027 .041 .053 .069 .083 .416 .832 1.250 | \$.005 .010 .015 .030 .060 .016 .032 .050 .066 .082 .100 .500 1.500 | \$.005 .011 .017 .035 .070 .019 .038 .058 .077 .097 .116 .583 1.166 1.750 | \$.006 .013 .020 .040 .080 .022 .044 .067 .089 .111 .133 .667 1.333 2.000 4,000 |
| \$100.00 | 12 months | 4.000 | 5.000 | 6.000 | 7.000 | 8.000 |

TO FIND THE INTEREST ON ANY SUM FOR ANY TIME

Point off two places from the right of the principal and multiply it by the number of months. One-half the result is the interest at 6 percent.

Deduct one-sixth for 5 percent; one-tiple for 4 percent; add one-sixth for

the number of months. One-half the result is the interest at 6 percent. Deduct one-sixth for 5 percent; one-third for 4 percent; add one-sixth for 7 percent; one-third for 8 percent, etc.

VI. Compound Interest

31 %

3 %

1.0950 1.0900 1.0950

21 %

2 %

2.2522

2.2972

2.3432

2,3901

2.4379

2.5363

2.5871

2.6916

42

43

45 2.4866

48

49 2.6388 2.7522

2.8210

2.8915

2.9638

3.0379

3.1139

3.1917

3.2715

3.3533

3.4371

3.3599

3.4607

3.5645

3.6715

3.7816

3.8950

4.0119

4.1323

4.2562

4.3839

4.0978

4.2413

4.3897

4.5433

4.7024

4.8669

5.0373

5.2136

5.3961

5.5849

4.9931

5.1928

5.4005

5.6165

5.8412

6.0748

6.3178

6.5705

6.8333

7.1067

6.0781

6.3516

6.6374

6.9361

7.2482

7.5744

7.9153

8.2715

8.6437

9.0326

7.3920

7.7616

8.1497

8.5572

8.9850

9.4343

9.9060

10.4013

10.9213

11.4674

10.9029

11.5570

12,2505

12.9855

13.7646

14.5905

15,4659

16.3939

17.3775

18.4202

Compound Interest: $(1+r)^n$

41 %

1 0400 1 0450

5 %

1.0500

6 %

7 %

16.0227

17.1443

18.3444

19.6285

21.0025

22.4726

24.0457

25.7289

27.5299

29,4570

Amount of One Dollar Principal at Compound Interest Aprel 7 Years 4 %

| 1 | 1.0200 | 1.0250 | 1.0300 | 1.0350 | 1.0400 | 1.0450 | 1.0500 | 1.0600 | 1.0700 |
|----|--------|--------|--------|--------|--------|--------|--------|---------|---------|
| 2 | 1.0404 | 1.0506 | 1.0609 | 1.0712 | 1.0816 | 1.0920 | 1.1025 | 1.1236 | 1.1449 |
| 3 | 1.0612 | 1.0769 | 1.0927 | 1.1087 | 1.1249 | 1.1412 | 1.1576 | 1.1910 | 1.2250 |
| 4 | 1.0824 | 1.1038 | 1.1255 | 1.1475 | 1.1699 | 1.1925 | 1.2155 | 1.2625 | 1.3108 |
| 5 | 1.1041 | 1.1314 | 1.1593 | 1.1877 | 1.2167 | 1.2462 | 1.2763 | 1.3382 | 1.4026 |
| 6 | 1.1262 | 1.1597 | 1.1941 | 1.2293 | 1.2653 | 1.3023 | 1.3401 | 1.4185 | 1.5007 |
| 7 | 1.1487 | 1.1887 | 1.2299 | 1.2723 | 1.3159 | 1.3609 | 1.4071 | 1.5036 | 1.6058 |
| 8 | 1.1717 | 1.2184 | 1.2668 | 1.3168 | 1.3686 | 1.4221 | 1.4775 | 1.5938 | 1.7182 |
| 9 | 1.1951 | 1.2489 | 1.3048 | 1.3629 | 1.4233 | 1.4861 | 1.5513 | 1.6895 | 1.8385 |
| 10 | 1.2190 | 1.2801 | 1.3439 | 1.4106 | 1.4802 | 1.5530 | 1.6289 | 1.7908 | 1.9672 |
| 11 | 1.2434 | 1.3121 | 1.3842 | 1.4600 | 1.5395 | 1.6229 | 1.7103 | 1.8983 | 2.1049 |
| 12 | 1.2682 | 1.3449 | 1.4258 | 1.5111 | 1.6010 | 1.6959 | 1.7959 | 2.0122 | 2.2522 |
| 13 | 1.2936 | 1.3785 | 1.4685 | 1.5640 | 1.6651 | 1.7722 | 1.8856 | 2.1329 | 2.4098 |
| 14 | 1.3195 | 1.4120 | 1.5126 | 1.6187 | 1.7317 | 1.8519 | 1.9799 | 2.2609 | 2.5785 |
| 15 | 1.3459 | 1.4483 | 1.5580 | 1.6753 | 1.8009 | 1.9353 | 2.0789 | 2.3966 | 2.7590 |
| 16 | 1.3728 | 1.4845 | 1.6047 | 1.7340 | 1.8730 | 2.0224 | 2.1829 | 2.5404 | 2.9522 |
| 17 | 1.4002 | 1.5216 | 1.6528 | 1.7947 | 1.9479 | 2.1134 | 2.2920 | 2.6928 | 3.1588 |
| 18 | 1.4282 | 1.5597 | 1.7024 | 1.8575 | 2.0258 | 2.2085 | 2.4066 | 2.8543 | 3.3799 |
| 19 | 1.4568 | 1.5987 | 1.7535 | 1.9225 | 2.1068 | 2.3079 | 2.5270 | 3.0256 | 3.6165 |
| 20 | 1.4859 | 1.6386 | 1.8061 | 1.9898 | 2.1911 | 2.4117 | 2.6533 | 3.2071 | 3.8697 |
| 21 | 1.5157 | 1.6796 | 1.8603 | 2.0594 | 2.2788 | 2.5202 | 2.7860 | 3.3996 | 4.1406 |
| 22 | 1.5460 | 1.7216 | 1.9161 | 2.1315 | 2.3699 | 2.6337 | 2.9253 | 3.6035 | 4.4304 |
| 23 | 1.5769 | 1.7646 | 1.9736 | 2.2061 | 2.4647 | 2.7522 | 3.0715 | 3.8197 | 4.7405 |
| 24 | 1.6084 | 1.8087 | 2.0328 | 2.2833 | 2.5633 | 2.8760 | 3.2251 | 4.0489 | 5.0724 |
| 25 | 1.6406 | 1.8539 | 2.0938 | 2.3632 | 2.6658 | 3.0054 | 3.3864 | 4.2919 | 5.4274 |
| 26 | 1.6734 | 1.9003 | 2.1566 | 2.4460 | 2.7725 | 3.1407 | 3.5557 | 4.5494 | 5.8074 |
| 27 | 1.7069 | 1.9478 | 2.2213 | 2.5316 | 2.8834 | 3.2820 | 3.7335 | 4.8223 | 6.2139 |
| 28 | 1.7410 | 1.9965 | 2.2879 | 2.6202 | 2.9987 | 3.4297 | 3.9201 | 5.1117 | 6.6488 |
| 29 | 1.7758 | 2.0464 | 2.3566 | 2.7119 | 3.1187 | 3.5840 | 4.1161 | 5.4184 | 7.1143 |
| 30 | 1.8114 | 2.0976 | 2.4273 | 2.8068 | 3.2434 | 3.7453 | 4.3219 | 5.7435 | 7.6123 |
| 31 | 1.8476 | 2.1500 | 2.5001 | 2.9050 | 3.3731 | 3.9139 | 4.5380 | 6.0881 | 8.1451 |
| 32 | 1.8845 | 2.2038 | 2.5751 | 3.0067 | 3.5081 | 4.0900 | 4.7649 | 6.4534 | 8.7153 |
| 33 | 1.9222 | 2.2589 | 2.6523 | 3.1119 | 3.6484 | 4.2740 | 5.0032 | 6.8406 | 9.3253 |
| 34 | 1.9607 | 2.3153 | 2.7319 | 3.2209 | 3.7943 | 4.4664 | 5.2533 | 7.2510 | 9.9781 |
| 35 | 1.9999 | 2.3732 | 2.8139 | 3.3336 | 3.9461 | 4.6673 | 5.5160 | 7.6861 | 10.6766 |
| 36 | 2.0399 | 2.4325 | 2.8983 | 3.4503 | 4.1039 | 4.8774 | 5.7918 | 8.1473 | 11.4239 |
| 37 | 2.0807 | 2.4933 | 2.9852 | 3.5710 | 4.2681 | 5.0969 | 6.0814 | 8.6361 | 12.2236 |
| 38 | 2.1223 | 2.5557 | 3.0748 | 3.6960 | 4.4388 | 5.3262 | 6.3855 | 9.1543 | 13.0793 |
| 39 | 2.1647 | 2.6196 | 3.1670 | 3.8254 | 4.6164 | 5.5659 | 6.7048 | 9.7035 | 13.9948 |
| 40 | 2.2080 | 2.6851 | 3.2620 | 3.9593 | 4.8010 | 5.8164 | 7.0400 | 10.2857 | 14.9745 |

Investment appraisal

Appraisal for investment usually means considering the rates of return for various projects and selecting the one with the 'best' return. Methods of appraisal for investment depend first on the estimation of the net cash flow from an investment, where all taxes, subsidies, grants, etc., have been allowed for in estimating the cash flow. Methods differ according to the way in which the flows of cash over time are related to the initial investment:

Rate of return = the total of the estimated cash flows over the life of the investment, divided by the number of years life, and expressed as a percentage of the investment. Where a unit of 100 is invested to give the following net cash flows over 10 years: 1, 10.0; 2, 11.0; 3, 12.1; 4, 13.3; 5, 14.6; 6, 16.1; 7, 17.7; 8, 19.5; 9, 21.4; 10, 23.6; then:

the crude rate of return is the total of those flows = 159.3, divided by 10 = 15.93, which is 15.93% as a percentage of the 100 units originally invested.

Pay back = the number of years after which the original investment would have been recouped. In the above example, this would be after year 8, when a cumulative amount of 114.3 would have been received net.

Discounted cash flow

The above two methods make no allowance for the time factor in the cash flows; as any sum could be earning interest in an alternative investment, it is more realistic to 'discount' the cash flows to be received in future years by an expected rate of interest. Tables for the amount accumulated by 1 unit at different rates of interest and for different periods are included on pages 208–211. The 'discount factor', giving the present value of any future amount allowing for the rate of interest concerned, is the reciprocal of the figure in the accumulation tables. A special table of discount factors is included on the facing page.

The following table shows the effect of 'discounting' the cash flows in the above example at interest rates of 5% and 10%; this follows the convention of regarding the first year as not subject to discounting, so that year 2 is discounted at the rate for 1 year as shown in the discount factor table. Further, the convention of regarding all receipts and payments as taking place on one day of each year is adopted.

| Period | Net | Interest at | 5% | Interest at | 10% |
|--------|-----------|-----------------|------------------|-----------------|------------------|
| | cash flow | Discount factor | Present value | Discount factor | Present value |
| 1 | 10.0 | 1.0000 | 10.0 | 1.0000 | 10.0 |
| 2 | 11.0 | 0.9524 | 10.5 | 0.9091 | 10.0 |
| 3 | 12.1 | 0.9070 | 11.0 | 0.8264 | 10.0 |
| 4 | 13.3 | 0.8638 | 11.5 | 0.7513 | 10.0 |
| 5 | 14.6 | 0.8227 | 12.0 | 0.6830 | 10.0 |
| 6 | 16.1 | 0.7835 | 12.6 | 0.6209 | 10.0 |
| 7 | 17.7 | 0.7462 | 13.2 | 0.5645 | 10.0 |
| 8 | 19.5 | 0.7107 | 13.9 | 0.5132 | 10.0 |
| 9 | 21.4 | 0.6768 | 14.5 | 0.4665 | 10.0 |
| 10 | 23.6 | 0.6446 | 15.2 | 0.4241 | 10.0 |

The total cash flow at present value is 124.4 discounted at 5%, and 100 discounted at 10%, compared with the crude total flow of 159.3. Assuming an interest rate of 5% the investment of 100 units will give a 'profit' of 24.4, and assuming an interest rate of 10%, the investment of 100 gives a return of exactly 100, so it yields no profit at that rate of interest (this is because the net cash flows used in the example are the same as the amount accumulated from 10 at 10% p.a., as indicated in the table on page 210).

Where the present value of the flow of cash, discounted at a certain rate, exactly equals the initial amount of investment, that rate is sometimes called the DCF 'solution' rate, since it is the rate of return given by the investment made. In the above example, 10% is the DCF solution rate. DCF solution rates are usually calculated by interpolation from rates which are approximately known.

Where the investment is also spread over more than one period, allowance is also made for discounting the investment payments. In the following example the effect of spreading a 100 unit investment over 3 periods is illustrated, discounting taking place at the DCF solution rate which differs accordingly.

| Period | Investment | in 1 period | Investment in 3 periods | | | |
|------------|------------------|------------------|-------------------------|------------------|--|--|
| | Net cash flow | Present value | Net cash flow | Present value | | |
| Investment | | | | | | |
| 1 | 100 | 100 | 25 | 25.0 | | |
| 2 | | | 50 | 37.8 | | |
| 2 3 | | | 25 | 14.3 | | |
| Returns | | | | | | |
| 1 | 20 | 20.0 | 20 | 20.0 | | |
| 2 3 | 20 | 16.6 | 20 | 15.1 | | |
| 3 | 20 | 13.8 | 20 | 11.5 | | |
| 4 | 20 | 11.5 | 20 | 8.7 | | |
| 5 | 20 | 9.6 | 20 | 6.6 | | |
| 6 | 20 | 8.0 | 20 | 5.0 | | |
| 7 | 20 | 6.6 | 20 | 3.8 | | |
| 8 | 20 | 5.5 | 20 | 2.8 | | |
| 9 | 20 | 4.6 | 20 | 2.2 | | |
| 10 | 20 | 3.8 | 20 | 1.6 | | |

The total discounted amount or present value is 100 for the 1 period investment example, with a DCF solution rate of 20.3%; for the example with investment over 3 periods, the total discounted amount is 77.2 units (since investment flows are also discounted) with a DCF solution rate of 32.2%. The higher rate is obtained because the investment does not need to be made immediately, but the returns are nevertheless the same.

The basic formula for computing a present value is:

$$\frac{B_t}{(1+r)^t}$$

where B_t is the benefit in year t and r is the discount rate. The same formula would hold for costs – simply substituting C for B. The general formula for computing a present value of a set of benefits and costs that occur through time, known as a **net present value** (NPV) would be:

$$\sum_{t} \frac{B_{t} - C_{t}}{(1+r)^{t}}$$

The CBA rule then, is that for any policy or project, the NPV should be positive.

To illustrate the above rule, consider a project that has the following sequence of costs and benefits:

| | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 |
|-------------|--------|------------|--------|--------|--------|
| Cost | 30 | 10 | 0 | 0 | 0 |
| Benefit | 0 | 5 | 15 | 15 | 15 |
| Net benefit | -30 | - 5 | 15 | 15 | 15 |

Note that costs appear as minuses and benefits as pluses. Suppose the discount rate, r, is 10 per cent (which is written as 0.1). Then the computation is:

$$-30/1.1 - 5/(1.1)^2 + 15/(1.1)^3 + 15/(1.1)^4 + 15(1.1)^5$$

Typically this would be done with a discounted cash flow computer program, but in this case the calculations are simple:

$$-27.3 - 4.1 + 11.3 + 10.3 + 9.3 = -0.5$$

The NPV is negative and therefore the project is not worthwhile. Notice that without the discounting procedure, benefits of 45 exceed costs of 35. Discounting can therefore make a big difference to the ultimate decision to accept or reject a project.

The choice faced by a decision-maker may be a simple 'accept/reject' decision like the one above, but it may also be one of choosing between competing alternatives, e.g. a hydroelectric power plant or a coal-fired plant or a nuclear power station. If each option has a positive NPV, the choice should be made on the basis of the highest NPV. Yet another decision context arises where a number of projects can be chosen but the budget available is limited. The rule then is to *rank* the projects according to the *ratio* of the PV of benefits to the PV of costs (the 'benefit-cost ratio') and work down the ranked list until the budget is exhausted.

The practice of *discounting* arises because individuals attach less weight to a benefit or cost in the future than they do to a benefit or cost now. Impatience, or 'time preference', is one reason why the present is preferred to the future. The second reason is that, since capital is productive, £1's worth of resources now will generate more than a £1's worth of goods and services in the future. Hence an entrepreneur would be willing to pay more than £1 in the future to acquire £1's worth of these resources now. This argument for discounting is referred to as the 'marginal productivity of capital' argument, the use of the word 'marginal' indicating that it is the productivity of additional units of capital that is relevant.

0.0006

50

0.0004

0.0003

0.0002

0.0001

| Rate of nterest: % 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | |
|--------------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|--------|--------|--------|--------|--------|------------------|------------------|-----|
| | | | | | | | | | | | | | | | , |
| 'ears | | | | | | | | | | | | | | | Yea |
| 1 0.9901 | 0.9804 | 0.9709 | 0.9615 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.9009 | 0.8929 | 0.8850 | 0.8772 | 0.8696 | |
| 2 0.9803 | 0.9612 | 0.9426 | 0.9246 | 0.9070 | 0.8900 | 0.8734 | 0.8573 | 0.8417 | 0.8264 | 0.8116 | 0.7972 | 0.7831 | 0.7695 | 0.7561 | |
| 0.9706 | 0.9423 | 0.9151 | 0.8890 | 0.8638 | 0.8396 | 0.8163 | 0.7938 | 0.7722 | 0.7513 | 0.7312 | 0.7118 | 0.6931 | 0.6750 | 0.6575 | |
| 0.9610 | 0.9238 | 0.8885 | 0.8548 | 0.8227 | 0.7921 | 0.7629 | 0.7350 | 0.7084 | 0.6830 | 0.6587 | 0.6355 | 0.6133 | 0.5921 | 0.5718 | |
| 0.9515 | 0.9057 | 0.8626 | 0.8219 | 0.7835 | 0.7473 | 0.7130 | 0.6806 | 0.6499 | 0.6209 | 0.5935 | 0.5674 | 0.5428 | 0.5194 | 0.4972 | |
| 0.9420 | 0.8880 | 0.8375 | 0.7903 | 0.7462 | 0.7050 | 0.6663 | 0.6302 | 0.5963 | 0.5645 | 0.5346 | 0.5066 | 0.4803 | 0.4556 | 0.4323 | |
| 0.9420 | 0.8706 | 0.8131 | 0.7599 | 0.7107 | 0.6651 | 0.6227 | 0.5835 | 0.5470 | 0.5132 | 0.4817 | 0.4523 | 0.4251 | 0.3996 | 0.3759 | |
| | 0.8535 | 0.7894 | 0.7307 | 0.6768 | 0.6274 | 0.5820 | 0.5403 | 0.5019 | 0.4665 | 0.4339 | 0.4039 | 0.3762 | 0.3506 | 0.3269 | |
| | | 0.7664 | 0.7026 | 0.6446 | 0.5919 | 0.5439 | 0.5002 | 0.4604 | 0.4241 | 0.3909 | 0.3606 | 0.3329 | 0.3075 | 0.2843 | |
| 0.9143 | 0.8368 0.8203 | 0.7441 | 0.7026 | 0.6139 | 0.5584 | 0.5083 | 0.4632 | 0.4224 | 0.3855 | 0.3522 | 0.3220 | 0.3323 | 0.3673 | 0.2472 | |
| 0.0000 | 0.0042 | 0.7224 | 0.6496 | 0.5847 | 0.5268 | 0.4751 | 0.4289 | 0.3875 | 0.3505 | 0.3173 | 0.2875 | 0.2607 | 0.2366 | 0.2149 | |
| 0.8963 0.8874 | 0.8043 0.7885 | 0.7224 0.7014 | 0.6246 | 0.5568 | 0.3208 | 0.4440 | 0.4269 | 0.3555 | 0.3303 | 0.3173 | 0.2567 | 0.2307 | 0.2076 | 0.2149 | |
| | | | | | 0.4688 | 0.4150 | 0.3677 | 0.3362 | 0.2897 | 0.2575 | 0.2292 | 0.2042 | 0.1821 | | |
| 3 0.8787 | 0.7730 | 0.6810 | 0.6006 | 0.5303 | | | | | | | | | | 0.1625 | |
| 4 0.8700 | 0.7579 | 0.6611 | 0.5775 | 0.5051 | 0.4423 | 0.3878 | 0.3405 | 0.2992 | 0.2633 | 0.2320 | 0.2046 | 0.1807 | 0.1597 | 0.1413 | |
| 0.8613 | 0.7430 | 0.6419 | 0.5553 | 0.4810 | 0.4173 | 0.3624 | 0.3152 | 0.2745 | 0.2394 | 0.2090 | 0.1827 | 0.1599 | 0.1401 | 0.1229 | |
| 0.8528 | 0.7284 | 0.6232 | 0.5339 | 0.4581 | 0.3936 | 0.3387 | 0.2919 | 0.2519 | 0.2176 | 0.1883 | 0.1631 | 0.1415 | 0.1229 | 0.1069 | |
| 7 0.8444 | 0.7142 | 0.6050 | 0.5134 | 0.4363 | 0.3714 | 0.3166 | 0.2703 | 0.2311 | 0.1978 | 0.1696 | 0.1456 | 0.1252 | 0.1078 | 0.0929 | |
| 0.8360 | 0.7002 | 0.5874 | 0.4936 | 0.4155 | 0.3503 | 0.2959 | 0.2502 | 0.2120 | 0.1799 | 0.1528 | 0.1300 | 0.1108 | 0.0946 | 0.0808 | |
| 9 0.8277 | 0.6864 | 0.5703 | 0.4746 | 0.3957 | 0.3305 | 0.2765 | 0.2317 | 0.1945 | 0.1635 | 0.1377 | 0.1161 | 0.0981 | 0.0829 | 0.0703 | |
| 0.8195 | 0.6730 | 0.5537 | 0.4564 | 0.3769 | 0.3118 | 0.2584 | 0.2145 | 0.1784 | 0.1486 | 0.1240 | 0.1037 | 0.0868 | 0.0728 | 0.0611 | |
| 0.8114 | 0.6598 | 0.5375 | 0.4388 | 0.3589 | 0.2942 | 0.2415 | 0.1987 | 0.1637 | 0.1351 | 0.1117 | 0.0926 | 0.0768 | 0.0638 | 0.0531 | |
| 0.8034 | 0.6468 | 0.5219 | 0.4220 | 0.3418 | 0.2775 | 0.2257 | 0.1839 | 0.1502 | 0.1228 | 0.1007 | 0.0826 | 0.0680 | 0.0560 | 0.0462 | |
| | 0.6342 | 0.5067 | 0.4057 | 0.3256 | 0.2618 | 0.2109 | 0.1703 | 0.1378 | 0.1117 | 0.0907 | 0.0738 | 0.0601 | 0.0491 | 0.0402 | |
| | | | | | 0.2470 | 0.1971 | 0.1577 | 0.1264 | 0.1015 | 0.0307 | 0.0659 | 0.0532 | | | |
| 0.7876 0.7798 | 0.6217 0.6095 | 0.4919 0.4776 | 0.3901 0.3751 | 0.3101 0.2953 | 0.2330 | 0.1842 | 0.1377 | 0.1264 | 0.1013 | 0.0736 | 0.0588 | 0.0332 | 0.0431 0.0378 | 0.0349 0.0304 | |
| | | | | 0.004.4 | 0.1741 | 0.1214 | 0.0004 | 0.0754 | 0.0572 | 0.0427 | 0.0224 | 0.0350 | 0.0100 | 0.0151 | |
| 0 0.7419 | 0.5521 | 0.4120 | 0.3083 | 0.2314 | 0.1741 | 0.1314 | 0.0994 | 0.0754 | 0.0573 | 0.0437 | 0.0334 | 0.0256 | 0.0196 | 0.0151 | |
| 0.6717 | 0.4529 | 0.3066 | 0.2083 | 0.1420 | 0.0972 | 0.0668 | 0.0460 | 0.0318 | 0.0221 | 0.0154 | 0.0107 | 0.0075 | 0.0053 | 0.0037 | |
| 0.6080 | 0.3715 | 0.2281 | 0.1407 | 0.0872 | 0.0543 | 0.0339 | 0.0213 | 0.0134 | 0.0085 | 0.0054 | 0.0035 | 0.0022 | 0.0014 | 0.0009 | |
| Rate of nterest: % 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | |
| | | | | | | | | | | | | | | | Ye |
| ears | | | | | 0.0004 | 0.04.07 | 0.0400 | 0.0005 | 0.0000 | 0.7027 | 0.7074 | 0.7012 | 0.7750 | | тe |
| 1 0.8621 | 0.8547 | 0.8475 | 0.8403 | 0.8333 | 0.8264 | 0.8197 | 0.8130 | 0.8065 | 0.8000 | 0.7937 | 0.7874 | 0.7812 | 0.7752 | 0.7692 | |
| 2 0.7432 | 0.7305 | 0.7182 | 0.7062 | 0.6944 | 0.6830 | 0.6719 | 0.6610 | 0.6504 | 0.6400 | 0.6299 | 0.6200 | 0.6104 | 0.6009 | 0.5917 | |
| 3 0.6407 | 0.6244 | 0.6086 | 0.5934 | 0.5787 | 0.5645 | 0.5507 | 0.5374 | 0.5245 | 0.5120 | 0.4999 | 0.4882 | 0.4768 | 0.4658 | 0.4552 | |
| 4 0.5523 | 0.5337 | 0.5158 | 0.4987 | 0.4823 | 0.4665 | 0.4514 | 0.4369 | 0.4230 | 0.4096 | 0.3968 | 0.3844 | 0.3725 | 0.3611 | 0.3501 | |
| 5 0.476,1 | 0.4561 | 0.4371 | 0.4190 | 0.4019 | 0.3855 | 0.3700 | 0.3552 | 0.3411 | 0.3277 | 0.3149 | 0.3027 | 0.2910 | 0.2799 | 0.2693 | |
| 6 0.4104 | 0.3898 | 0.3704 | 0.3521 | 0.3349 | 0.3186 | 0.3033 | 0.2888 | 0.2751 | 0.2621 | 0.2499 | 0.2383 | 0.2274 | 0.2170 | 0.2072 | |
| 7 0.3538 | 0.3332 | 0.3139 | 0.2959 | 0.2791 | 0.2633 | 0.2486 | 0.2348 | 0.2218 | 0.2097 | 0.1983 | 0.1877 | 0.1776 | 0.1682 | 0.1594 | |
| 8 0.3050 | 0.2848 | 0.2660 | 0.2487 | 0.2326 | 0.2176 | 0.2038 | 0.1909 | 0.1789 | 0.1678 | 0.1574 | 0.1478 | 0.1388 | 0.1304 | 0.1226 | |
| 9 0.2630 | 0.2434 | 0.2255 | 0.2090 | 0.1938 | 0.1799 | 0.1670 | 0.1552 | 0.1443 | 0.1342 | 0.1249 | 0.1164 | 0.1084 | 0.1011 | 0.0943 | |
| 0.2267 | 0.2080 | 0.1911 | 0.1756 | 0.1615 | 0.1486 | 0.1369 | 0.1262 | 0.1164 | 0.1074 | 0.0992 | 0.0916 | 0.0847 | 0.0784 | 0.0725 | |
| 1 0.1954 | 0.1778 | 0.1619 | 0.1476 | 0.1346 | 0.1228 | 0.1122 | 0.1026 | 0.0938 | 0.0859 | 0.0787 | 0.0721 | 0.0662 | 0.0607 | 0.0558 | |
| | 0.1778 | 0.1013 | | | | | 0.0834 | 0.0757 | 0.0687 | 0.0625 | 0.0568 | 0.0517 | 0.0471 | 0.0429 | |
| 2 0.1685 | | | | | | | | | | | 0.0303 | 0.0317 | | 0.0429 | |
| 3 0.1452 | 0.1299 | 0.1163 | 0.1042 | 0.0935 | 0.0839 | 0.0754 | 0.0678 | 0.0610 | 0.0550 | 0.0496 | 0.0447 | | 0.0365 | | |
| 4 0.1252 | 0.1110 | 0.0985 | 0.0876 | 0.0779 | 0.0693 | 0.0618 | 0.0551 | 0.0492 | 0.0440 | 0.0393 | | 0.0316 | 0.0283 | 0.0254 | |
| 0.1079 | 0.0949 | 0.0835 | 0.0736 | 0.0649 | 0.0573 | 0.0507 | 0.0448 | 0.0397 | 0.0352 | 0.0312 | 0.0277 | 0.0247 | 0.0219 | 0.0195 | |
| 0.0930 | 0.0811 | 0.0708 | 0.0618 | 0.0541 | 0.0474 | 0.0415 | 0.0364 | 0.0320 | 0.0281 | 0.0248 | 0.0218 | 0.0193 | 0.0170 | 0.0150 | |
| 7 0.0802 | 0.0693 | 0.0600 | 0.0520 | 0.0451 | 0.0391 | 0.0340 | 0.0296 | 0.0258 | 0.0225 | 0.0197 | 0.0172 | 0.0150 | 0.0132 | 0.0116 | |
| 8 0.0691 | 0.0592 | 0.0508 | 0.0437 | 0.0376 | 0.0323 | 0.0279 | 0.0241 | 0.0208 | 0.0180 | 0.0156 | 0.0135 | 0.0118 | 0.0102 | 0.0089 | |
| 9 0.0596 | 0.0506 | 0.0431 | 0.0367 | 0.0313 | 0.0267 | 0.0229 | 0.0196 | 0.0168 | 0.0144 | 0.0124 | 0.0107 | 0.0092 | 0.0079 | 0.0068 | |
| 0.0514 | 0.0433 | 0.0365 | 0.0308 | 0.0261 | 0.0221 | 0.0187 | 0.0159 | 0.0135 | 0.0115 | 0.0098 | 0.0084 | 0.0072 | 0.0061 | 0.0053 | |
| 1 0.0443 | 0.0370 | 0.0309 | 0.0259 | 0.0217 | 0.0183 | 0.0154 | 0.0129 | 0.0109 | 0.0092 | 0.0078 | 0.0066 | 0.0056 | 0.0048 | 0.0040 | |
| | 0.0370 | 0.0303 | 0.0233 | 0.0217 | 0.0151 | 0.0126 | 0.0105 | 0.0088 | 0.0074 | 0.0062 | 0.0052 | 0.0044 | 0.0037 | 0.0031 | |
| 2 0.0382 | | | | 0.0151 | 0.0131 | 0.0128 | 0.0086 | 0.0033 | 0.0074 | 0.0002 | 0.0032 | 0.0034 | 0.0037 | 0.0031 | |
| 3 0.0329 | 0.0270 | 0.0222 | 0.0183 | | | | | 0.0071 | 0.0033 | 0.0049 | 0.0041 | 0.0034 | | 0.0024 | |
| 4 0.0284 5 0.0245 | 0.0231 0.0197 | 0.0188 0.0160 | 0.0154 0.0129 | 0.0126 0.0105 | 0.0103 0.0085 | 0.0085 0.0069 | 0.0070 0.0057 | 0.0057 | 0.0047 | 0.0039 | 0.0032 | 0.0027 | 0.0022 0.0017 | 0.0018 | |
| | | | | | | | | | | | | | | | |
| 0.0116 | 0.0090 | 0.0070 | 0.0054 | 0.0042 | 0.0033 | 0.0026 | 0.0020 | 0.0016 | 0.0012 | 0.0010 | 0.0008 | 0.0006 | 0.0005 | 0.0004 | |
| 0.0026 | 0.0019 | 0.0013 | 0.0010 | 0.0007 | 0.0005 | 0.0004 | 0.0003 | 0.0002 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0000 | 0.0000 | |
| 0.0006 | 0.0004 | 0.0003 | 0.0002 | 0.0001 | 0.0001 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | |

0.0000

0.0001

0.0000

0.0000

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0.0000

Step 6. Determining Cost Effectiveness*

The important economic consideration when designing a passive solar heated building is the trade-off between the cost of extra thermal mass and movable insulation (less the installed cost of the conventional construction it replaces) and the future cost of the fuel saved by the system over its lifetime. Operating and maintenance cost must also be included; however, for most passive systems this cost is negligible. The cost of solar heat can be estimated by the following formula:

$$cost of solar heat = \begin{array}{c} \left(\begin{array}{c} solar \\ system \times capital \ recovery \\ cost & factor \end{array} \right) \begin{array}{c} annual \ operating \\ and \ maintenance \\ cost \\ \hline annual \ solar \ heating \ contribution \ (Q_{c \ year}) \end{array} \right)$$

*Adapted from Los Alamos Scientific Laboratory, *Pacific Regional Solar Heating Handbook*. ERDA, San Francisco, California, 1976.

The *capital recovery factor* is determined from bankers' tables or formulas. It is defined as the value of capital to the individual. It may be the interest rate that your money would earn if you invested it, or the annual cost of a loan made to finance the extra cost of the passive system. For example, the capital recovery factor of a 10% 30-year loan is 0.106.

To illustrate the use of the formula, if we assume, for example, that

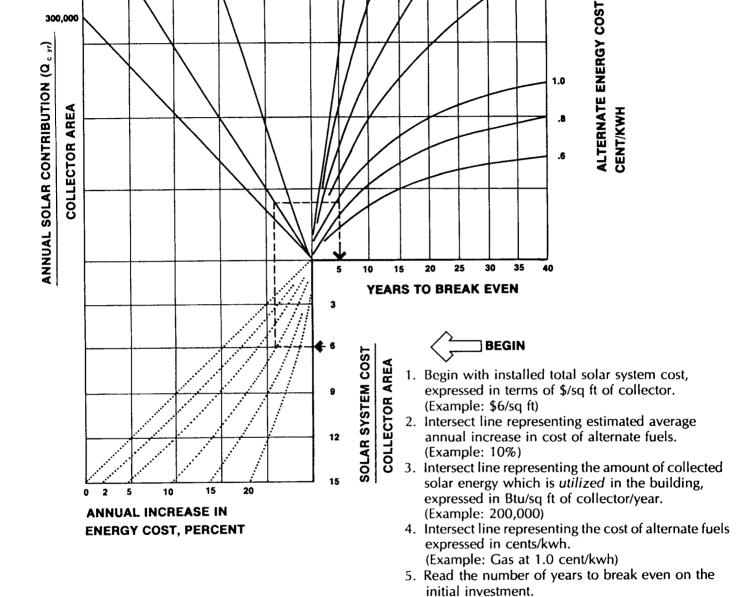
- —the passive solar heating system costs \$5,000 above installed conventional construction costs,
- —the capital recovery factor is 0.106 for a 30-year loan at 10% interest,
- —the operating and maintenance cost for the system is \$25 a year, and
- —the annual solar heating contribution is 100 million Btu's,

from the formula, the cost of solar heat is then:

cost of solar heat =
$$\frac{(\$5,000 \times 0.106) + \$25}{100 \text{ million Btu's}}$$
$$= \$5.55 \text{ per million Btu's}.$$

This figure does not take into account considerations that would make the cost less expensive, such as tax incentives, deduction of interest payments and business depreciation, or considerations that can make it more expensive, such as property tax evaluation increases and fuel cost deductions (business expense).

Another method for calculating the cost effectiveness of a system is the nomograph in figure 1-9. This method allows for the increase in future annual fuel costs to be included in the procedure. By plotting the cost of the system, the annual projected increase in energy costs, the annual solar heating contribution and the cost of conventional fuel, the nomograph computes the break-even time on the system's initial cost.



100,000

200,000

Fig. 1-9: Solar system cost nomograph.

Source: Adapted from GSA, "Energy Conservation Design Guidelines for New Office Buildings," as quoted by P.D. Maycock in "Solar Energy: The Outlook for Widespread Commercialization of Solar Heating and Cooling," ERDA.

(Example: 5 years)

Based on 8% interest, 1% maintenance/year.

Table 1-4 Capital Recovery Factors

| Years | Interest Rate |
|-------|---------------|

| | 51/2% | 6% | 7% | 8% | 10% | 12% | 15% |
|----|----------|----------|----------|----------|----------|----------|----------|
| 1 | 1.055 00 | 1.060 00 | 1.070 00 | 1.080 00 | 1.100 00 | 1.120 00 | 1.150 00 |
| 2 | 0.541 62 | 0.545 44 | 0.553 09 | 0.560 77 | 0.576 19 | 0.591 70 | 0.615 12 |
| 3 | 0.370 65 | 0.374 11 | 0.381 05 | 0.388 03 | 0.402 11 | 0.416 35 | 0.437 98 |
| 4 | 0.285 29 | 0.288 59 | 0.295 23 | 0.301 92 | 0.315 47 | 0.329 23 | 0.350 27 |
| 5 | 0.234 18 | 0.237 40 | 0.243 89 | 0.250 46 | 0.263 80 | 0.277 41 | 0.298 32 |
| 6 | 0.200 18 | 0.203 36 | 0.209 80 | 0.216 32 | 0.229 61 | 0.243 23 | 0.264 24 |
| 7 | 0.175 96 | 0.179 14 | 0.185 55 | 0.192 07 | 0.205 41 | 0.219 12 | 0.240 36 |
| 8 | 0.157 86 | 0.161 04 | 0.167 47 | 0.174 01 | 0.187 44 | 0.201 30 | 0.222 85 |
| 9 | 0.143 84 | 0.147 02 | 0.153 49 | 0.160 08 | 0.173 64 | 0.187 68 | 0.209 57 |
| 10 | 0.132 67 | 0.135 87 | 0.142 38 | 0.149 03 | 0.162 75 | 0.176 98 | 0.199 25 |
| 11 | 0.123 57 | 0.126 79 | 0.133 36 | 0.140 08 | 0.153 96 | 0.168 42 | 0.191 07 |
| 12 | 0.116 03 | 0.119 28 | 0.125 90 | 0.132 70 | 0.146 76 | 0.161 44 | 0.184 48 |
| 13 | 0.109 68 | 0.112 96 | 0.119 65 | 0.126 52 | 0.140 78 | 0.155 68 | 0.179 11 |
| 14 | 0.104 28 | 0.107 58 | 0.114 34 | 0.121 30 | 0.135 75 | 0.150 87 | 0.174 69 |
| 15 | 0.099 63 | 0.102 96 | 0.109 79 | 0.116 83 | 0.131 47 | 0.146 82 | 0.171 02 |
| 16 | 0.095 58 | 0.098 95 | 0.105 86 | 0.112 98 | 0.127 82 | 0.143 39 | 0.167 95 |
| 17 | 0.092 04 | 0.095 44 | 0.102 43 | 0.109 63 | 0.124 66 | 0.140 46 | 0.165 37 |
| 18 | 0.088 92 | 0.092 36 | 0.099 41 | 0.106 70 | 0.121 93 | 0.137 94 | 0.163 19 |
| 19 | 0.086 15 | 0.089 62 | 0.096 75 | 0.104 13 | 0.119 55 | 0.135 76 | 0.161 34 |
| 20 | 0.083 68 | 0.087 18 | 0.094 39 | 0.101 85 | 0.117 46 | 0.133 88 | 0.159 76 |
| 21 | 0.081 46 | 0.085 00 | 0.092 29 | 0.099 83 | 0.115 62 | 0.132 24 | 0.158 42 |
| 22 | 0.079 47 | 0.083 05 | 0.090 41 | 0.098 03 | 0.114 01 | 0.130 81 | 0.157 27 |
| 23 | 0.077 67 | 0.081 28 | 0.088 71 | 0.096 42 | 0.112 57 | 0.129 56 | 0.156 28 |
| 24 | 0.076 04 | 0.079 68 | 0.087 19 | 0.094 98 | 0.111 30 | 0.128 46 | 0.155 43 |
| 25 | 0.074 55 | 0.078 23 | 0.085 81 | 0.093 68 | 0.110 17 | 0.127 50 | 0.154 70 |
| 26 | 0.073 19 | 0.076 90 | 0.084 56 | 0.092 51 | 0.109 16 | 0.126 65 | 0.154 07 |
| 27 | 0.071 95 | 0.075 70 | 0.083 43 | 0.091 45 | 0.108 26 | 0.125 90 | 0.153 53 |
| 28 | 0.070 81 | 0.074 59 | 0.082 39 | 0.090 49 | 0.107 45 | 0.125 24 | 0.153 06 |
| 29 | 0.069 77 | 0.073 58 | 0.081 45 | 0.089 62 | 0.106 73 | 0.124 66 | 0.152 65 |
| 30 | 0.068 81 | 0.072 65 | 0.080 59 | 0.088 83 | 0.106 08 | 0.124 14 | 0.152 30 |
| 31 | 0.067 92 | 0.071 79 | 0.079 80 | 0.088 11 | 0.105 50 | 1.123 69 | 0.152 00 |
| 32 | 0.067 10 | 0.071 00 | 0.079 07 | 0.087 45 | 0.104 97 | 0.123 28 | 0.151 73 |
| 33 | 0.066 33 | 0.070 27 | 0.078 41 | 0.086 85 | 0.104 50 | 0.122 92 | 0.151 50 |
| 34 | 0.065 63 | 0.069 60 | 0.077 80 | 0.086 30 | 0.104 07 | 0.122 60 | 0.151 31 |
| 35 | 0.064 97 | 0.068 97 | 0.077 23 | 0.085 80 | 0.103 69 | 0.122 32 | 0.151 13 |